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**Large-scale snowpack estimation using ensemble data assimilation  
methodologies, satellite observations and synthetic datasets**

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**Large-scale snowpack estimation using ensemble data assimilation  
methodologies, satellite observations and synthetic datasets**

**by**

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## **Dedication**

I dedicate this thesis to my parents and my wife.

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# **Large-scale snowpack estimation using ensemble data assimilation methodologies, satellite observations and synthetic datasets**

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This work focuses on a series of studies that contribute to the development and test of advanced large-scale snow data assimilation methodologies. Compared to the existing snow data assimilation methods and strategies, which are limited in the domain size and landscape coverage, the number of satellite sensors, and the accuracy and reliability of the product, the present work covers the continental domain, compares single- and multi-sensor data assimilations, and explores uncertainties in parameter and model structure.

In the first study a continental-scale snow water equivalent (SWE) data assimilation experiment is presented, which incorporates Moderate Resolution Imaging Spectroradiometer (MODIS) snow cover fraction (SCF) data to Community Land Model (CLM) estimates via the ensemble Kalman filter (EnKF). The greatest improvements of the EnKF approach are centered in the mountainous West, the northern Great Plains, and the west and east coast regions, with the magnitude of corrections (compared to the use of model only) greater than one standard deviation (calculated from SWE climatology) at

given areas. Relatively poor performance of the EnKF, however, is found in the boreal forest region. In the second study, snowpack related parameter and model structure errors were explicitly considered through a group of synthetic EnKF simulations which integrate synthetic datasets with model estimates. The inclusion of a new parameter estimation scheme augments the EnKF performance, for example, increasing the Nash-Sutcliffe efficiency of season-long SWE estimates from 0.22 (without parameter estimation) to 0.96. In this study, the model structure error is found to significantly impact the robustness of parameter estimation. In the third study, a multi-sensor snow data assimilation system over North America was developed and evaluated. It integrates both Gravity Recovery and Climate Experiment (GRACE) Terrestrial water storage (TWS) and MODIS SCF information into CLM using the ensemble Kalman filter (EnKF) and smoother (EnKS). This GRACE/MODIS data assimilation run achieves a significantly better performance over the MODIS only run in Saint Lawrence, Fraser, Mackenzie, Churchill & Nelson, and Yukon river basins. These improvements demonstrate the value of integrating complementary information for continental-scale snow estimation.

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# Chapter 1: Introduction

## 1.1 IMPORTANCE OF LARGE-SCALE SNOWPACK ESTIMATION

Snowpacks are an important component of the Earth's climate system, serving as critical freshwater reservoirs and playing a unique role in the global water and energy cycles. Of all the large-scale (e.g., regional to continental to hemispheric scale) terrestrial features, snowpacks have the largest fluctuations in space and time, with the area ranging from 7% to 40% in the Northern Hemisphere during the annual cycle. Associated with these fluctuations are variations in the surface albedo and radiation balance, turbulent heat exchange with the atmosphere, water vapor input to the atmosphere through sublimation and evaporation, and water input to the soil and river systems through melt. Consequently, an accurate estimation of snow water equivalent (SWE), snow depth, and other snowpack properties on a large-scale is important for many active research areas, which include:

(1) Hydrological prediction and water resources management. Much of the global population (one-sixth, according to Barrett et al., 2005) lives in areas where streamflow is dominated by snowmelt runoff. Therefore, a reliable description of spatial and temporal variability of snowpack is critical for the estimation of freshwater availability in those regions.

(2) Assessment of climate change impacts in cold regions. Global climate change may have profound impacts on land hydrological processes. However, the impacts on snowpack variation in large time scales (e.g., inter-annual to decadal scale or larger) are

still poorly understood at the global scale, except for some assessments for areas with abundant snow data (e.g., western U.S. (Mote et al., 2005)).

(3) Characterization of climate-snowpack linkages, as related to atmospheric general circulation and some low-frequency climate system modes. Continental-scale snow anomalies can lead to considerable variations in the atmosphere (e.g., Cohen and Entekhabi 2001; Gong et al., 2002), and in turn can be controlled by atmospheric temperature and/or general circulation (e.g., Derksen et al., 1997; Clark and Serreze, 2000). Low-frequency climate modes, although largely produced from ocean-atmosphere interaction, are often seen over land (including snowpack variability). Recent research (Ge and Gong, 2009) demonstrated a significant relationship between North American snow depth and the Pacific Decadal Oscillation (PDO) and the Pacific-North American (PNA) pattern. As highlighted in their work, characterization of these relationships hinges on a newly available continental-scale snow depth dataset (Dyer and Mote 2006).

In addition to the above mentioned areas, large-scale snowpack information is also valuable to many other applications, for example, evaluation of coupled Global Climate Models (GCMs) in terms of their ability to represent observed snow dynamics (e.g., Frei and Gong, 2005) and the derivation of initial land data for climate and meteorological numerical simulation (e.g., Souma and Wang, 2009).

## **1.2 LARGE-SCALE SNOWPACK VARIABILITY MONITORING**

Snowpack variability is complex in both temporal and spatial scales. Temporally it mainly involves accumulation and melting stages. At accumulation stage, the dominant

processes include precipitation, sublimation, wind blowing, etc. At melting stage, the dominant processes include solar radiation, canopy-snow interaction, snow-albedo feedback, etc. Spatially, the distribution of snowpack can show different patterns across various scales. For example, at 1~100 meters scale, snow distribution could be controlled by distributions of leaf area, plant type composition, canopy density (Liston, 2004). At 1~10km scale, snow variability was found (e.g., Donald et al., 1995; Pomeroy et al., 1998) to follow two-parameter log-normal distribution. Given the general interchangeability among specific distribution formats by fitting appropriate parameters, the snow variability at the above scale can be also characterized by other distributions, such as Poisson or Gamma distribution. In addition, field work (e.g., Shook and Gray, 1996; Deems et al., 2008) demonstrated that snow distribution has fractal property, indicating consistent driving processes running at multi-scales. The detail fractal feature can be function of local physiography and vegetation characteristics (Deems et al., 2008).

Currently, the task of monitoring large-scale snowpacks depends on ground (in situ) and satellite observations. These two approaches are briefly reviewed in this section, with additional discussion on their limitations (along with the strength of the data assimilation approach) in next section of this chapter. There are other complementary methods for snow monitoring, such as low flying aircraft scanning, which are not discussed here because their data are not used.

### **1.2.1 Ground measurements**

Ground surveys of snowpack properties, including SWE, snow depth, snow density, and grain size through well designed snow courses and/or operational meteorological

stations, is highly accurate compared to other approaches. In North America there are several ground survey programs that provide long-term snowpack monitoring over large areas. For example, the Snowpack Telemetry (SNOTEL, <http://www.wcc.nrcs.usda.gov/snow/>) is an extensive, automated system that collects snowpack and related climatic data in the western United States. Installed and maintained by the Natural Resources Conservation Service (NRCS), SNOTEL includes 730 sites in 11 states (including Alaska), most of which are located in remote high-mountain watersheds where access is difficult. The data from SNOTEL are delivered in near-real-time using meteor burst communications technology. Another example is the Canadian Daily Snow Depth and Snow Water Equivalent Database ([http://www.ccin.ca/datasets/snowcd/docs/1999/DOCUMNTS/INTRO\\_E.HTM](http://www.ccin.ca/datasets/snowcd/docs/1999/DOCUMNTS/INTRO_E.HTM)) which consists of daily ruler measurements of snowpack taken by Meteorological Service of Canada (CMC) observers. The dataset extends from late 1800s to after 2000, although most of the data were collected after 1950. At their peak in the early 1980s, there were over 1700 snow course observations per year in the database. The number of associated snow course stations sharply declined after 2000.

### **1.2.2 Satellite observations and inversion**

As a promising alternative of ground snow measurements, satellite observations have been explored by the research community in recent decades. This remotely sensed information is becoming a major tool for large-scale snow characterization, mainly owing to its superb spatial coverage (usually at continental to global scale), near-real-time delivery, and many other cost-effective features.

Different physical mechanisms are used by these space-born sensors for monitoring various features of snowpacks. In particular, the areal extent of snowpack can be detected and monitored by visible/infrared (VIS/IR) sensors because the reflectivity of snow in these bands is unique compared with other types of land cover (Hall et al., 2002). The passive microwave sensors can detect thermal radiation from snow, from which they can infer snow mass and/or depth (as well as grain size, density and other snowpack internal properties) information (Derksen et al, 2003; Tedesco et al, 2004; Foster et al, 2005). Other technologies include active microwave sensing (e.g., Tsang et al., 2007), which can be used to quantify the areal extent of snowpack.

All these remote sensing approaches consist of some “inversion” algorithms, which map actual signals obtained at satellites (e.g., electromagnetic fields at ground) to those variables of interest (e.g., SWE, snow depth). These inversions depend on various assumptions. Some of these algorithms are relatively simple and straightforward, for example, the normalized difference of snow index (NDSI) for snow areal retrieval (Hall et al., 2007), and linear regression of brightness temperature for snow depth retrieval (Derksen et al, 2003). Other algorithms involve more complicated mechanisms, for example, using radiative transfer models to derive snow mass and snow depth information from passive microwave observations (e.g., Tedesco and Kim, 2006). Each inversion method may have its own strengths and weaknesses, depending on the geophysical properties of the location where it is applied, and the corresponding assumptions on which it relies.

### 1.3 SNOW DATA ASSIMILATION

Ground or satellite measurements alone cannot fully meet the need for accurate characterization of snowpack at large-scale for a number of reasons involved. The value of in situ observations is constrained by its spatial representativeness, which is usually at the order of 10~100 m and a function of local topography, vegetation, wind, etc (e.g., Liston, 2004). Accordingly, the use of point scale ground measurements to delineate macro-scale (10~100 km in grid size) snow variability can introduce significant error (e.g., Pan et al., 2006). Satellite measurements, on the other hand, are usually not a direct reflection of snowpack hydrological properties. The estimates from inverting satellite signals can often be contaminated by some unresolved factors, such as the complex topography, vegetation and meteorological conditions (e.g, clouds). The error associated with this inversion process can be very complicated, with its magnitude varying from location to location and from season to season. Before being widely applied in different climatic and/or hydrological applications, these satellite products need to be comprehensively evaluated (Foster et al, 2005) regarding their application scope and error quantification. However, regional to continental evaluation of satellite retrievals can be very difficult, considering the lack of benchmark data (independent high-quality observations) at these scales. In addition, the spatial and temporal scales of these satellite observations could significantly differ from (usually coarser than) those required by applications because of sensor and orbit limitations.

Given these limitations of in situ and remote sensing snowpack observations, snow data assimilation has emerged in recent years as an innovative approach (Andreadis and Lettenmaier, 2006; Clark et al., 2006; Durand and Margulis 2007, 2008). Its goal is to

more accurately characterize snowpack variability across a variety of scales. Its central idea is to combine snow observations with model estimates. Here model refers to the numerical simulation of snowpack physical processes driven by meteorological forcing. There are a large number of studies about developing numerical models to estimate snowpack (Jordan, 1991; Koren, 1999; Niu and Yang, 2004). In general, snow models are subject to various errors, such as forcing (e.g., precipitation and temperature data) error, physical parameterization (structural) error, and parameter error. Schemes (e.g., data assimilation) that optimally integrate models and observations offer promises to reduce errors in each of them. In its early stage, snow data assimilation used a direct insertion method (Liston, 1999; Rodell, 2004), which assumes snow observations are perfect. Recent research recognized that more sophisticated methods are needed to derive weights that combine models and observations and represent their individual uncertainty, and fit other requirements such as sequential estimation. The Kalman type algorithms (e.g., the Kalman filter) and ensemble (Monte Carlo) approaches (ensemble Kalman filter (EnKF), Evenson, 1994) were introduced to address this need, particularly for the purpose of accurately representing the temporally and/or spatially varying error statistics of models and/or observations. In addition, various kinds of ensemble snow data assimilation schemes have been developed to accommodate distinct properties of different snow observations (Andreadis and Lettenmaier, 2006; Durand and Margulis 2007). These include the data from the inversion of the satellite signal, and radiance (both VIS/IR and microwave) observation directly obtained by satellite.

## **1.4 MOTIVATION FOR DEVELOPING ADVANCED LARGE-SCALE SNOW DATA ASSIMILATION SCHEMES**

In general, the current snow data assimilation schemes are not adequate for large-scale snowpack estimation. Most previous ensemble snow data assimilation experiments were designed at watershed or smaller scale, and so many complex issues that could be critical for large-scale retrieval have been neglected. In particular, the impacts of different climatic (e.g., temperature and precipitation regime, and wind pattern) and geographical (e.g., topography, vegetation) conditions on the data assimilation performance are especially important but not well understood. These impacts can only be explored and assessed over a large-scale region. Also the robustness of data assimilation algorithms, such as the observational operator (a function that relates an observation with a model estimate) and the error parameters in the EnKF, has not been adequately tested in previous research. The spatial heterogeneity of snowpack and land cover, together with other complexities involved for a large domain, may impose additional requirements on these algorithms. Consequently, the development and evaluation of new observational functions or other components may become necessary.

The motivation for the research in this dissertation not only came from the above mentioned “large domain” problem, but also from other theoretical and practical considerations pertinent to snow estimation. In particular, the effects of parameter and model structural error on snow data assimilation are not discussed in the literature, which limits the value of proposed algorithms because they often need to be applied in untested areas where both the true (or most appropriate) model structure and parameters are unknown. This deficiency can be especially evident in large-scale applications, because

the proper parameter (even structure) may be spatially varying and difficult to estimate. It is necessary to quantify and mitigate the impacts of these errors with some “flow-dependent” approach (which means running concurrently with model propagation).

Furthermore, my research has been motivated by the fact that only limited satellite information (single sensor observation) has been considered in traditional large-scale snow data assimilation studies. There are always drawbacks inherent to any given type of observation (e.g., Moderate Resolution Imaging Spectroradiometer (MODIS) observed snow cover fraction (SCF)) and their negative effects (e.g., systematic error) can be preserved in associated data assimilation products. As advocated in some synthetic radiance research (e.g., Durand and Margulis 2006, 2007), assimilation of complementary information from different radiometer sensors or frequencies can mitigate the problem and lead to better snow estimates. However, these studies focused on assimilating synthetic radiometer observations (which include the brightness temperature and/or albedo at microwave and/or VIS/IR bands) at relatively small scale. One problem is that their effectiveness could be influenced by high standing vegetation (e.g, forest), as well as the patchy pattern of snow cover because the thermal emission from vegetation and soil can dominate the radiometer signal (Andreadis et al., 2008). In this regard a relatively coarse grid (as commonly adopted in large-scale simulations) blending multiple vegetation types and snow cover/free patches, could affect performance of these approaches. In addition these multi-frequency algorithms are complicated by the “many-to-one” problem (the radiometric signal is a function of many snowpack properties like SWE, snow depth, snow density, grain size, etc). The estimation of a particular property (e.g., SWE) could be significantly influenced by errors

in quantification of others (e.g., grain size) (Andreadis et al., 2008). Although the snowpack radiative transfer models (RTM) that have been incorporated that can simulate these properties (and their errors), their ability (e.g., in grain size simulation) to cope with geographic heterogeneity (e.g., snowpack or vegetation variability) on a large-scale has not been adequately evaluated in the literature. Another caveat associated with the multi-frequency algorithms is that microwave bands are generally less effective in estimating snowpack with liquid water. Novel approaches are needed that can integrate further complementary observations and accommodate specific features confronted in large-scale application, and also avoid the problems of multi-frequency radiometer assimilation.

This dissertation is a first attempt to address all the limitations raised above. It focuses on the scientific question of how to estimate large-scale snowpack properties accurately through advanced ensemble data assimilation methods and multiple types of observations. These investigations have not been previously performed, so some “proof-of-concept” studies are given in this dissertation. In brief, my research in this dissertation improves on previous work by 1) using a newly developed observational operator for a North American data assimilation experiment, in which various climatic and geographic zones are covered and their impacts to the EnKF performance are comprehensively evaluated; 2) performing simultaneous state and parameter estimation in a synthetic EnKF framework, and investigating the dependence of parameter estimation on model structure error is investigated; 3) blending observations from two sensors (measuring SCF and terrestrial water storage (TWS), respectively) into a North American snow data assimilation framework that integrates two differing ensemble methods, and factors that

can hamper multi-frequency radiometer assimilation are generally circumvented by the unique features of MODIS and GRACE observations.

## **1.5 OUTLINE OF THIS DISSERTATION**

Chapter 2 presents a continental-scale SWE data assimilation experiment, which integrates MODIS SCF data with Community Land Model (CLM) estimates via the EnKF. It uses a newly available observational function, and the performance of data assimilation is comprehensively evaluated over various climatic and geographical environments. Chapter 3 provides a group of synthetic EnKF experiments that jointly estimate state and parameter. It incorporates a parameter estimation scheme and evaluates its merit for snowpack estimation. Also Chapter 3 provides a preliminary assessment of the impacts of model structure error on the performance of parameter estimation. Chapter 4 develops a multi-sensor snow data assimilation system over North America. It integrates both Gravity Recovery and Climate Experiment (GRACE) TWS and MODIS SCF information into CLM using the ensemble Kalman filter (EnKF) and smoother (EnKS). Chapter 5 summarizes the major finds, and presents possible directions for future research.

## **Chapter 2: Enhancing the estimation of continental-scale snow water equivalent by assimilating MODIS snow cover with the Ensemble Kalman Filter<sup>1</sup>**

### **2.1 ABSTRACT**

SWE datasets at continental-scale are generally not available, although they are important for climate research. This study investigates the feasibility of a framework for developing such needed datasets over North America, through the EnKF approach that assimilates the snow cover fraction observed by the MODIS into the CLM. I use meteorological forcing from the GLDAS to drive CLM, and apply a snow-density based observation operator. This new operator is able to fit the observed seasonally varying relationship between the snow cover fraction and the snow depth. Surface measurements from Canada and Advanced Microwave Scanning Radiometer-Earth Observing System (AMSR-E) estimates (in particular regions) are used to evaluate the assimilation results. The filter performance including its ensemble statistics in different landscapes and climatic zones is interpreted. Compared to the open loop, the EnKF method more accurately simulates the seasonal variability of SWE and reduces the uncertainties in the ensemble spread. Different simulations are also compared with spatially distributed climatological statistics from a regrided dataset, which shows that the SWE estimates from the EnKF are most improved in the mountainous West, the Northern Great Plains, and the West and East Coast regions. However in boreal forest the performance of the

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<sup>1</sup>Substantial portions of this chapter were previously published in Su, H., Z.-L. Yang, G.-Y. Niu, and R. E. Dickinson (2008), Enhancing the estimation of continental-scale snow water equivalent by assimilating MODIS snow cover with the ensemble Kalman filter, *J. Geophys. Res.*, 113, doi:10.1029/2007JD009232. The References section contains full citations for all articles referenced here.

EnKF is degraded. Limitations of the assimilation system are analyzed and the domain wide innovation mean and normalized innovation variance are assessed, yielding valuable insights (e.g., about the misrepresentation of filter parameters) as to implementing the EnKF method for the estimation of large-scale snow properties.

## **2.2 INTRODUCTION**

Snow is a very important component of the climate system that controls surface energy and water balances. Its high albedo, low thermal conductivity, and properties of surface water storage impact regional to global climate, as has been documented in numerous observational and modeling studies (e.g., Barnett et al., 1999; Yang et al., 2001; Gong et al., 2003).

The various properties characterizing snow are highly variable and so have to be determined as dynamically active components of climate. These include SWE, density, and SCF. However, on large spatial scales the properties of snow are not easily quantified either from modeling or observations. For example, station based snow measurements often lack spatial representativeness, especially in regions where the topography, vegetation and overlaying atmosphere produce considerable heterogeneity of the snowpack distribution (Liston, 2004). In recent decades SWE and snow depth products have been available from passive microwave sensors (e.g., AMSR-E). Nevertheless, since the microwave signature of snowpack depends on a number of varying features (e.g., snow grain size, density, liquid water content, vegetation, etc), direct estimation (e.g., linear regression) of snow parameters that does not include these dynamic properties can be plagued by complicated errors (Grody et al. 1996; Forster et al., 2005;

Dong et al., 2005). In addition, snow estimation from land surface models (LSMs) can have large uncertainties partly due to their imperfect parameterizations of snow dynamics and the errors in their meteorological forcing. Since neither observations nor LSMs alone are capable of providing adequate information about the time space variability of continental snow properties, it becomes necessary to combine their information as achievable through the technology of land surface data assimilation (e.g., McLaughlin, 2002; Houser et al., 1998; Reichle et al., 2002; Margulis et al., 2002; Crow et al., 2003). Such assimilation can effectively reduce estimation uncertainties through optimally combining the information from both LSMs and observations.

A number of studies have initially applied data assimilation methods for deriving snow properties (e.g., SWE) (e.g., Rodell and Houser, 2004; Slater and Clark, 2006; Dong et al., 2007; Durand and Margulis, 2006, 2007). Among these studies the ensemble Kalman filter (EnKF) has been used to combine the observed SCF information with the model simulated SWE (e.g., Andreadis and Lettenmaier, 2006; Clark et al., 2006). The SWE, a prognostic variable derived from the snow mass balance, has been optimally updated through its correlative relationship with other more readily observed quantities (e.g., SCF). However, most of these studies were confined to small river basins or plot scales, and few have addressed continental or hemispheric applications where the snow effects on the atmospheric circulation may be pronounced and where the simulation and observational uncertainties of snow properties may depend on different landscape properties and climate zones. Thus, more optimal methods of estimation on these scales are needed. Further, only limited (some very simple) snow physical models and observational functions were involved in previous studies, and the performance of the

data assimilation was inadequately evaluated for operational application. Therefore the feasibility of data assimilation methods for the retrieval of such properties on a large-scale has not yet been decisively demonstrated.

The purpose of this paper is to assess the feasibility of the EnKF methodology and a new observational operator for the retrieval of SWE on a continental-scale. It demonstrates that the SCF as measured by the MODIS instrument can be assimilated into continental SWE fields simulated by a highly complex LSM - the National Center for Atmosphere Research (NCAR) CLM. Section 2 gives a brief description of the EnKF, the CLM, and a recently developed SCF observational operator. Datasets and experiments are discussed in Section 3. The results analyses are given in Section 4. Section 5 discusses limitations of the proposed method, with concluding remarks in Section 6.

## **2.3 METHODOLOGY**

The EnKF based snow data assimilation system used in this paper has two essential components: (1) an LSM (including its snow model) that evolves related state variables in an ensemble approach and provides background error statistics; (2) the Kalman filter updating scheme that combines the physical simulations with observations using an observational function.

### **2.3.1 The LSM**

The CLM (e.g., Bonan et al., 2002, Oleson et al., 2004) numerically simulates energy, momentum, and water exchanges between the land surface and the overlying atmosphere at each computational grid. It employs 10 soil layers to resolve soil moisture

and temperature dynamics and uses plant functional types (PFTs) to represent sub-grid vegetation heterogeneity. The CLM snow model simulates a snowpack with multi-layers (1-5 layers) depending on its thickness, and accounts for processes such as liquid water retention, diurnal cycling of thawing–freezing, snow melting, and surface frost and sublimation. Heat and water are transported between its adjacent snow layers, also between its top layer and the overlying canopy and/or the atmosphere. Snow layers may be combined or divided every time step to ensure a realistic representation of snow physics and numerical stability. The grid averaged albedo is area weighted using a snow cover fraction. The CLM also explicitly incorporates densification processes (e.g., destructive or equitemperature metamorphism, compaction by snow overburden, and melt metamorphism) following Anderson (1976), for calculating snow density of each snow layer. This multi-layer approach is found to significantly enhance the simulation quality, correcting the previously underestimated snow mass and early time of melting that is obtained in a single layer model (Yang and Niu, 2003).

The SWE propagation equation in the CLM can be summarized as follows:

$$x_t = x_{t-1} + (P_t - E_t - M_t)dt \quad (2.1)$$

where  $x_t$  and  $x_{t-1}$  denote the SWE in a sub-grid tile of a grid at time step  $t$  and  $t-1$ , respectively.  $P_t$  represents the solid precipitation provided by measurements,  $E_t$  represents the loss of snow due to sublimation and evaporation, and  $M_t$  represents the melting of snow. The latter two quantities are calculated from the model. By adding together layers, the sub-grid tile total SWE can be obtained as:

$$x_t = \sum_{i=0}^{snl+1} (w_{ice,i} + w_{liq,i}) \quad (2.2)$$

where  $w_{ice,i}$  and  $w_{liq,i}$  denote solid and liquid water mass in layer  $i$ , and  $snl$  denotes the number of layers. Each of these terms has its own mass balance equation similar to (2.1).

### 2.3.2 The EnKF and its implementation

The EnKF was first introduced by Evensen (1994) as a Monte Carlo approach to accomplish the Kalman filter updating scheme in numerical modeling systems. It is also related to the theory of Stochastic Dynamic Prediction (Epstein, 1969). Detailed descriptions and discussions of this method in various contexts are available in the literature (e.g., Evensen, 1994, 2003; Reichle et al., 2002; Hamill, 2006).

Using the model physical configuration described in 2.1, the EnKF is implemented as follows: (a) each sample (ensemble member) of model state variables is propagated at every time step using prognostic equations like equation (1); these simulations are driven by perturbed meteorological forcing data (the method of sampling forcing is introduced in Section 3); (b) each sample of the LSM forecast variables is updated (e.g., SWE in this study) using Equation (3):

$$x_{it}^{j'} = x_{it}^j + K_t(y_t - H(x_{it}^j) + v_t^i) \quad (2.3)$$

where  $x_{it}^{j'}$  denotes the filter updated states (e.g., SWE),  $x_{it}^j$  the model simulated states,  $i$  the ensemble index,  $j$  the tile index in a given grid,  $y_t$  the observation in that grid (SCF in this study), and  $H$  the observational operator (to be described subsequently).

$v_t^i$  is randomly drawn from a Gaussian distribution (with zero mean and the variance equal to  $R_t$  as described below) to ensure an adequate spread of the analysis ensemble members (Burgers et al., 1998).

The  $K_t$  in Equation (2.3), which is the ‘‘Kalman gain’’, takes the form of:

$$K_t = P_t^b H^T (HP_t^b H^T + R_t)^{-1} \quad (2.4)$$

where  $P_t^b$  represents the error covariance of simulated ensembles;  $R_t$ , the error covariance of observed SCF. The latter is a prescribed value in this study. The model state  $x_{i,t}^j$  is a sub-grid tile based value, while the observational statistic  $y_t$  (SCF) is defined at a grid. The model is compared with observation using  $H(x_{i,t}^j)$ , the summation of model predicted SCF over all tiles in the specified grid:

$$H(x_{i,t}^j) = \sum_{e=1}^n h(x_{i,t}^e) \quad (2.5)$$

where  $e$  loops all the tiles in the grid and  $h(x_{i,t}^e)$  denotes the observational operator at each tile weighted by the tile area. It should be emphasized that the above implementation does not directly assimilate SWE measurements nor does it directly update the CLM simulated SCF. Instead the implementation updates the CLM simulated SWE with SCF observations, which requires an observation function linking the state variable SWE and the MODIS observed SCF as described in section 2.3.3.

The updated SWE or  $x_{i,t}^j$  in Equation (2.3) represents the total snow mass for the entire snowpack, which must be disaggregated into ice and liquid parts for each of the layers according to (2.2). A simple rule is designed for this allocation. Snow mass is

always added or subtracted in the layers starting from the top, and the ratio between solid and liquid water components is kept the same after each allocation (this is a simple assumption, since there is no information about liquid/solid ratio from SCF observation). The total snow mass and energy are conserved as the layers are separated or combined, and the procedure follows the existing parameterization in the snow layering scheme (Oleson et al., 2004). The snow depth in each layer is also updated accordingly. In CLM the snow density is calculated from the snow water equivalent and snow depth. Therefore it can be indirectly updated with these two variables.

### 2.3.3 The Observational operator

A snow depletion curve (SDC) that parameterizes the relationship between regional averaged SWE and SCF has been used to optimize SWE estimates in recent ensemble based data assimilation experiments (e.g., Andreadis and Lettenmaier, 2006; Clark et al., 2006). Its basic philosophy is that the accumulation or ablation of the unevenly distributed snow determines both SWE and SCF such that both are highly correlated (Yang et al., 1997; Luce et al., 1999, 2004; Liston, 2004). Accordingly, any observed SCF information should contribute to the estimation of SWE.

A new SCF parameterization has been developed by Niu and Yang (2007) using the snowpack density to account for the large-scale depletion pattern and its temporal variability. This SCF scheme, which is used in this study to transfer observational information into the CLM, takes the following mathematical form:

$$SCF = \tanh\left(\frac{h_{sno}}{2.5z_0(\rho_{sno} / \rho_{new})^\alpha}\right) \quad (2.6)$$

where SCF is the fractional snow cover,  $h_{sno}$  and  $z_0$  are the spatially averaged snow depth (or rewritten to be a function of SWE and snow density) and the ground roughness length, respectively.  $\rho_{new}$  is a prescribed fresh snow density with adjustable values depending on local conditions.  $\rho_{sno}$  is the model calculated snow density. The curve shape parameter  $\alpha$  is tunable and assumed to be controlled by several factors including scale and, hypothetically, the grid-specific physiographic properties.

The snow depth and snow cover relationship (Equation 2.6) differs from any of the parameterizations reviewed by Liston (2004). Instead of one static curve for the entire snow season, it provides a family of snow depletion curves with each such curve representing a non-linear relationship between SCF and snow depth characterized by a unique value of snowpack density (Figure 2.1). Further, this SCF operator accommodates the multi-layer structure of CLM snow model by using the layer integrated snow density in the Equation (6). Niu and Yang (2007) evaluated the validity of this seasonally varying SCF scheme using long term (1979-1996) ground based data of SWE and snow depth in North America (Brown et al., 2003) and satellite observed monthly SCF from Advanced Very High Resolution Radiometer (AVHRR). Equation (6) performs reasonably well in terms of reconstructing the relationship between SCF and snow depth in large river basins in North America.

To apply Equation (6) for data assimilation, it is needed to calibrate  $\rho_{new}$  and  $\alpha$  based on field measurements or other high-quality datasets at hand. This study sets  $\rho_{new}$  to  $100 \text{ kg/m}^3$  (Dingman, 2002) for each grid in the model domain. The value ‘2.5’ in Equation (2.6) is itself tunable, but it is here assumed to be a constant for simplicity.

My experiments use gridded North America snow datasets (1979-1996) (Brown, 2003) and AVHRR monthly SCF data to calibrate the shape parameter  $\alpha$ . The reason to use the AVHRR SCF dataset is that it covers the same time period as the data in Brown et al. (2003). These datasets are regridded to  $1^\circ$  by  $1^\circ$  resolution, the resolution used for the off-line model. An optimal  $\alpha$  is obtained by requiring the SCF derived from Equation (6) to best fit the AVHRR observed SCF in a least mean square error sense. The Genetic Algorithm (GA) is used to efficiently search for this optimal parameter. I account for the region-specific variability of  $\alpha$  by considering three landscape categories: (1) flat regions with low standing vegetation (e.g., the prairie in the Northern Great Plains); (2) flat regions with high standing vegetation (e.g., the boreal forest of Canada) and (3) mountainous regions (e.g., the Rocky Mountains). This approach to representing heterogeneity of SDC is comparable to that of Liston (2004), which used a statistical distribution to characterize SDC and retrieve related parameters (e.g., CV in Liston (2004)) based on the physiographic properties of a geographic region to represent.

Three regions in North America have been used to represent the above landscape categories, each large enough to retrieve the optimal value of  $\alpha$ . The calibrated  $\alpha$  (using observations from 1979 to 1993) and correlation coefficient between reconstructed and observed SCF in the validation period (using observations from 1994–1996) are given in Table 2.1. Table 2.1 shows that  $\alpha$  is slightly less than one for the flat and low vegetation region, greater than two for the flat and high vegetation region, and in between over mountainous regions.

## 2.4 EXPERIMENTAL SETUP AND DATASETS

My experiments use near surface meteorological forcing variables from the Global Land Data Assimilation System (GLDAS) at  $1^\circ \times 1^\circ$  resolution (Rodell et al., 2004) to drive CLM. The GLDAS forcing data are observationally derived fields including precipitation, air temperature, air pressure, specific humidity, shortwave and longwave radiation. The vegetation and soil parameters from finer resolution raw data of CLM2.0 as used in previous studies (Bonan et al., 2002; Niu et al., 2005) are aggregated. CLM is run from January 2002 to June 2004, spanning the time period during which the MODIS retrieved SCF is available.

The GLDAS precipitation and temperature fields are perturbed in order to account for uncertainties in these model inputs to the snow dynamics. The samples of precipitation forcing are derived by multiplying the GLDAS values by spatially correlated log-normal random fields (with zero mean and unit variance), as described in Nijssen and Lettenmaier (2004). The e-folding scale of horizontal error correlations are assumed to be  $1^\circ$  in latitude/longitude coordinates, to provide the spatial covariance of forcing uncertainties. The relative error is defined at 50% in the log-normal distribution approach. Temperature ensembles are produced in the same way, except that typical normal random fields are applied to mimic true uncertainties, with zero mean and  $3^\circ\text{C}$  standard deviation. The ensemble size is set to 25, a compromise between computational affordability in the large land assimilation system and the filter effectiveness. Previous studies (e.g., Reichle et al., 2002; Andreadis and Lettenmaier, 2006) showed reasonable performance for the EnKF with this ensemble size.

MODIS observed snow cover fraction is assimilated into the CLM. MODIS uses 36 spectral bands to retrieve land surface properties. Its snow mapping algorithm detects land snow fraction using NDSI (Hall et al., 1995), and has the ability to distinguish between snow and cloud (Hall et al., 2002). The spatial resolution of SCF data from MODIS can be as high as 500 m but the product applied in this research is MOD10C1 with 0.05° resolution (Hall et al., 2002). I determine from the 0.05° cells, a weighted average at 1° resolution using the CMG confidence indices (Hall et al., 2002), assuming that the raw data SCF is unchanged by cloud obscuration. A threshold of 50% for the cloud cover is used to determine whether or not the SCF observation is used in the corresponding grid. This value is reasonable in that it does not have large negative effects on the filter performance compared to a stricter criteria, while rendering the system a relative increase in the SCF data frequency. The model is spun up to November 2002, and after that the MODIS SCF data sets are assimilated.

The MODIS SCF has errors whose standard deviation varies seasonally and geographically. Accurate characterization of the MODIS SCF error structure is beyond the scope of this study. An extensive literature search (e.g., Klein and Barnett, 2003; Simic et al., 2004; Brubaker et al., 2005; Hall and Riggs, 2007) indicates that it is fairly reasonable to assume the MODIS error at 10% in this particular study. Using this simple, stationary error criteria is also consistent with previous research (e.g., Andreadis and Lettenmaier, 2006). To account for parameter errors, a Gaussian error distribution with zero mean and 10% (based on nominal value in Table 1) standard deviation is prescribed for  $\alpha$  in Equation (2.6).

High-quality, spatially distributed ground SWE data at the continental-scale are generally not available as independent datasets for validation. Furthermore, since the snow density is simulated to be a time-dependent variable as considered in Equation 2.6, the abundant measurements of snow depth across North America (e.g., the NOAA Coop measurements) may not be directly applied as a benchmark for evaluating the SWE. Another limitation is the requirement that GLDAS forcing data overlap with MODIS observations, precluding their use for long-term simulations.

Based on these considerations, two independent observational sources are used to evaluate the assimilated continental-scale SWE fields. The first source is the ground measurements in Canada (Canadian Snow CD, 2000) which contain snow course surveyed SWE data over recent decades. The Canada snow course data are mainly located in river basins in southern Canada (Canadian Snow CD, 2000; Brown et al., 2003) encompassing different topographic and vegetative types. The measurements from winter 2002 to summer 2003 (overlapping with the CLM integration period) are scattered in western mountainous regions and southern flat regions, with a relatively small portion of area in the central southern prairie region. The other source is AMSR-E derived SWE data. AMSR-E (flown on board the NASA Aqua satellite) is a passive microwave radiometer with a wide range of frequencies (from 6.9–89 GHz), which can provide spatially and temporally continuous SWE estimation with adequate resolution for global analyses. These SWE estimates may have large errors in mountainous regions, forests, and where the snow is wet (e.g., Dong et al., 2005; Foster et al., 2005). Under certain circumstances (e.g., for low vegetation flat regions where snow is dry and shallow) the snow grain size and snow density assumed in the retrieval algorithm are relatively

reliable (e.g., the Northern Great Plains), the passive microwave retrieved SWE can be relatively accurate (Brubaker et al., 2001; Mote et al., 2003; Foster et al., 2005).

## **2.5 RESULTS**

### **2.5.1 Initial evaluation of the assimilated SWE dataset**

#### ***2.5.1.1 Comparison with ground observations***

Distributed observations in the Canadian prairie region are limited, but they are still suitable for my evaluation. Figure 2.2 shows the inter-station averaged measurements and their simulation counterparts within the region of 52°–54°N, 112°–114° in the 2002–2003 cold season. This comparison is rather representative in my assessing the assimilation quality for several reasons. First, it illustrates the relatively low frequency of ground observations, though the accumulation and melting stages are clearly displayed. Second, it represents some typical benefits through incorporating the SCF information into the CLM simulation in broad prairie regions. Figure 2.2 shows that the assimilated SWE values at the peak and melting stage are elevated to value closer to the observations. The extent to which the SWE is adjusted changes from place to place, determined by the weighting of model forecasted SCF and MODIS observed SCF according to the ensemble error statistics. In this particular case, the CLM predicted SCF is lower than that from the MODIS observations, and the filter partially corrected this difference during the assimilation cycles. Although only limited ground validation are provided here, it is argued that these analyses are consistent with the purpose in current research, which is to obtain a qualitative assessment on the proposed methodology.

### ***2.5.1.2 Comparison with passive microwave sensor retrieved data in selected regions***

Global SWE estimates from AMSR-E are available for the period of the CLM simulations in selected regions in North America. In the mid-latitude flat and low vegetation covered regions with a shallow snowpack, such as the Missouri River Basin and the North Central River Basin in the Northern Great Plains, AMSR-E derived daily SWE products can be utilized for assessing assimilation results. The comparisons are shown in Figure 2.3 and Figure 2.4. In each plot the daily time series of basin averaged snow water equivalent estimates are displayed, representing the EnKF assimilation run, the open-loop run (without assimilation) and the AMSR-E estimation, respectively. The figures indicate that the SCF assimilation significantly adjusts the snow estimation in these two basins and provides results more like the AMSR-E estimates. During December to February when the snow is likely to be dry in those regions, the AMSR-E retrieved SWE should have less uncertainty induced by liquid water content (Tedesco et al., 2006). During this time, the EnKF simulations better agree with satellite observations than over the melting period of March and April. Some new snow retrieval algorithms are currently under development for more accurately inverting or assimilating the passive microwave signals (e.g., Markus et al., 2006; Durand and Margulis, 2006). The above results may be further evaluated when those enhanced SWE estimations from space-borne sensors are available.

### ***2.5.1.3 Spatial patterns evaluation***

A ground based SWE regrided dataset from Brown et al. (2003) is used to further assess the distribution of EnKF assimilated SWE. Its climatological monthly

mean values and the associated anomalies facilitate us to interpret the difference between the model above (open loop) and EnKF simulations. Figure 2.5 shows the spatial distribution of monthly mean SWE (Feb, 2003) from different simulations, also the climatological mean (comparisons in other months have similar results). It is clear that in many regions the EnKF results and the climatology are more similar to each other than with the open loop, particularly in the Northern Great Plains, the middle-west mountainous regions, west coastal regions, and part of the east costal regions. However, the EnKF simulation has a high bias in the boreal forests, which may reflect the forest effects on MODIS SCF data, or the systematic error in the meteorological forcing.

Figure 2.6 shows the climatological standard deviation of SWE (Feb) as derived from the multi-year reanalysis dataset, and the absolute difference between each simulation (Feb, 2003) and the climatology. It demonstrates that in most of the regions where the EnKF and the climatology are in better agreement, their differences are within the range of inter-annual variability. Figure 2.7 further supports this conclusion using a temporal comparison of monthly mean SWE (from Nov, 2002 to Jun, 2003) in three small representative places within those regions summarized above. The error bars associated with the climatological mean denotes the standard deviations of monthly SWE. During the majority of the snow season (e.g., from Jan to Mar), the EnKF simulated monthly mean values are usually confined within the error bar. In contrast, the open loop simulations are often outside of the standard deviation range. Specifically in the first region ( $41^{\circ}$ – $42^{\circ}$  N,  $75^{\circ}$ – $80^{\circ}$ W) the difference between the open loop and the mean is nearly twice a standard deviation, which suggests the erroneousness of the open loop simulation there. The above spatial evaluation takes an indirect approach because

the multi-year data used to construct climatological statistics do not cover my simulation periods. However, it should be meaningful, partly because of the relative stability of climatological mean and standard deviation of large-scale SWE.

### **2.5.2 Assessing the behavior of ensemble filtering in large-scale snow assimilation**

The ensemble simulations of SWE at the CLM grid test sites with different land surface properties and climatic scenarios are presented in Figures 2.8, 2.9, 2.10. Figure 2.8 shows by the middle-latitude prairie grid that the model simulations have large spreads in both accumulation and melting periods. This variability is markedly reduced in the data assimilation run, especially in the melting season. Apparently, the GLDAS forcing terms do not fully constrain the timing of melting compared to the EnKF. Meanwhile the decrease in the EnKF ensemble variance demonstrates that the EnKF algorithm is implemented properly in this simulation.

Typical simulation results in boreal forest regions are shown in Figure 2.9. Similar to those displayed in Figure 2.8, the ensemble uncertainties are reduced in the EnKF run. However, the effect of altering the peak SWE is not as significant as that shown in Figure 2.8. These areas are covered by large extent of snow of a longer duration than that of the prairie regions (where the snow cover is usually ephemeral), so it is easier for the model simulated SCF to agree with MODIS observation, making the filter update more smooth.

The filter feature for a mountainous grid in Colorado (Figure 2.10) appears to be similar to those in Figures 2.8 and 2.9. However, it differs from the other two in that the timing of snow melt is largely altered in the EnKF simulation due to the incremental

information obtained from MODIS. Since it is a mountainous grid, this SWE updating is possibly useful for local water resources management.

## 2.6 DISCUSSION

The EnKF snow simulation system has several limitations. The snow model used and the other physical representations of land surface processes are not perfect. For example, although it has detailed vertical processes, the model does not adequately represent horizontal processes such as the bare soil effects and heat advection across snow patches. Both such limitations in the model physics and the systematic error in the meteorological forcing may result in a bias in the estimate of SWE and other quantities, which would make the filter system sub-optimal. The innovation mean (the mean of the difference between the observation and the model simulated corresponding variable (SCF in this study)), can be used to evaluate the bias in the data assimilation system. If the system is bias free and purely linear, the innovation mean should be zero (Dee, 1995). The domain wide innovation mean distribution for the winter season of 2002–3003 is shown in Figure 2.11. It shows that this statistic is significantly larger than its theoretical expectation (which is zero) in some grids in the western U.S. and the Northern Great Plains, indicating the model system has negative bias there. In contrast, its value is lower than zero in the north-east of North America, representing positive bias there. The bias in the snow assimilation system might be reduced by following the “cdf matching” method applied in Reichle and Koster (2004) in which the satellite observations are scaled to agree with the model simulated climatology (soil moisture in their paper). Other potential

approaches may include enhanced representation of model parameters and structures (system identification) in the data assimilation framework.

Determining the covariance of forcing errors is another important issue in land data assimilation systems (Reichle and Koster, 2003; Crow and Loon, 2006). The forcing error variances largely dictate the ensemble evolving path and the magnitude of the EnKF updates. The mean of normalized innovation variance can be used to detect the misrepresentation of model error in the data assimilation system, as defined below:

$$\varphi = E\left[\frac{\nu^T \nu}{HP_t^b H^T + R_t}\right] \quad (2.7)$$

where  $\nu$  represents the average of innovation over the ensemble members, and  $E[\ ]$  represents the temporal mean.

If the EnKF is used with optimal statistical conditions (e.g., linear models and observational operators, and additive Gaussian errors), and the model errors are perfectly represented by the ensemble statistics, then the mean of the normalized variance of the innovation should =1.0 (Dee, 1995). The spatial distribution of the mean of the normalized innovation variance for the winter season in 2002–2003 is shown in Figure 2.12. Its value is significantly larger than this theoretical expectation in some grids in the western U.S., the North Great Plains and the eastern coastal regions, but is lower than one in the northern tundra area. The prescribed forcing errors may be underestimated in the regions where this statistic is larger than one, while in the regions where this statistic is lower than 1.0, the forcing errors may be overestimated. This implication is intuitively reasonable considering that in the middle latitude region where the ground temperature often fluctuates around the freezing point in the cold season, and in the mountainous

region where the precipitation is difficult to observe from both station and satellite, the atmospheric forcing errors are easily underestimated. Some methods can be applied to tackle the above problem, for example, using ground observations to derive reliable error estimation through the comparisons with the model forcings (e.g., Reichle et al., 2002), or using observed land variables (e.g., SWE) to calibrate the error statistics. These approaches treat the error covariance as a tunable parameter in the data assimilation system. However they are suitable for applications with more atmosphere or land surface measurements.

## **2.7 CONCLUDING REMARKS**

This research investigates the feasibility of applying an EnKF data assimilation approach with a highly complex land surface model (CLM) for optimally estimating continental-scale snow water equivalent with MODIS observed SCF. A newly developed observational operator based on snow density is applied. Through this operator and the sequential assimilation scheme, the useful information contained in the MODIS snow cover data are projected into the CLM propagated ensemble SWE fields. An evaluation of the results for North America indicates the validity of the proposed method, which depends on ground snow measurements and independent satellite observations. In addition, the multi-year regridded dataset is used to provide a reliable reference to evaluate the spatial differences between the EnKF and open loop simulations. Analyses of the filter performance further suggests that the EnKF is suitable for resolving uncertainties associated with the large-scale snow simulation system in distinct landscape and climatic zones. This work also characterizes some key issues in the EnKF snow

estimation framework, such as the system bias and model error misrepresentation. It provides the spatial distributions of related statistics useful for characterizing the quality of the data assimilation system. The method could be improved by better quantification of the errors in the modeling system including its mean value (bias) and variance.

Table 2.1 Calibrated parameter  $\alpha$  used in observation operator for different land types

	Flat and Low Vegetation	Mountainous region	Flat and high vegetation
Optimized $\alpha$	0.98	1.69	2.21
Correlation Coefficient R	0.92	0.82	0.96

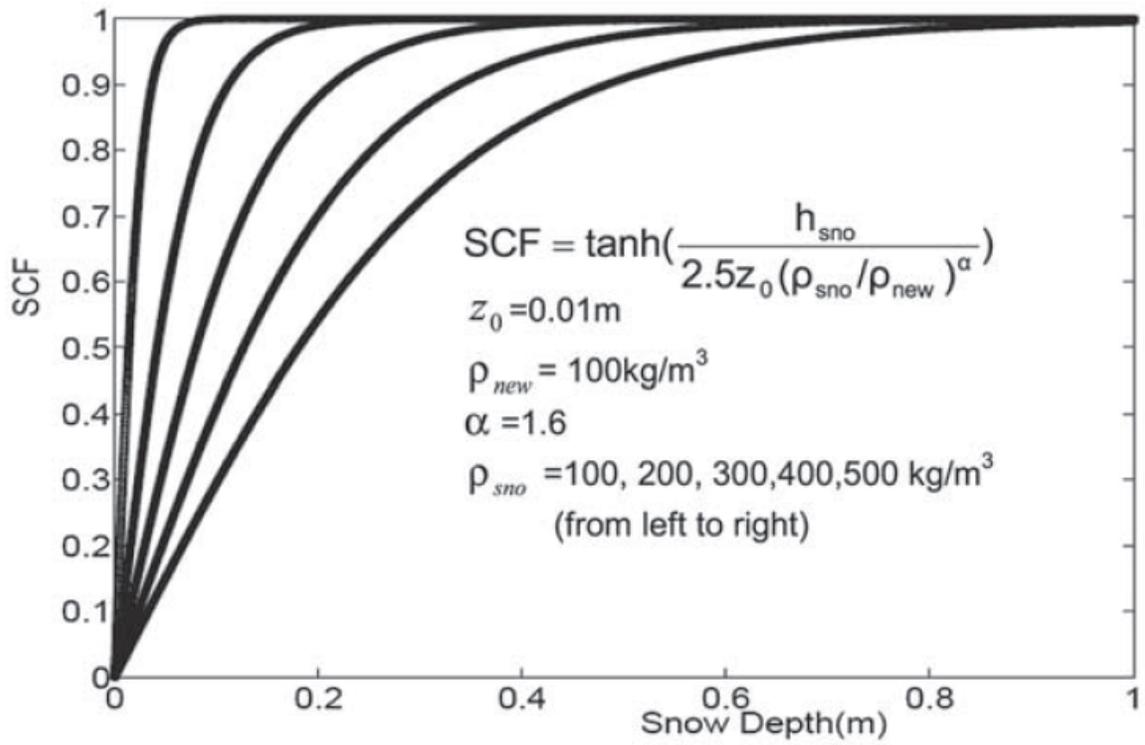


Figure 2.1. SCF parameterization using snow density. Each curve represents a different snow density in equation (6).

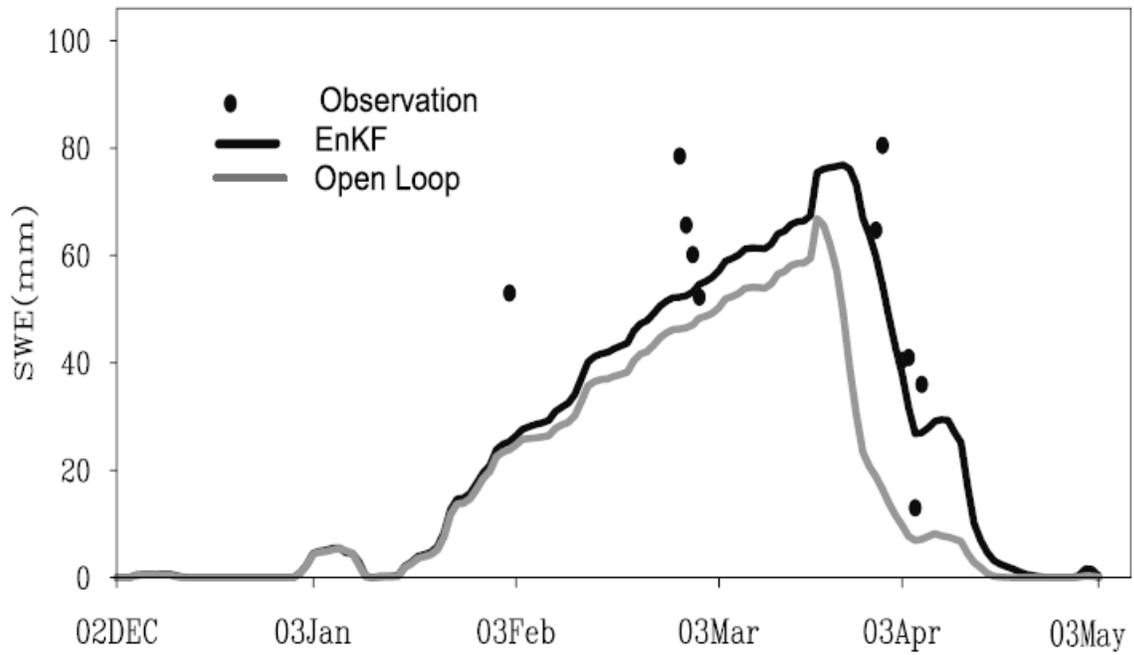


Figure 2.2. Comparison of regional averaged SWE ( $52^{\circ}$ – $54^{\circ}$  N,  $112^{\circ}$ – $114^{\circ}$ W, shown as the rectangular box in the upper panel in Figure 2.5, in 2002–2003) from simulation results and ground observations.

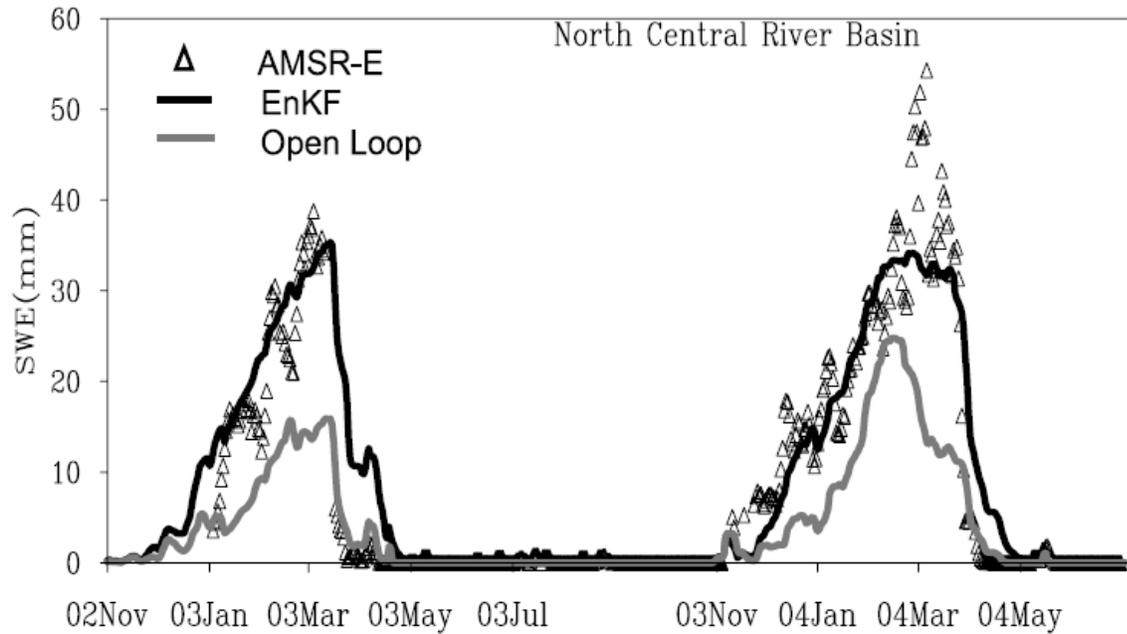


Figure 2.3. Comparisons among daily basin averaged SWE estimations in North Central River Basin. A five-day moving average is used on AMSR-E data to filter out the high frequency fluctuations in the original AMSR-E daily data.

This high frequency component is assumed to be caused by the incomplete coverage of the AMSR footprints in this region, which is frequently present during the simulation period. Same filter is used in AMSR data in Figure 5.

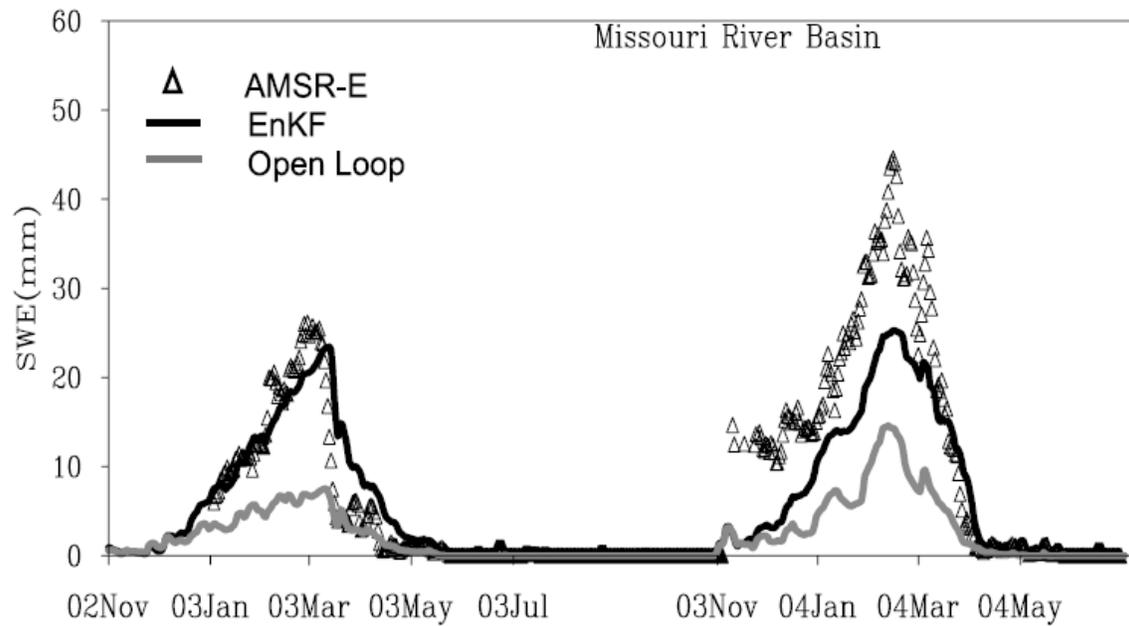
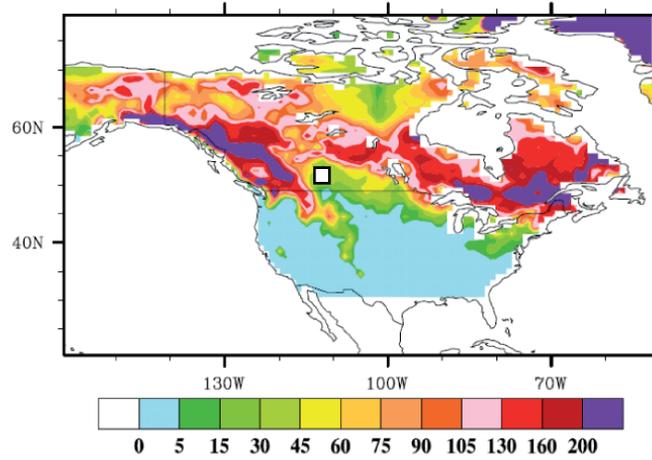
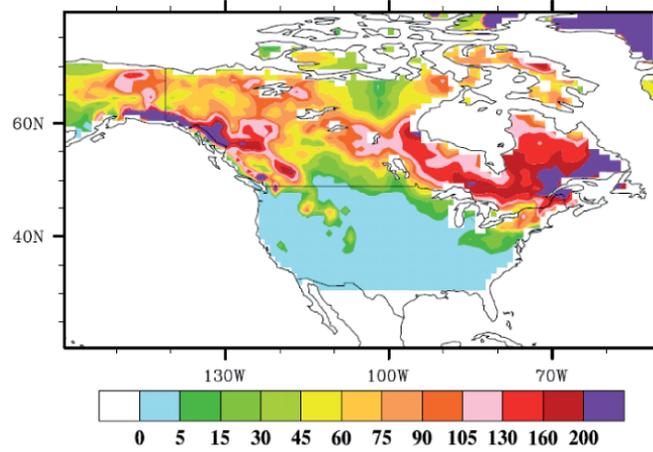


Figure 2.4. Comparisons among daily basin averaged SWE estimations in the Missouri River Basin.

The EnKF run (Feb, 2003)



The Open Loop run (Feb, 2003)



The Climatology (Feb)

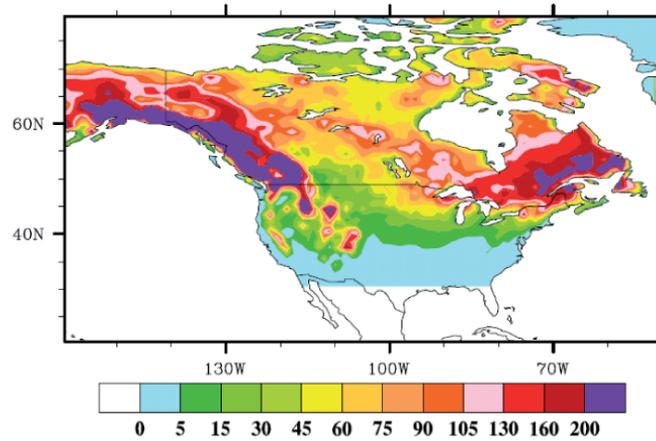
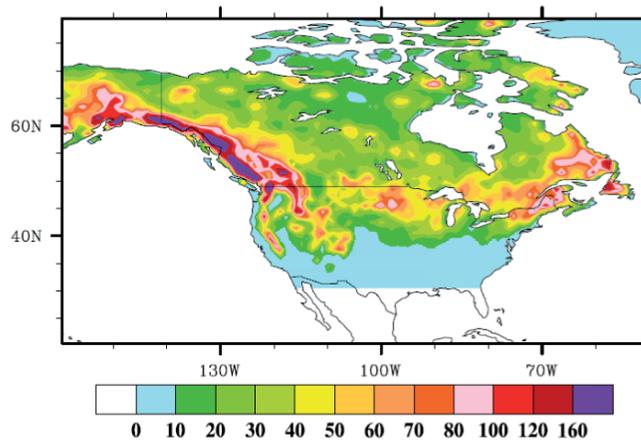
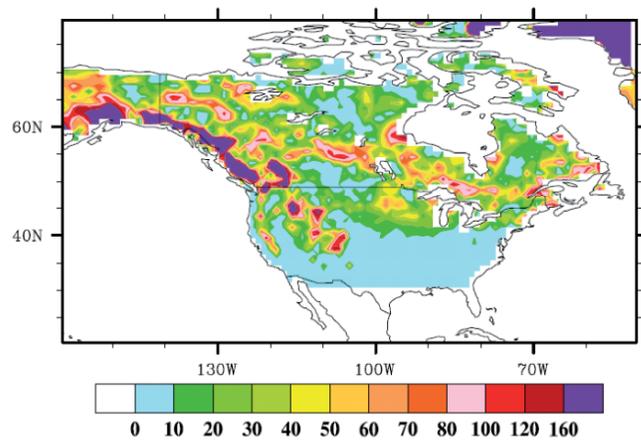


Figure 2.5. The spatial distribution of the monthly averaged SWE (mm) in Feb from the EnKF and open loop simulations, the climatology from reanalysis dataset, and the AMSR dataset.

Standard deviation (Feb)



EnKF (Feb, 2003) – Climatology (Feb)



Open Loop (Feb, 2003) – Climatology (Feb)

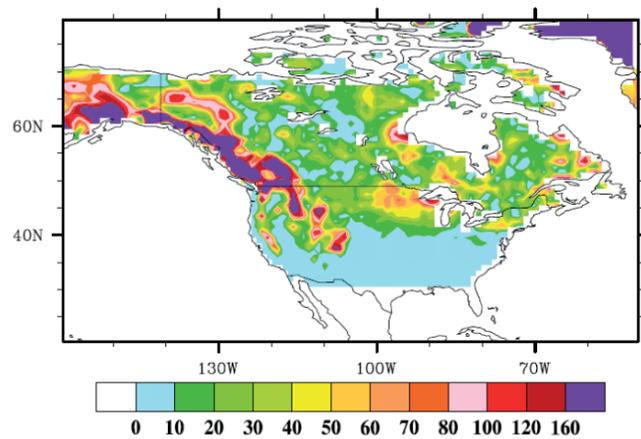


Figure 2.6. The spatial distribution of SWE standard deviation (mm) in Feb derived from the reanalysis dataset, the absolute value of monthly mean (Feb) difference (mm) between the EnKF and climatology, also the difference (mm) between the open loop and climatology.

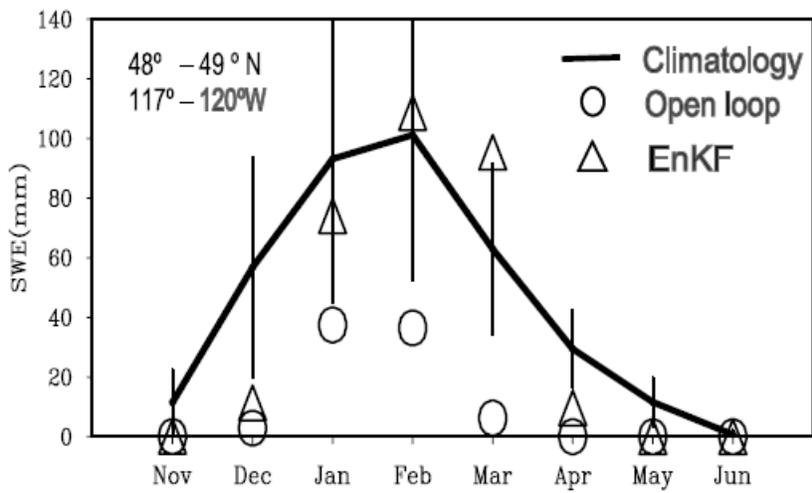
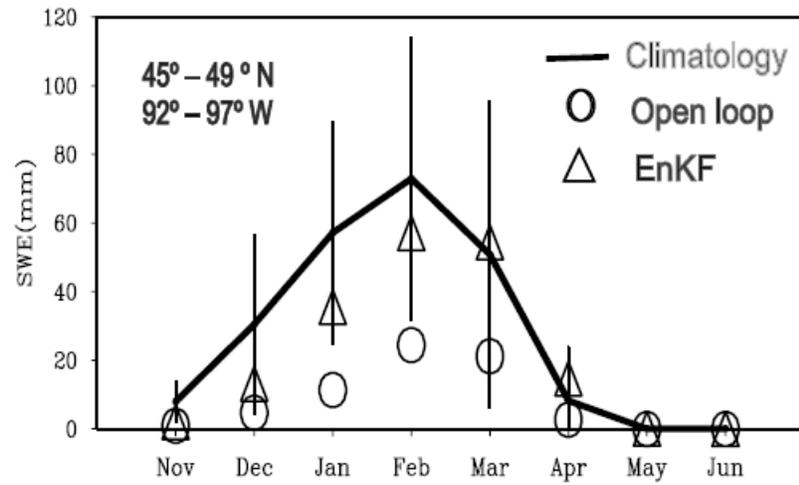
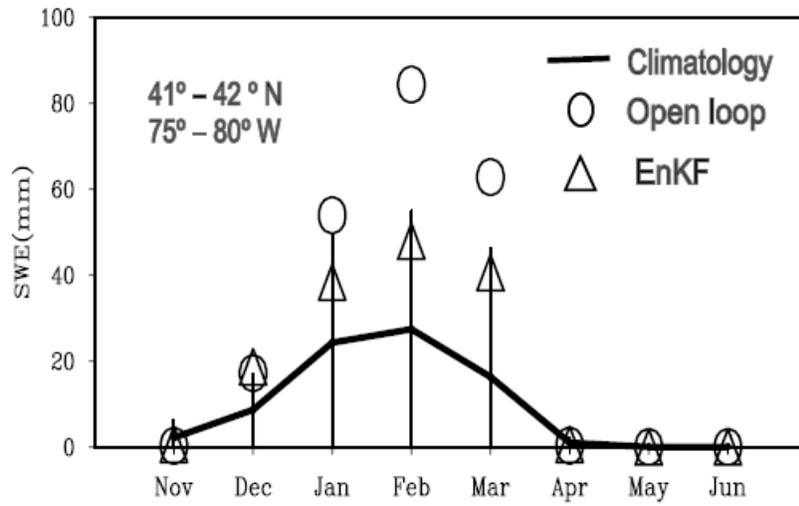


Figure 2.7. Comparison of the EnKF and open loop simulated monthly mean SWE with reanalysis derived climatological mean from Nov, 2002 to Jun, 2003 in three rectangular regions.

The error bar (vertical line) is given for each climatological mean value, which stands for the standard deviation (inter-annual variability) of each month.

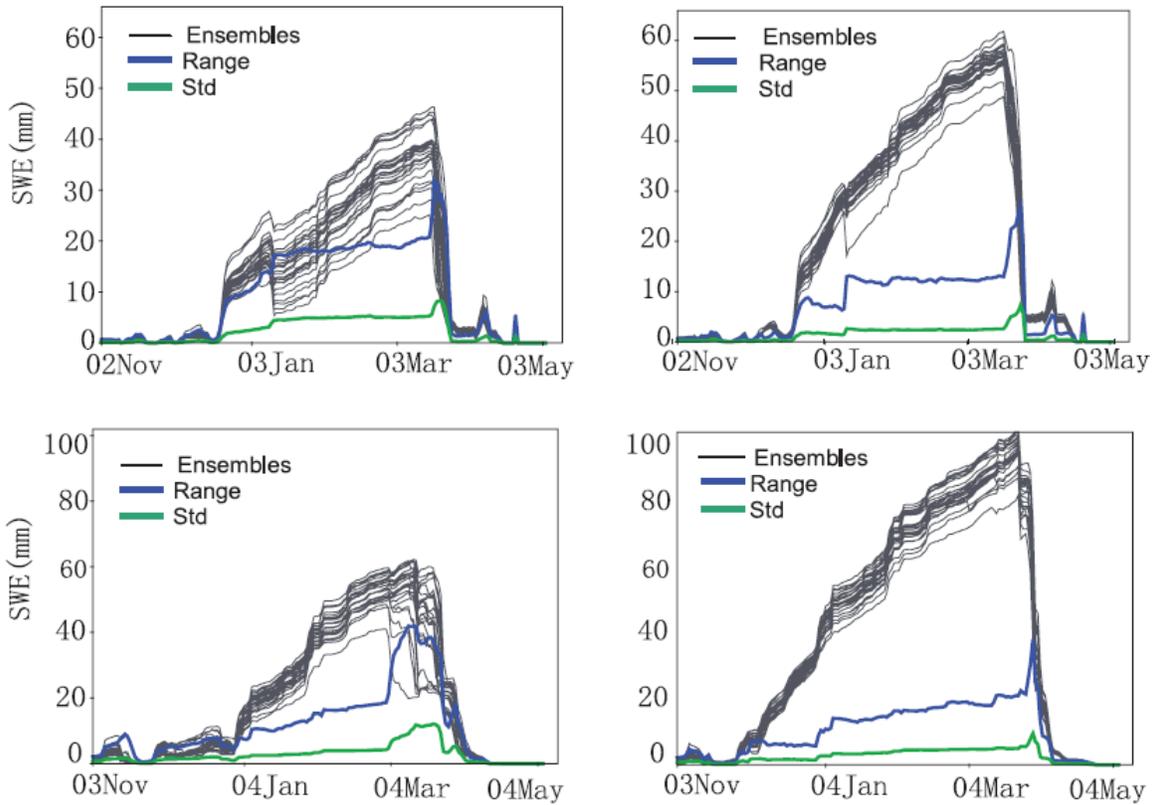


Figure 2.8. Ensemble simulations of SWE and their error statistics at a grid in the prairie region.

Left : Open loop run; right: EnKF run. Upper: 2002-2003; Lower: 2003-2004. Ensemble simulations are represented by gray curves, the range (difference between the maximal ensemble value and the minimal ensemble value) of ensemble is the blue curve, and the standard deviation of ensemble is the green curve.

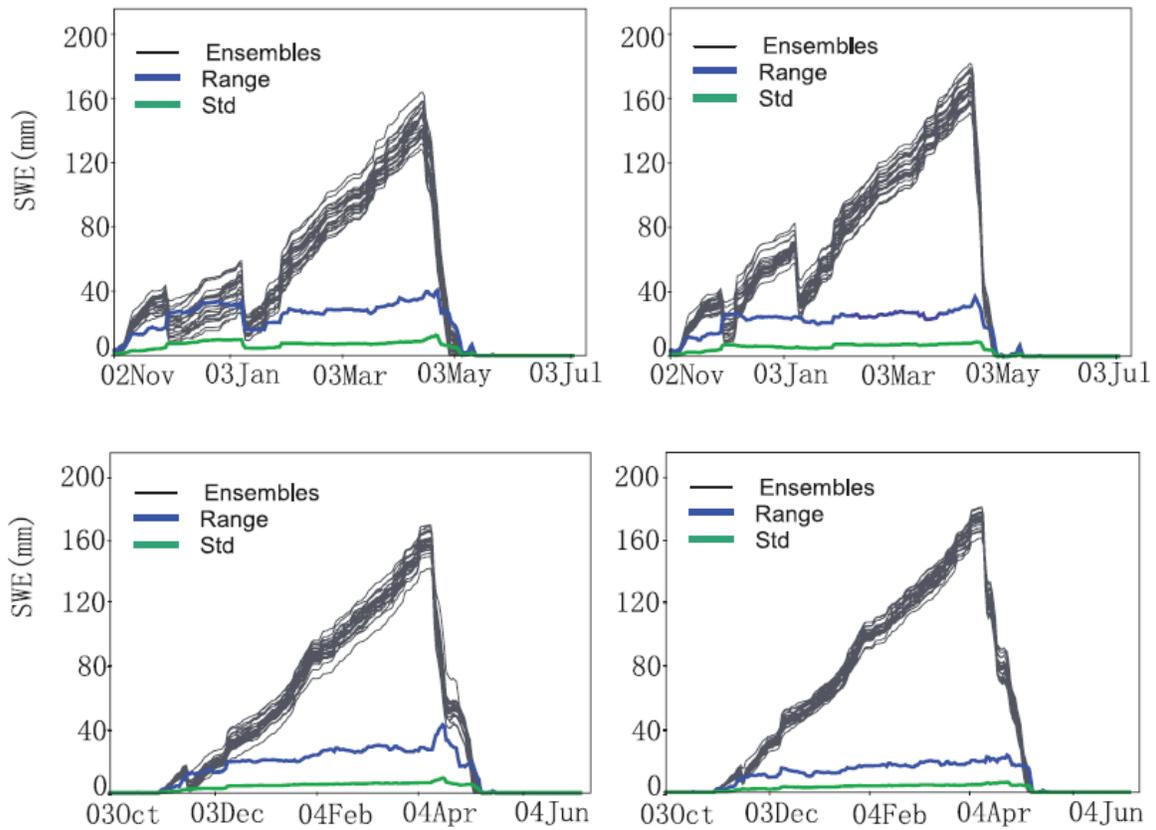


Figure 2.9. Ensemble simulations of SWE and their error statistics at a grid in the boreal forest region.

Left : Open loop run; right: EnKF run. Upper: 2002-2003; Lower: 2003-2004. Ensemble simulations are represented by gray curves, the range (difference between the maximal ensemble value and the minimal ensemble value) of ensemble is the blue curve, and the standard deviation of ensemble is the green curve.

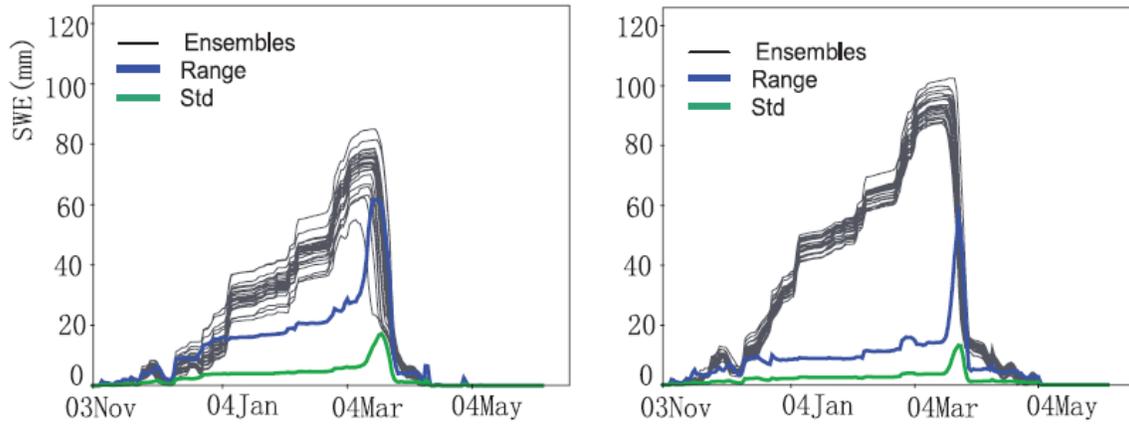


Figure 2.10. Ensemble simulations of SWE and their error statistics at the grid in the mountainous region.

Left : Open loop run; right: EnKF run. Ensemble simulations are represented by gray curves, the range (difference between the maximal ensemble value and the minimal ensemble value) of ensemble is the blue curve, and the standard deviation of ensemble is the green curve.

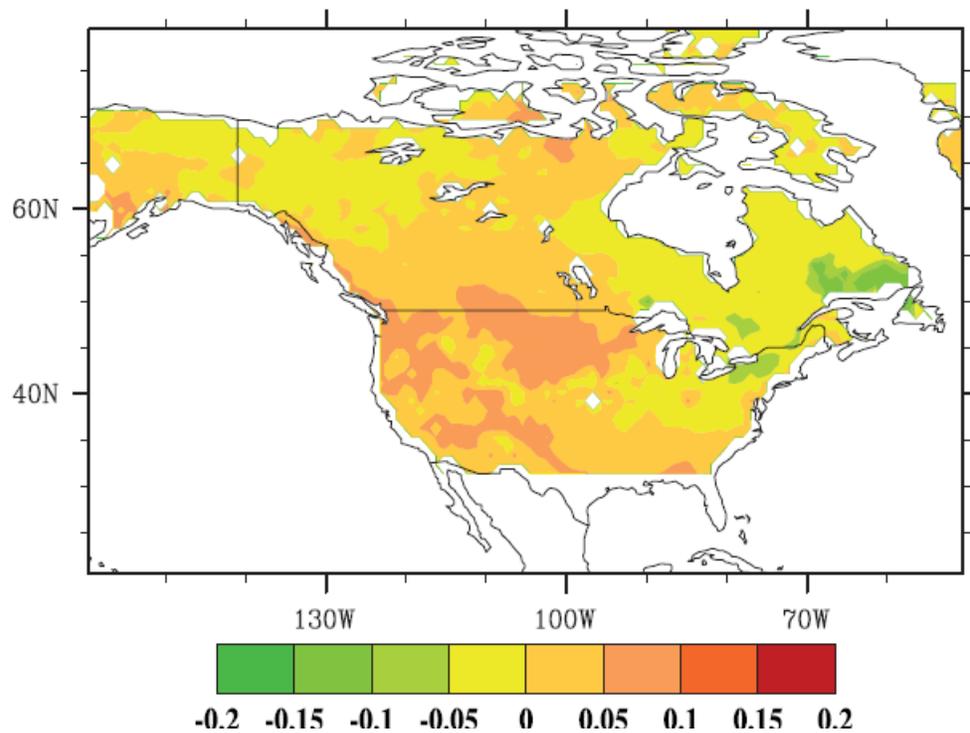


Figure 2.11. Spatial distribution of the average of the innovation (difference between observation and simulation) mean for the winter season in the 2002-2003 simulation (December 2002 to April 2003).

This value is significantly larger than its theoretical expectation, zero, in some grids in the western U.S. and the North Great Plains, indicating the model system has low bias there. In contrast, the value is lower than zero in the north-east of North America, representing the model system has high bias there.

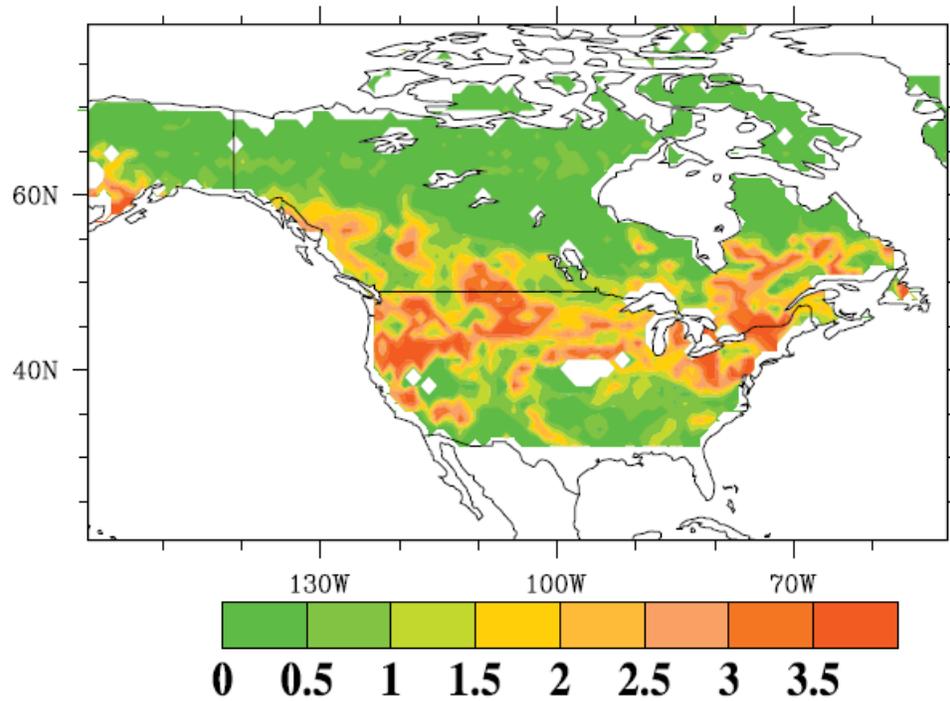


Figure 2.12. Spatial distribution of the mean of normalized innovation variance (equation (2.7) for the winter season in 2002–2003 (December 2002 to April 2003).

This value is significantly larger than its theoretical expectation, one, in some grids in the western U.S., the North Great Plains and the eastern coastal regions. In contrast, the value is lower than one in the northern tundra area.

## **Chapter 3: Parameter estimation in ensemble based snow data assimilation: a synthetic study**

### **3.1 ABSTRACT**

Estimating erroneous parameters in ensemble-based snow data assimilation systems has received little attention in the literature. The objective of this study is to assess the effectiveness, performance, and sensitivity of the ensemble based method to other sources of error such as model structural error. Synthetic one-dimensional snow data assimilation with the ensemble Kalman filter was run to achieve this objective. The traditional Kalman analysis equation is augmented to include a parameter vector. The first part of the paper investigates the effectiveness of this parameter estimation approach in a perfect-model-structure scenario, and the second part focuses on its dependence on model structure by introducing a simple parameterization error.

Results from first part research show that this parameter estimation approach reduces the systematic error of SWE estimates, and retrieves the correct parameter value. In addition, the simulation of related ground energy variables was improved due to correction of parameters and their influence through model physics. Results from the second part indicate that, at least in this experiment, there is an evident dependence of parameter search convergence on model structural error. In the imperfect-model-structure run, the parameter search diverges, although it can simulate the state variable well. Empowered by the state-space infrastructure of the EnKF, this result suggests that, good data assimilation performance in estimating state variables is not a sufficient indicator of reliable parameter retrieval in the presence of model structural error (here I have good performance along with parameter divergence). The generality of this conclusion needs to

be tested by data assimilation experiments with more complex structural error configurations.

### **3.2 INTRODUCTION**

As an important freshwater resource, snow also affects the land surface energy balance via its unique thermodynamic properties (e.g., high albedo, low thermal conductivity) that vary spatially and temporally. In this respect accurately characterizing snow conditions is critical for hydrological forecasts, diagnosing hydroclimatologic trends (Brown et al., 2003) and subsystem interactions (e.g, land snow cover-atmosphere interaction), and monitoring floods and droughts, among other applications. Although this need of snow data is pressing, the related tasks of snow monitoring have not been satisfactorily accomplished over a wide range of scales (e.g., from the watershed-scale snowpack monitoring to global-scale snow mapping). One difficulty involved in this data inadequacy is a cold environment that prohibits extensive ground survey efforts.

Remotely sensed snow information provides a new opportunities for snow estimation. The EnKF methods have been used with such datasets to estimate snow water equivalent (SWE) and other cold region variables (e.g., Clark et al., 2006; Durand and Margulis, 2007; Su et al., 2008). The various work focused on different spatial scales, while they used the same error-covariance based algorithm to sequentially adjust model simulations. Theoretically, the EnKF method requires that the function relating observations and model simulations is free of systematic error, to accurately propagate the ensemble and to avoid bias in the update equation. However, land surface model (LSM) and observational functions applied in the above studies may have system errors

that originate from a broad range of sources including, for example, incomplete representation of snow properties and associated dynamical processes, uncertainties in model parameters, and scaling or physical discrepancy (Blöschl, 1999) between observation and model estimates of snow properties, etc. Each of the related sources of error is linked to different stages of model development or remote sensing data processing. The mixture of these errors in the highly non-linear LSM simulation makes their individual effects difficult to isolate and interpret (Clark et al., 2008). Affected by these uncertainties, the snow data assimilation system is vulnerable to systematic error and unrealistic updates, especially in estimating the ensemble mean. In particular, parametric errors are common in LSMs and observational functions, yielding negative effects on the EnKF algorithm. Because of the nonlinear nature of the hydrological system, these effects may be magnified through interactions with other error sources (Liu and Gupta, 2007).

To tackle such issues, recent studies (Andreadis et al., 2007) have examined the impacts of parameter uncertainty in multi-scale snow simulations that include its electromagnetic signatures. However, few studies have focused on methods to correct parameter uncertainty in ensemble snow data assimilation systems. In most of the EnKF experiments, critical parameters characterizing snowpack dynamics were simply treated as perfectly known or by inflating with prescribed noise (e.g., Andreadis et al., 2006; Su et al., 2008). Related studies in meteorology (Anderson, 2001, Aksoy et al., 2006) have shed light on how to deal with this drawback. Their work combined parameters and states in an “augmented vector” and reduced the parameter-state optimization to a state-variable filtering problem. Following the same general method, this study concentrates on

reducing parameter uncertainties in a highly-nonlinear and dissipative snow model forced with prescribed meteorological data.

Besides its overall performance, another inherently related question is that how state-space based parameter estimation is dependent on model physical structures (or, the physical structural error in the system). This issue has often been neglected in previous research. In other words, it is currently not clear that whether the parameter estimation algorithm can achieve performance comparable to those using perfect-structure model in simulating snowpack state variables and retrieve reliable parameter values, given that the model has structural error. The insights gained from addressing this question may benefit snow data assimilation in a broad sense. Currently there are a wide range of physical structures (parameterizations) in different snow models (e.g., Etchevers, et al., 2002), reflecting distinct (or incompatible) perspectives that represent the same real world process. These different perspectives usually result from, for example, limited predicative capability for a given model structure and availability and quality of measurements. Although it is difficult to rank the physical appropriateness of these model structures, and each model structure (describing physically equivalent processes) may only capture part of the truth, understanding the impact of their differences on the parameter estimation performance in the EnKF environment is crucial to model selection in snow data assimilation. Further, according to Clark et al (2008), for streamflow simulation in a given climate regime, selection of model structure could be just as important as selection of model parameters. This brought upon the similar concern for my research, which is, can parameter estimation, if conducted elaborately, fully compensate for the structural deficiency in the EnKF snow estimation system. Insights obtained from this study might

contribute to accurately evaluating the cross-region transferability of those estimated parameters for individual model structure given that true (or most appropriate) structures and parameters are often unknown (or partially known) for the tested region.

This paper consists of two-fold research that are closely related to each other and can be accomplished in a common data assimilation framework. First, performance of parameter estimation in a synthetic EnKF snow data assimilation system is comprehensively evaluated. In this part the model physical structure is assumed perfectly known. Built on the similar data assimilation infrastructure, a relatively simple model structure error is introduced in the second part and performance of parameter estimation is compared to that of the perfect-model-structure run. The next section introduces the LSM, the EnKF method, and the parameter estimation scheme. Two different snow data assimilation experiments are described in sections 3 and 4. A further discussion of results is given in section 5 with concluding remarks in section 6.

### **3.3 METHODOLOGY**

The CLM (2.0 version, Bonan et al., 2002) is used to propagate land state variables. CLM numerically simulates energy, momentum and water exchanges between the land surface and the overlying atmosphere. It employs 10 soil layers to resolve soil moisture and temperature dynamics and uses plant functional types (PFTs) to represent sub-grid vegetation heterogeneity. Its snow model simulates a snowpack with multi-layers (1-5 layers) depending on its thickness, and accounts for processes such as liquid water retention, diurnal cycling of thawing–freezing, snowpack densification, snow melting, and surface frost and sublimation. Besides these features, the CLM used in this

research includes a new SCF parameterization which dynamically adjust the relationship between grid averaged SWE and SCF (Niu and Yang, 2007). Estimating a related parameter in this parameterization is one of the central topics in this experiment. More discussion about this parameter and the associated equation is given in section 3. The general performance of CLM2.0 in cold region simulations is given by Bonan et al. (2002), and Niu and Yang (2006, 2007).

The classic EnKF method (Evensen, 1994) is implemented with an observation perturbing scheme (Burgers et al., 1998). Additional discussion of the EnKF scheme in CLM is given by Su et al. (2008). Modifications to include parameter estimation are incorporated in the same mathematical framework. Equation (3.1) gives a brief statement of the parameters-augmented EnKF analysis.

$$([x_t, \delta]^T)^a = ([x_t, \delta]^T)^b + K_t(y_t - H([x_t, \delta]^T)^b) \quad (3.1)$$

where  $x_t$  and  $\delta$  are state and parameter vectors, all of which are in an ensemble form;  $K_t$ ,  $y_t$  and  $H$  are the Kalman gain, observations, and observation operator, respectively. Superscripts  $a$  and  $b$  denote analysis and background, respectively. To deal with the problems of variance reduction in parameter ensemble space and filter divergence, this research adopt the “conditional covariance inflation” method proposed by Aksoy et al. (2006), which prescribes a threshold for the parameter ensemble variance, without augmenting ensemble spread at each system propagation step. Equation (3.2) gives the formulation of this inflation method (which is the evolution equation of parameter ensemble  $\delta$ ).

$$\delta_{t+1}^b = \delta_t^a \quad \text{if } \text{Var}(\delta_t^a) \geq Q_0$$

$$\delta_{t+1}^b = \delta_t^a + \varepsilon \quad \text{if } \text{Var}(\delta_t^a) \leq Q_0, \quad \varepsilon \in N(0, Q_0 - \text{Var}(\delta_t^a)) \quad (3.2)$$

In which  $N(0, Q_0 - \text{Var}(\delta_t^a))$  represents the normal distribution with zero mean and variance of  $Q_0 - \text{Var}(\delta_t^a)$ .  $Q_0$  is the prescribed variance threshold. This inflation approach has been shown successful in a highly non-linear and flow-dependent meteorological data assimilation system (Aksoy et al. 2006), where the proper constraints on parameter ensemble variance are shown to be important for the accurate EnKF update. Because there is no prior knowledge about the evolution of parameters,  $Q_0$  largely controls the parameter ensemble trajectory. The selection of  $Q_0$  and its implications are discussed in following sections.

### **3.4 THE PERFORMANCE OF PARAMETER ESTIMATION WITH PERFECT-MODEL-STRUCTURE**

The first group of simulations is synthetic experiment in which a single grid simulation for six months (November-April) is created with CLM driven by ensemble meteorological forcing. In the experiment, the true state of related variables is known. Table 1 provides a list of these simulations. The model time step is 30 minutes, which is small enough to characterize those major snowpack dynamic processes. For simplicity, only one vegetation tile type (grass) is used in the grid. Therefore the parameters involved in the forest-snowpack thermodynamic interactions (e.g., as shown in Niu and Yang, 2004) are neglected. In addition, the subgrid snow cover heterogeneity is included. Since the patch of snow cover can drive similar process across a diverse range of scales in influencing snowpack radiative energy balance, the related experiments in this one-

dimensional synthetic study can have some degree of spatial representativeness. Ensemble forcing is produced by perturbing nominal precipitation and air temperature with 50% and 3° C (rms) Gaussian error, respectively. The ensemble runs contain 59 members and an additional run is conducted to represent synthetic truth. This provides a benchmark for quantitatively understanding parameter estimation effects. Synthetic SWE observations are produced every two days by adding Gaussian perturbations (20 mm rms) to the true state.

Here consider estimation of two parameters that are typically difficult to determine from measurements. These are: (1) exponent  $\alpha$  in the snow cover fraction parameterization described by equation (3) (Niu and Yang, 2007); (2) liquid water holding capacity  $\theta$  (the maximum volume, in percentage, of liquid water in snowpack, equation 5). The parameter  $\alpha$  governs the relationship between the snow depth (or SWE) and the snow cover fraction (SCF), strongly influencing grid averaged albedo and snowpack energy processes (equation (4)). Niu and Yang (2007) have demonstrated the significant sensitivity of CLM performance in simulating cold region variables to this parameterization (3) and the parameter  $\alpha$ , implying their potential importance to the snow data assimilation.

$$SCF = \tanh\left(\frac{h_{sno}}{2.5z_0(\rho_{sno} / \rho_{new})^\alpha}\right) \quad (3.3)$$

$$A_{total} = A_{snow} * SCF - A_{grass} * (1 - SCF) \quad (3.4)$$

$$\theta_{drainage} = \theta_{liquid-snowpack} - \theta, \quad \text{if } \theta_{liquid-snowpack} > \theta \quad (3.5)$$

Here  $h_{sno}$  and  $z_0$  are the snow depth and the ground surface roughness length, respectively;  $\rho_{new}$  is a prescribed fresh snow density;  $\rho_{sno}$  is the model calculated snow density (Niu and Yang, 2007).  $A_{total}$  is the grid averaged albedo to calculate the ground energy balance,  $A_{snow}$  and  $A_{grass}$  are the snow and grass albedo, respectively (with  $A_{snow}$  much larger than  $A_{grass}$ ). With other conditions unchanged, increasing  $\alpha$  generally leads to a decrease of SWE and vice versa. The parameter  $\theta$  sets the threshold for the variability of liquid water content in the snowpack, thus controlling its thermodynamic properties, stratigraphic characteristics (e.g., snow density), and melting process. With other conditions unchanged, increasing  $\theta$  generally leads to an increase of SWE, and vice versa. In previous research (e.g., Niu and Yang, 2007), this parameter is often given an empirical number without quantitative method to derive application specific value. The main reason could be that there are few physical laws, if any, to estimate  $\theta$ . It can exert significant effects on the dynamical processes. In section 3.3, it would be shown how an erroneous  $\theta$  can influence the simulation of snowpack.

A further reason to select these parameters is that I assume they are representative for the parametric uncertainty in this nonlinear model structure, and the demonstrated system behaviors could be typical in the scope defined by my central objectives in section 3.1. Considering that my purpose here is to preliminarily assess the overall performance of the parameter estimation approach and not to enumerate parameters in different components of the model and comprehensively characterize their joint estimation, increasing the number of analyzed parameters may be less important than the need of keeping the system tractable by limiting the size of parameter vector. Accordingly, the

interaction among multiple parameters and their differing ensemble trajectories are not focused on in this research (while the relationship between above two parameters and their different impacts to data assimilation are interpreted), although I recognize the potential importance of analyzing larger parameter vector in obtaining more insights of the system.

There are six simulations designed in this section (see Table 3.1 for description of these simulations). In SYN\_TRUE the true values of  $\alpha$  and  $\theta$  are 1.6 and 0.01, respectively. For the imperfect model simulations (SYN\_CR, DA\_PAR\_CR, DA\_PAR\_  $\alpha$  , DA\_PAR\_  $\theta$  )  $\alpha$  and  $\theta$  are set as 0.6 and 0.08, respectively, representing parameter errors. According to Aksoy et al. (2006), the initial standard deviation for parameter ensemble is set to the difference between the initial mean parameter value and the true parameter value (1.0 and 0.07 for  $\alpha$  and  $\theta$  , respectively), while the prescribed standard deviation (square root of  $Q_0$  in equation (2)) is set to 1/4 of the initial standard deviation. Other  $Q_0$  values have been tested and the results of both variables and parameters are very similar (refer to Figure in section 3.4 for more details about this sensitivity). So this paper presents the results with the above  $Q_0$  which is representative.

Figure 3.1 compares ensemble mean results of SWE from SYN\_CR, DA\_PAR\_CR and SYN\_TRUE. Table 3.2 gives Nash-Sutcliffe efficiency for ensemble mean of different simulation shown in Figure 1, representing their integrated performance. The SYN\_CR begins to deviate from the true values around the early stage of snow accumulation. This is mainly due to overestimation of SCF (due to the error in  $\alpha$ ).

During the melting stage, deviation from the true state increases nonlinearly, reaching hundreds of mm. This occurs because errors in SCF parameterization produce a positive feedback in the melting process. A greater SCF results in a higher albedo, causing a decrease in absorbed solar radiation and further increase in SCF. The  $\theta$  error further reduces melting amount, because more liquid water is allowed to stay in the snowpack than the true value. As a consequence, large errors persist in estimated SWE even when observations are assimilated (DA\_PAR\_CR).

Simultaneously estimating  $\alpha$  and SWE with equation (3.1) improves the results of SWE simulation (Figure 3.1, DA\_PAR\_ $\alpha$ ). The innovation (difference between observations and model simulation) in the EnKF updates the parameter ensemble at every time step when observation is available (every two days). The success of this EnKF in simulating SWE largely depends on an accurate statement of correlations between parameters and observations. This is partly achieved in the representation of energy feedback processes. Similarly, simultaneously estimating  $\theta$  and the usual SWE state variable improves the results (Figure 3.1, DA\_PAR\_ $\theta$ ). DA\_PAR\_ $\alpha$  provides better results than DA\_PAR\_ $\theta$ , indicating the system's greater sensitivity to errors in  $\alpha$ . DA\_PAR\_ $\theta$  probably does not fully compensate for bias in related energy processes. When both  $\alpha$  and  $\theta$  are adjusted the performance is similar to DA\_PAR\_ $\alpha$ , and the experiment results are not shown here.

Meanwhile I am also interested in whether my method obtains the right results (as shown above) by addressing the right problem. In another word, there should appear "concurrent convergence" (that means both the state variables and parameters converge to their true values respectively, in the EnKF simulation). Figures 3.2 and 3.3

demonstrate how the mean of parameter ensembles evolves with the sequential EnKF adjustment. True values of  $\alpha$  and  $\theta$  are approached in the corresponding simulations. Further analyses show that parameter identification depends on a “biased innovation” (which can be interpreted as the difference between the imperfect model run and true state in Figure 3.1), and the ensemble estimated correlation between the parameters and observed variables. The “biased innovation” forces the parameter ensembles to vary in a non-stationary mode (changing mean value), while the correlation contributes to controlling the direction and magnitude of that variability. It is noted that estimating both  $\alpha$  and  $\theta$  leads to good estimates of  $\alpha$  and overestimation of  $\theta$ , for which the ensemble mean remains near 0.06. This suggests competing mechanisms in multi-parameter estimation (especially in a single measurement variable situation), which may favor a few dominant parameters with others not being properly retrieved.

A follow-up question is whether this EnKF update (note that only SWE and parameters are updated in equation (3.1)) can transfer these benefits to simulation of other snowpack related variables, especially, those related to ground energy balance. Figure 3.4 gives the ensemble mean of daily averaged ground radiative temperature for all runs in Table 1, from April 2004 to June 2004 (the results are similar in the accumulation season). In this melting period, as expected, SYN\_TRUE and DA\_TRUE agree with each other, indicating the ability of data assimilation to accurately estimating longwave emission of snowpack in the absence of parameter error. This is achieved indirectly by adjusting SWE, which influence the radiative emission calculation through model physics (better calculation of SCF and absorbed solar radiation in energy balance equation). For SYN\_CR and DA\_PAR\_SYN, the estimation qualities are low. These

deficiencies are attributed to the parameter errors that degrade the ground energy balance calculation. The largest gap between these two simulations and the truth appears during the period when ground is snow-free as in SYN\_TRUE, implying that whether snow cover is present is a dominant factor to the radiative temperature estimation. For DA\_PAR\_ $\alpha$  and DA\_PAR\_ $\theta$ , the simulations are improved by different degrees, with DA\_PAR\_ $\alpha$  much closer to the true value.

Figures 3.5 and 3.6 present the simulations of ensemble mean ground sensible heat flux and albedo in daily averaged values. They show similar patterns as compared with Figure 3.4. In the melting period, sensible heat flux and grid averaged albedo are closely related to the size of snow area which is linked to SWE in the system. Therefore they can be better estimated if the errors in simulating ground snow cover (for albedo) and radiative energy balance (for sensible heat flux) are resolved. Also, the greater differences in May 2004 (compared to April 2004) between group 1: SYN\_TRUE, DA\_TRUE, DA\_PAR\_ $\alpha$  and group 2: SYN\_CR, DA\_PAR\_SYN and DA\_PAR\_ $\theta$  result from their different timing of snow-free conditions.

Figure 3.7 presents the ensemble mean of diurnal temperature range (DTR) of snowpack. In this experiment the DTR is defined as the temperature (layer averaged) difference between 3pm and 3am (local time). This variable can be used to diagnose the thermodynamic effects of liquid water refreezing within snowpack. In this regard the parameter  $\theta$  is crucial because it controls the available amount of liquid water to refreeze at night and influence the DTR. The larger  $\theta$  leads to more heat loss in a phase change form and decreases the DTR with increased night time snowpack temperature. The results agree with this by showing lower DTR along the entire snow season for

simulations with erroneous  $\theta$  (SYN\_CR, DA\_PAR\_SYN). DA\_PAR\_  $\alpha$  also underestimates DTR, demonstrating the independence between  $\alpha$  adjustment and the night time refreezing process. Estimating  $\theta$  enables DA\_PAR\_  $\theta$  to better capture the amplitude of DTR, which much more resembles the true value than DA\_PAR\_  $\alpha$ .

### 3.5 EFFECTS OF STRUCTURAL ERROR ON PARAMETER ESTIMATION

This section only investigates a simple case of structural error in snowpack simulation, to facilitate a straightforward diagnose of its effects. Here a primary goal is to keep the diagnostic framework simple and tractable, recognizing that complicated structural error behavior may result from incorporating multiple processes and their nonlinear interaction. Situations consisting of more complex structure errors would be valuable topics for further research. Another SCF parameterization (replacing equation 3.3) is introduced and represents the structural error. It is shown in equation (3.6). In addition to the above mentioned simplicity, at least two reasons are considered to construct the error in this way. First, both two parameterizations share the common role in the model architecture (representing grid-scale snow cover-snow depth relationship), so they are comparable. Second, they differ greatly in their formulation, representing significant structural difference.

Two simulations are designed. The DA\_STRUCT\_TRUE is the perfect-model-structure run using equation (3.3), and starts with an erroneous  $\theta = 0.6$ . The DA\_STRUCT\_NEW uses equation (3.6) with  $Z \ln d$  as the adjustable parameter.  $Z \ln d$  characterizes the roughness length of ground and is assumed uncertain in DA\_STRUCT\_NEW. To construct a comparable framework, all other structural and

parametric features in DA\_STRUCTURE\_TRUE and DA\_STRUCTURE\_NEW are the same as in SYN\_TRUE. Both of them assimilate a common dataset of SWE generated with the same approach in section 3.3.

$$SCF = \frac{h_{sno}}{10Z_d + h_{sno}} \quad (3.6)$$

As mentioned in section 3.2, the selection of  $Q_0$  in equation (2) influences the trajectory of parameter ensemble. To ensure a fair comparison, this work run the above simulations with different  $Q_0$ , to obtain enough spread to lead to the dependable results. In addition, the dependence of system performance and parameter retrieval on the selection of initial value of  $Z \ln d$  has been considered. My preliminary test found that varying this input did not affect the simulation too much, so use  $Z_{d0} = 0.01$  (a default value for CLM2.0,  $Z_{d0}$  denotes the initial value of  $Z_d$ ).

Figures 3.8 and 3.9 display the error (ensemble mean SWE minus corresponding true value) of DA\_STRUCTURE\_TRUE and DA\_STRUCTURE\_NEW respectively, for each of their own  $Q_0$  used to constrain the parameter ensemble variance. Note that each curve is given in the same color as the label showing magnitude of square root of  $Q_0$  (std). Here std is represented by a number multiplying the initial value. Tables 3.3, 3.4 give the temporal mean of these errors (in absolute value) for DA\_STRUCTURE\_TRUE and DA\_STRUCTURE\_NEW, respectively. Agreeing with results in section 3.3, DA\_STRUCTURE\_TRUE performs well in estimating SWE for most of the  $Q_0$  selected, except that the std equals half of  $\alpha_0$  (its SWE error is still much lower than in the data assimilation run without parameter estimation, not shown here). On the other hand,

DA\_STRUCT\_NEW performs almost equally well in estimating SWE (only with significantly larger error for  $\text{std}=1/4 Z_{d0}$ , while its SWE error is still much lower than the data assimilation run without parameter estimation, not shown here). Moreover, the same pattern exists in both figures; the error remains low at accumulation period and peaks at melting period. The evolution of parameter ensemble stops when the ground is snow-free for every ensemble member.

Figures 3.10 and 3.11 show how the parameters (ensemble mean) are updated in each simulation. A difference emerges in this comparison:  $\bar{\alpha}$  converges at the end of simulation to around 1.7 for different  $Q_0$ , while  $\bar{Z}_d$  ( $\bar{Z}_d$  represents the ensemble mean of  $Z_d$ ) diverges to significantly different values for different  $Q_0$ . Further inclusion of a broader range of  $Q_0$  in DA\_STRUCT\_NEW (including  $\text{std}=1/8, \dots$  to  $3Z_{d0}$ , which can give a reasonable performance in SWE estimation) don't result in an evident convergence zone. This has been shown in Tables 3.5, 3.6, where a broad spectrum of  $Q_0$  have been tested and the retrieved parameter have been given for DA\_STRUCT\_TRUE and DA\_STRUCT\_NEW. These results imply that DA\_STRUCT\_NEW is likely to reduce the transferability of estimated parameter because no consensus can be made about  $\bar{Z}_d$ .

To test the reliability of the above results, also concerning that the most appropriate model structure would be usually unknown for regions without adequate measurements, a “symmetric experiment” is given, where equation (3.6) is the synthetic true parameterization (structure) in the ensemble data assimilation framework, and equation

(3.3) represents the structural error. In this experiment, the observation is derived from the synthetic true simulation with (3.6) (true  $Z_d=0.01$ ), and assimilated into two different data assimilation run with equation (3.6) (DA\_STRUCTURE\_TRUE\_2) and (3.3) (DA\_STRUCTURE\_NEW\_2), respectively. In general, results in this experiment are very similar to those shown above. That means the state variable can be well estimated in both DA\_STRUCTURE\_TRUE\_2 and DA\_STRUCTURE\_NEW\_2, while the parameters converge in DA\_STRUCTURE\_TRUE\_2 ( $Z_d$ ), and don't show an evident convergence in DA\_STRUCTURE\_NEW\_2 ( $\alpha$ ). The details of these results are omitted here.

## 3.6 DISCUSSION

### 3.6.1 Parameter estimation convergence/divergence

In a perfect-model-structure run, parameter estimation in the ensemble snow data assimilation has shown promise in accurately estimating a suite of land surface variables. In this scenario, both variables and parameters converge to the true value simultaneously, which is in contrast to the result in the imperfect-model-structure run.

A hypothetical explanation for the above result is that, driven by model structural error, each  $Q_0$ , a degree of freedom constraining the parameter variance, seems to become an independent condition and leads the stochastic update to a unique value in the parameter space, while to the structure-error free case (DA\_STRUCTURE\_TRUE), the effects of  $Q_0$  on parameter retrieval appear to be refrained, with different  $Q_0$  amounting to largely equivalent constraints, which leads to parameter convergence.

The insensitivity of parameter estimation to the magnitude of prescribed parameter error  $Q_0$  in the perfect-model-structure run (in which the forcing and observation error are also perfectly represented) is somehow analogous to results shown in Crow and Van Loon (2006), which demonstrated that, if the single error (only refer to random error, the model structure is perfect) source and observation error are both perfectly represented in the EnKF soil moisture data assimilation system, the overestimation of model error has little impact on the accuracy of retrieved state variable. This linkage implies that the results of parameter convergence (or not) shown here can be interpreted from the observational control perspective, where the structural accuracy might foster a robust relation between observation (invariant for different  $Q_0$ ) and the parameter update. This relationship is important to the availability of a relatively consistent trajectory for the sequential parameter search against the variation of  $Q_0$ . In this experiment, this connection can be partly reflected by the refrained updates of  $\alpha$  (in the ablation stage) where  $Q_0$  have been increased (Figure 10, also Table 5, same observation data are used in different simulations). On the other side, the structural error may distort the representation of parameter uncertainty through ensemble and attenuate this connection between observation (structural invariant) and parameter (in the problematic structure), therefore hinder the presence of a consistent parameter evolution among different  $Q_0$ . This deficiency can be well characterized by an excessively broad divergence zone in the corresponding  $Q_0$  space (Figure 3.11 and Table 3.6, same observation data are used in different simulations).

The detailed features associated with the  $Q_0$  space may be dependent on a number of complex issues such as the structural role in parameter estimation, which is modulated by the EnKF effects associated with ensemble space dynamics (e.g., using ensemble covariance to calculate increments), as well as the observation control on parameter evolution. Evaluation of the above potential explanations warrants further investigation, which may include how to measure these connections and mechanisms (e.g. between the degree of freedom  $Q_0$  and parameter evolution), whether they are ad-hoc, and what they are conditioned on.

In addition, the above parameter search divergence in DA\_STRUCT\_NEW could be alleviated by developing a more physically based method to estimate  $Q_0$  or predict the variance of parameter ensemble, for example, linking them to the flow-dependent error covariance of state variables (an approach similar to bias estimation in De Lannoy et al., 2008). When  $Q_0$  or parameter variance could be calculated through a physically robust scheme, this divergence problem becomes trivial, and the optimal parameter can be identified. However, a fully dynamical parameterization of these ensemble-space parameters can be difficult, considering the nature of parameter (a physically constant value) in the snow hydrological system.

### **3.6.2 Several limitations in current research**

This study may have limitations in several aspects. First, there are alternative approaches to achieve the simultaneous state and parameter estimation that do not require time varying parameter (ensemble) (e.g., Vrugt et al., 2005, Clark and Vrugt, 2006). The relative strengths and limitations among these algorithms are still not clear, and their

optimal design and application remain an active research area in the land surface system characterization (Moradkhani et al., 2005).

It is also recognized that the structural error and associated parameter adopted in my research are simplistic, because it only involves a specific parameterization equation. In this regard an extended study of temporal behavior of parameter statistics (e.g., ensemble mean) with elaborately perturbed structures in the EnKF simulation is suggested. Along this line I highlight the importance of testing large number of parameters embedded in multiple model structural components. Niu and Yang (2004) discussed several important physical processes governing snowpack evolution and their various representation in LSM, for example, canopy interception (with or without), radiation transfer (traditional scheme or revised two-stream), and below canopy turbulence. The uncertainties in simulating these processes can be incorporated into current framework as structural error. The interactions among these structural components may give rise to far more complicated results (e.g., different relations between  $Q_0$  and parameter search convergence) than those revealed in this work. In addition, because parameters in LSM can have significant and complex interactions (e.g., Rosero et al., 2009), it is worthy to investigate the appropriate size of parameters involved in this estimation framework, for example, whether to use all snowpack related parameters or to select part of them.

### **3.7 CONCLUDING REMARKS**

This study investigates the performance of parameter estimation in snow data assimilation experiments, and its dependency on the model structure. In the synthetic

EnKF simulation without model structure error, simultaneous state and parameter estimation is effective. The algorithm reduces the systematic error in SWE estimates and accurately retrieves the parameter values. Further, a suite of other land surface variables, especially those related to snowpack (and ground) energy balance, are better estimated when the parameters are correctly updated. Another important implication from this research is that, in the presence of model structural error, parameter search convergence and accurate estimation of state variables might not be simultaneously achieved, indicating the potential problem resulting from structure error. In particular, this work introduces a new degree of freedom, parameter variance constraint, in the parameter estimation framework, and find that imperfect-model-structure leads to parameter divergence over a broad zone in this constraint space. This is in contrast to the clearly retrieved parameter convergence in the perfect-model-structure run. These results demonstrate that with a problematic model structure, good performance in estimating state variables does not necessarily mean that the associated parameter estimation is reliable. In this sense, my investigation may provide a way for diagnosing structural robustness in the ensemble snow data assimilation system. It is also emphasized that the generality of this result should be investigated with a more complex structural error configuration (e.g., a combination of multiple structural components).

Table 3.1. Description of simulations in experiments.

SYN_CR	Synthetic ensemble simulation with parameters error but without synthetic data assimilation
DA_PAR_CR	Synthetic ensemble simulation with parameters error and synthetic data assimilation
DA_PAR_ $\alpha$	Synthetic ensemble simulation with parameters error, synthetic data assimilation and parameter estimation of $\alpha$
DA_PAR_ $\theta$	Synthetic ensemble simulation with parameters error, synthetic data assimilation and parameter estimation of $\theta$
DA_TRUE	Synthetic ensemble simulation with true parameters and synthetic data assimilation
SYN_TRUE	Synthetic truth from a particular forcing set and true parameters
DA_STRUCTURE_TRUE	Synthetic ensemble simulation with parameter error in $\alpha$ , other feature same to DA_TRUE
DA_STRUCTURE_NEW	Synthetic ensemble simulation with parameter error in $Z_d$ , also with equation (3.6), other feature same to DA_TRUE
DA_STRUCTURE_TRUE_2	Synthetic ensemble simulation with parameter error in $Z_d$ , assimilates observation from another synthetic true with equation (3.6), other feature same to DA_TRUE
DA_STRUCTURE_NEW_2	Synthetic ensemble simulation with parameter error in $\alpha$ , assimilates observation from another synthetic true with equation (3.6), other feature same to DA_TRUE.

Table 3.2. The *Nash-Sutcliffe* efficiency for ensemble mean of different simulation shown in Figure 3.1. The value equal to 1 represents the perfect simulation, with the value the larger the better.

DA_TRUE	DA_PAR_α	DA_PAR_θ	DA_PAR_CR	SYN_CR
0.98	0.96	0.61	0.22	-1.21

Table 3.3. The temporal averaged error in SWE (ensemble mean minus the true value) for parameter estimation run DA\_STRUCT\_TRUE with different  $Q_0$  shown in Figure 3.8. Here  $Q_0$  is represented by standard deviation ( $\sqrt{Q_0}$ ), which is equal to R multiplying the initial parameter:  $\text{Std}=\text{R} * \alpha_0$ .

R	1/4	1/2	3/4	1	3/2
Error (mm)	7.49	11.36	8.08	7.68	7.71

Table 3.4. The temporal averaged error in SWE (ensemble mean minus the true value) for parameter estimation run DA\_STRUCT\_NEW with different  $Q_0$  shown in Figure 3.9. Here  $Q_0$  is represented by standard deviation ( $\sqrt{Q_0}$ ), which is equal to R multiplying the initial parameter: Std=R\*  $\alpha_0$ .

R	1/4	1/2	3/4	1	3/2
Error (mm)	19.96	8.86	8.61	8.63	8.62

Table 3.5. The ensemble mean of  $\alpha$  retrieved in DA\_STRUCT\_TRUE when ground is snow-free in May (for every ensemble member), as a function of different  $Q_0$  constraining the parameter variance. Here  $Q_0$  is represented by standard deviation ( $\sqrt{Q_0}$ ), which is equal to R multiplying the initial parameter: Std=R\*  $\alpha_0$ .

R	1/8	1/4	1/2	3/4	1	11/4	3/2	2	5/2	3
$\bar{\alpha}$	1.70	1.72	1.73	1.77	1.78	1.79	1.81	1.83	1.89	1.96

$$\frac{\bar{\alpha}_{Max} - \bar{\alpha}_{Min}}{\bar{\alpha}_{Min}} = 0.152$$

Table 3.6. The  $\overline{Z_d}$  retrieved in DA\_STRUCT\_NEW when ground is snow-free in May (for every ensemble member), as a function of different  $Q_0$  constraining the parameter variance. Here  $Q_0$  is represented by standard deviation ( $\sqrt{Q_0}$ ), which is equal to R multiplying the initial parameter: Std=R\*  $Z_{d0}$ .

R	1/8	1/4	1/2	3/4	1	11/4	3/2	2	5/2	3
$\overline{Z_d}$	0.0026	0.0042	0.0070	0.0090	0.0108	0.0129	0.0142	0.0181	0.0266	0.0362

$$\frac{\overline{Z_{d Max}} - \overline{Z_{d Min}}}{\overline{Z_{d Min}}} = 12.9$$

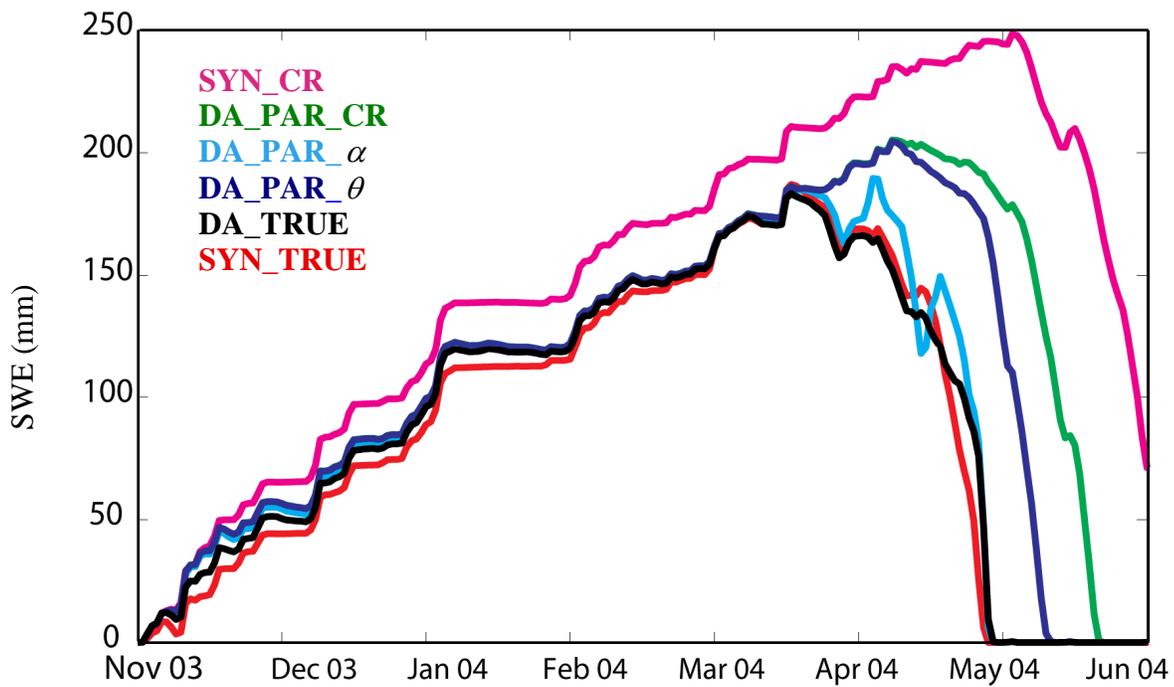


Figure 3.1. Ensemble mean simulations of SWE (mm) for SYN\_CR, DA\_PAR\_CR and SYN\_TRUE, DA\_PAR\_α, DA\_PAR\_θ, DA\_TRUE. (see Table 3.1 for the description of these simulations).

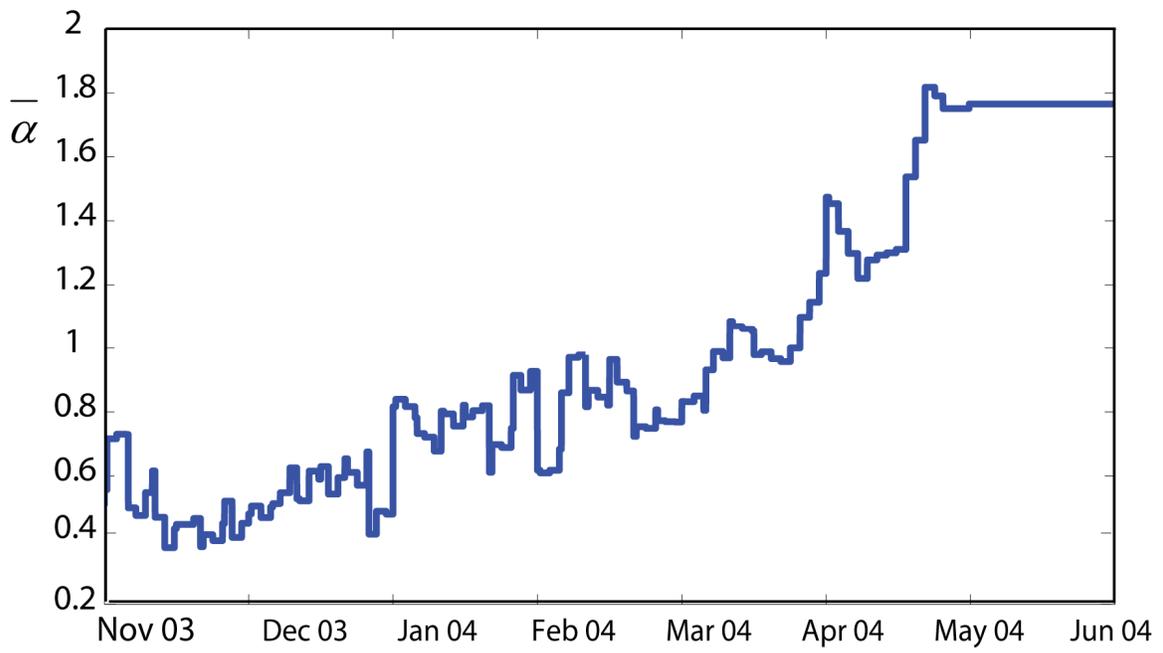


Figure 3.2. Parameter ensemble mean of  $\alpha$  in DA\_PAR\_ $\alpha$ .

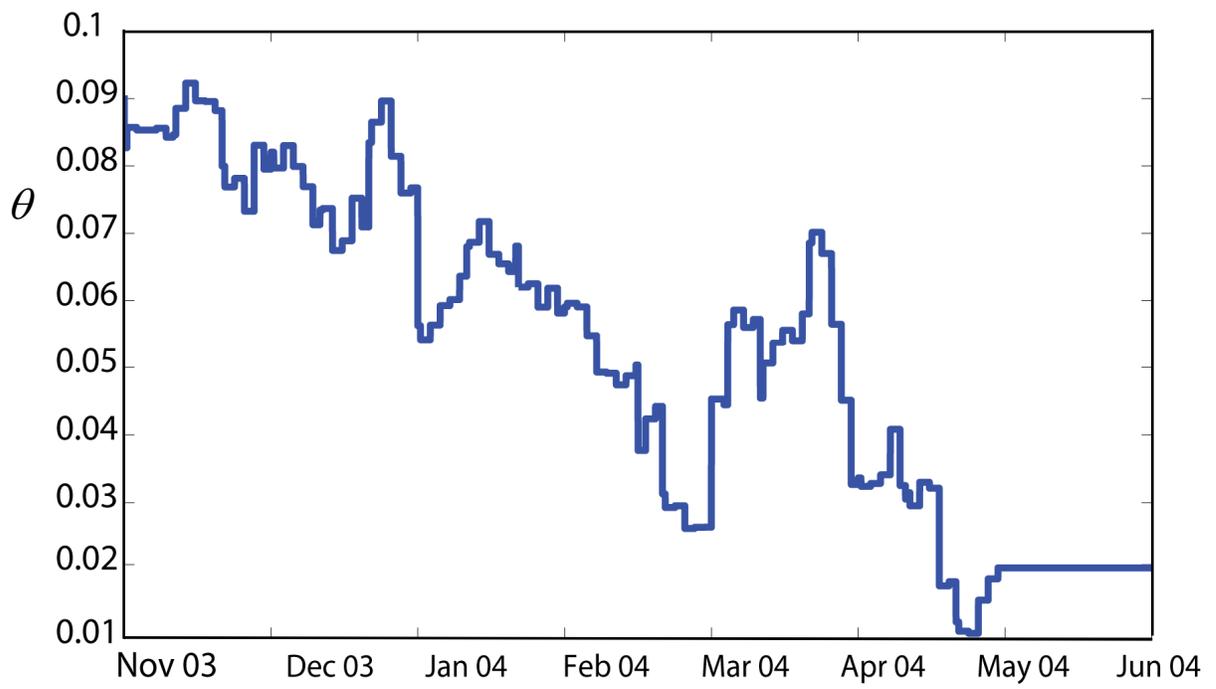


Figure 3.3. Parameter ensemble mean of  $\theta$  in DA\_PAR\_ $\theta$

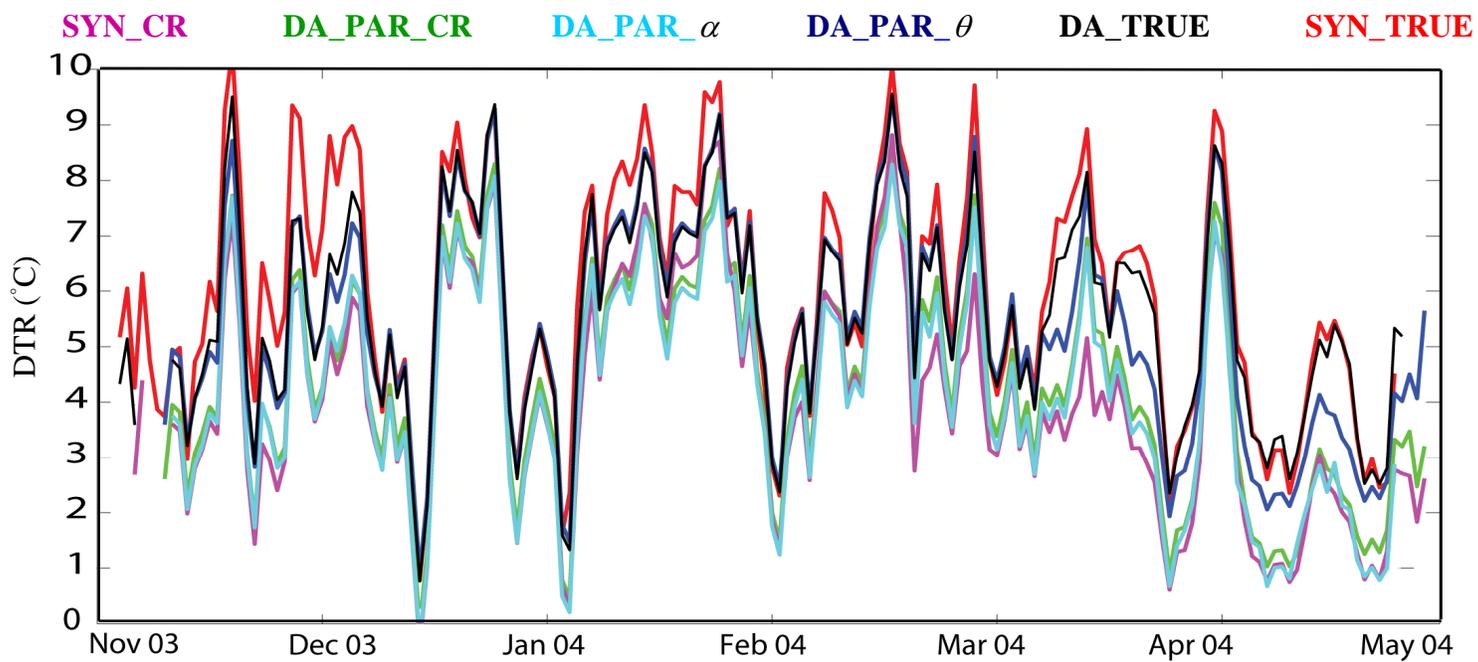


Figure 3.4. Ensemble mean of DTR (diurnal temperature range) for SYN\_CR, DA\_PAR\_CR and SYN\_TRUE, DA\_PAR\_α, DA\_PAR\_θ, DA\_TRUE.

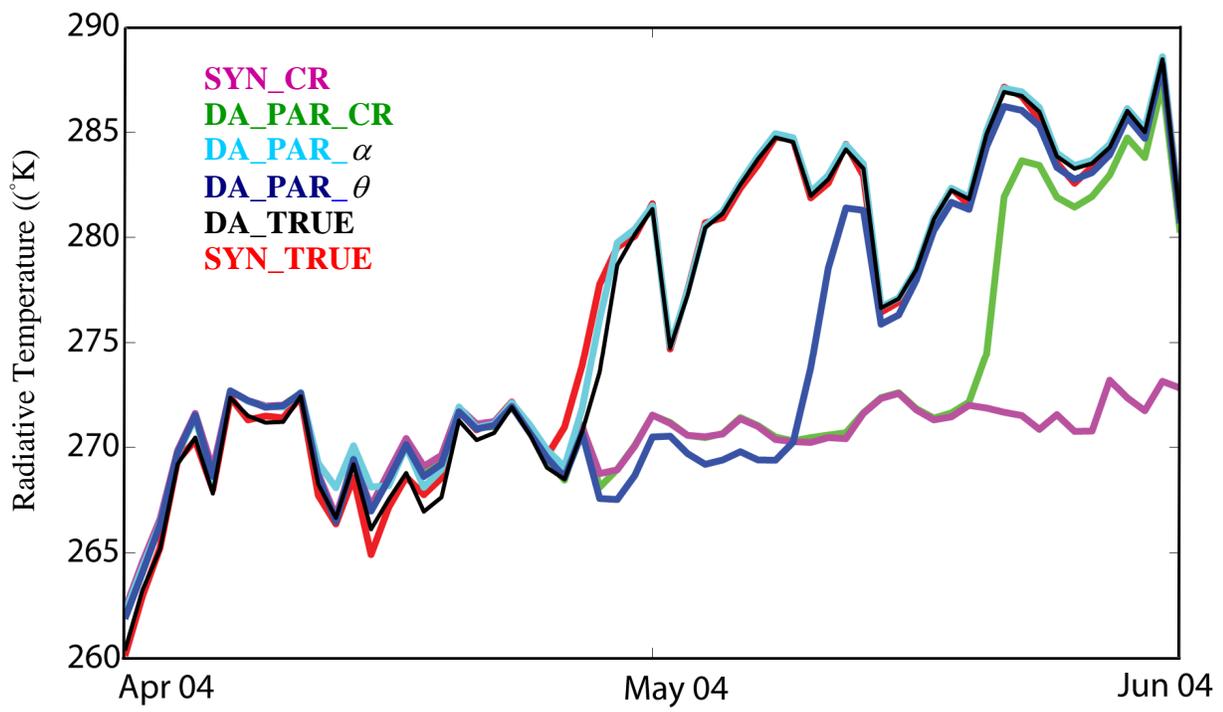


Figure 3.5. Daily averaged ensemble mean of ground radiative temperature for SYN\_CR, DA\_PAR\_CR and SYN\_TRUE, DA\_PAR\_α , DA\_PAR\_θ , DA\_TRUE.

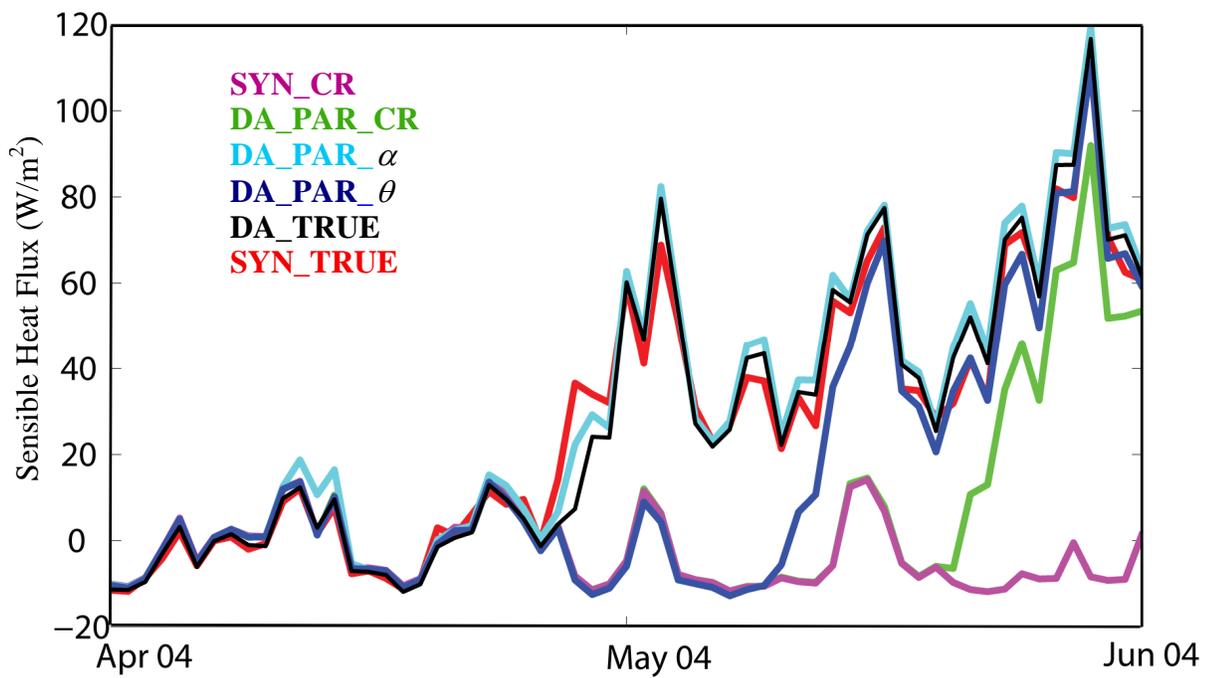


Figure 3.6. Daily averaged ensemble mean sensible heat flux for SYN\_CR, DA\_PAR\_CR and SYN\_TRUE, DA\_PAR\_α, DA\_PAR\_θ, DA\_TRUE.

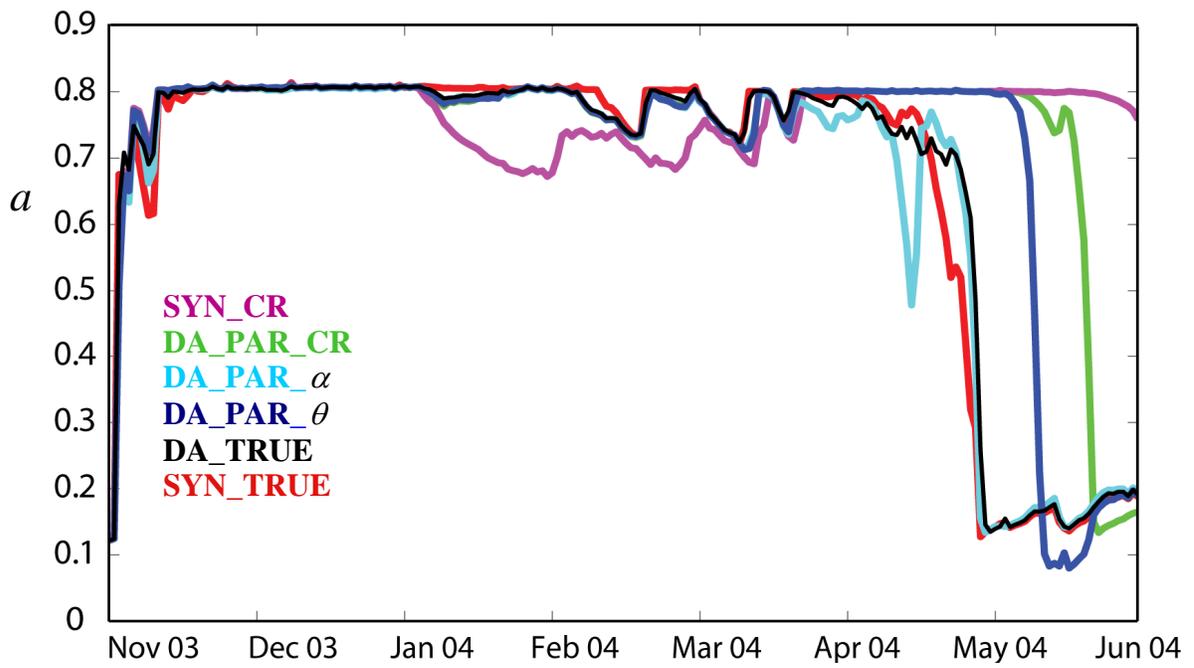


Figure 3.7. Daily averaged ensemble mean albedo for SYN\_CR, DA\_PAR\_CR and SYN\_TRUE, DA\_PAR\_α, DA\_PAR\_θ, DA\_TRUE.

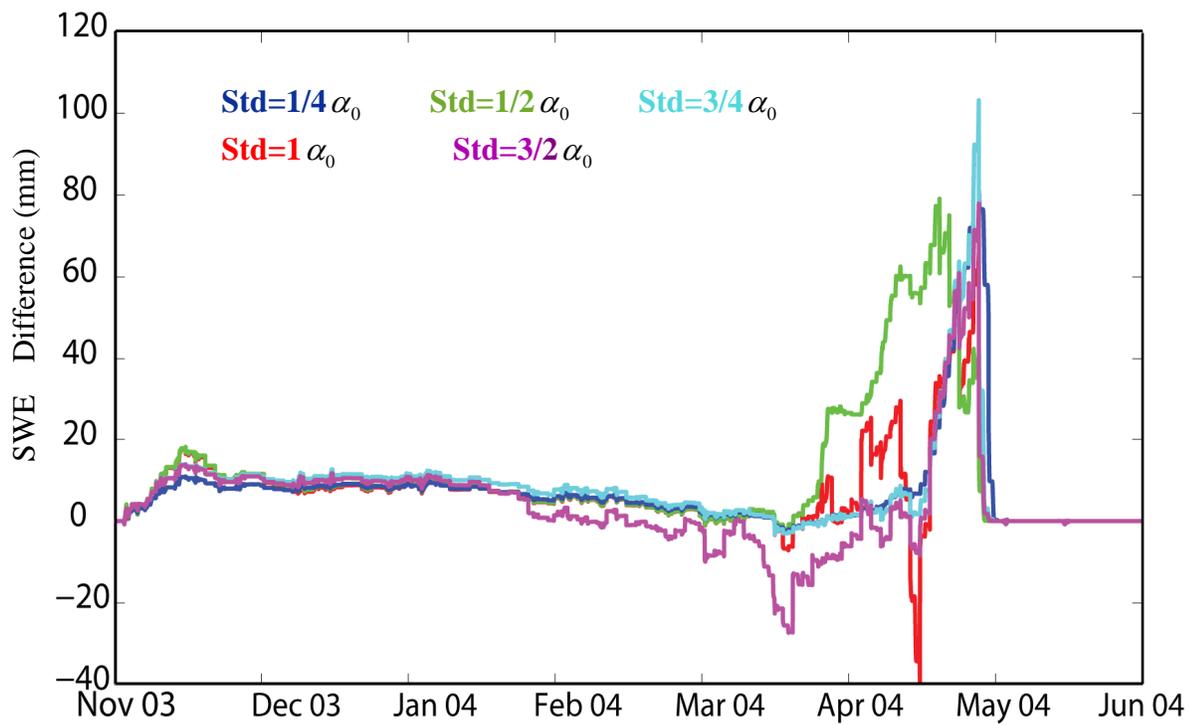


Figure 3.8. Ensemble mean error in SWE (mean – true value) for DA\_STRUCT\_TRUE with different  $Q_0$  constraining the parameter variance.

Here  $Q_0$  is represented by standard deviation ( $\sqrt{Q_0}$ ), which is equal to R multiplying the initial parameter:  $\text{Std}=\text{R} * \alpha_0$

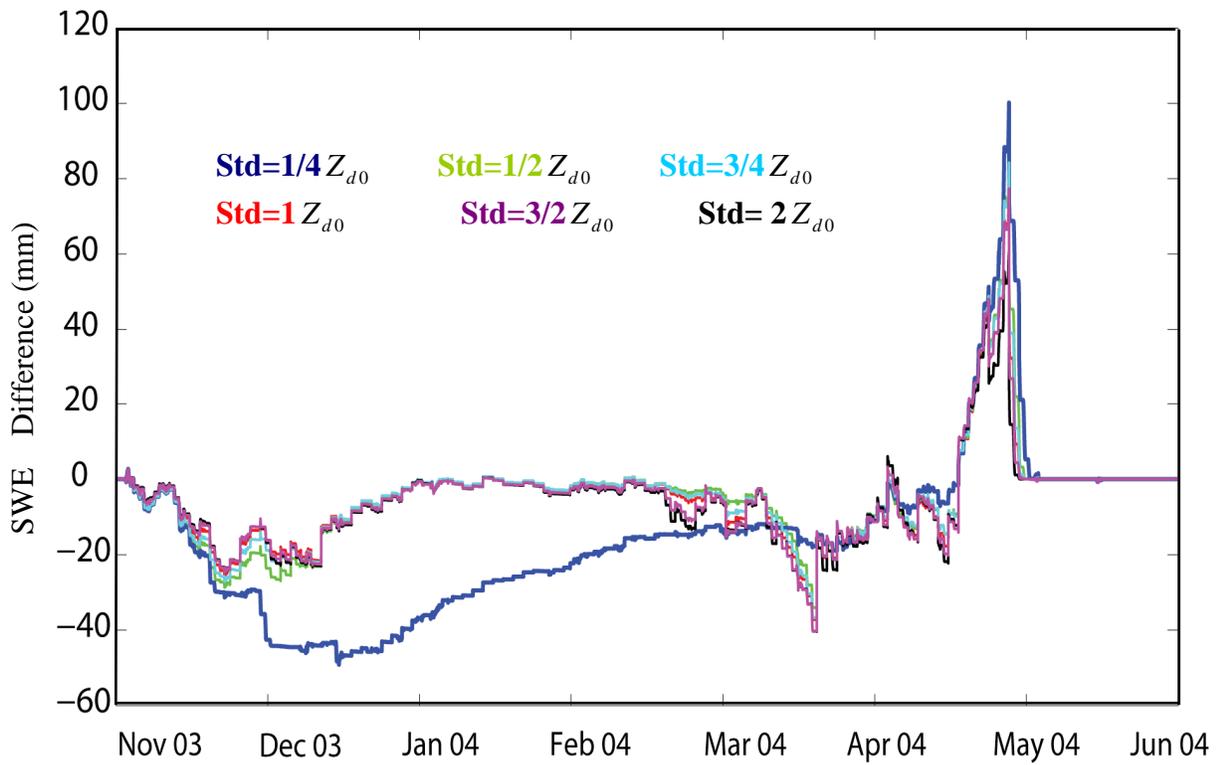


Figure 3.9. Ensemble mean error in SWE (mean – true value) for DA\_STRUCT\_NEW with different  $Q_0$  constraining the parameter variance.

Here  $Q_0$  is represented by standard deviation ( $\sqrt{Q_0}$ ), which is equal to R multiplying the initial parameter:  $\text{Std} = R * Z_{d0}$

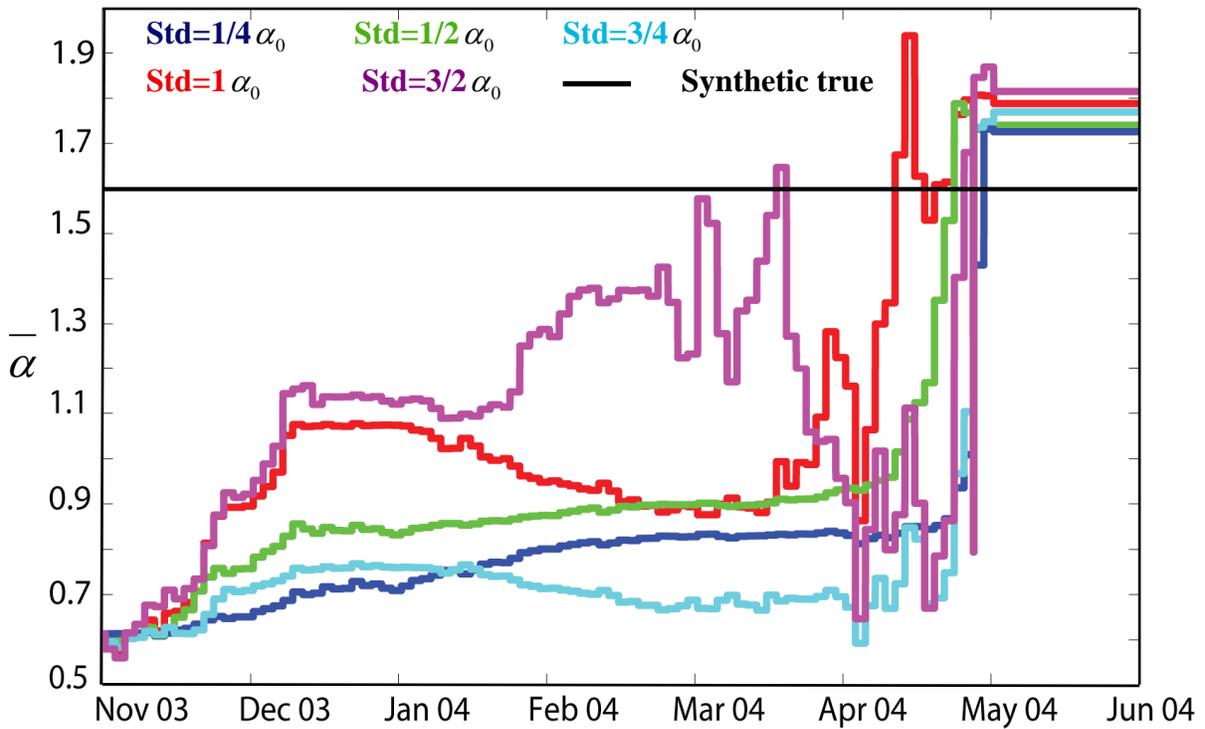


Figure 3.10. Parameter ensemble mean for DA\_STRUCT\_TRUE with different  $Q_0$  constraining the parameter variance.

Here  $Q_0$  is represented by standard deviation ( $\sqrt{Q_0}$ ), which is equal to R multiplying the initial parameter:  $\text{Std}=\text{R} * \alpha_0$

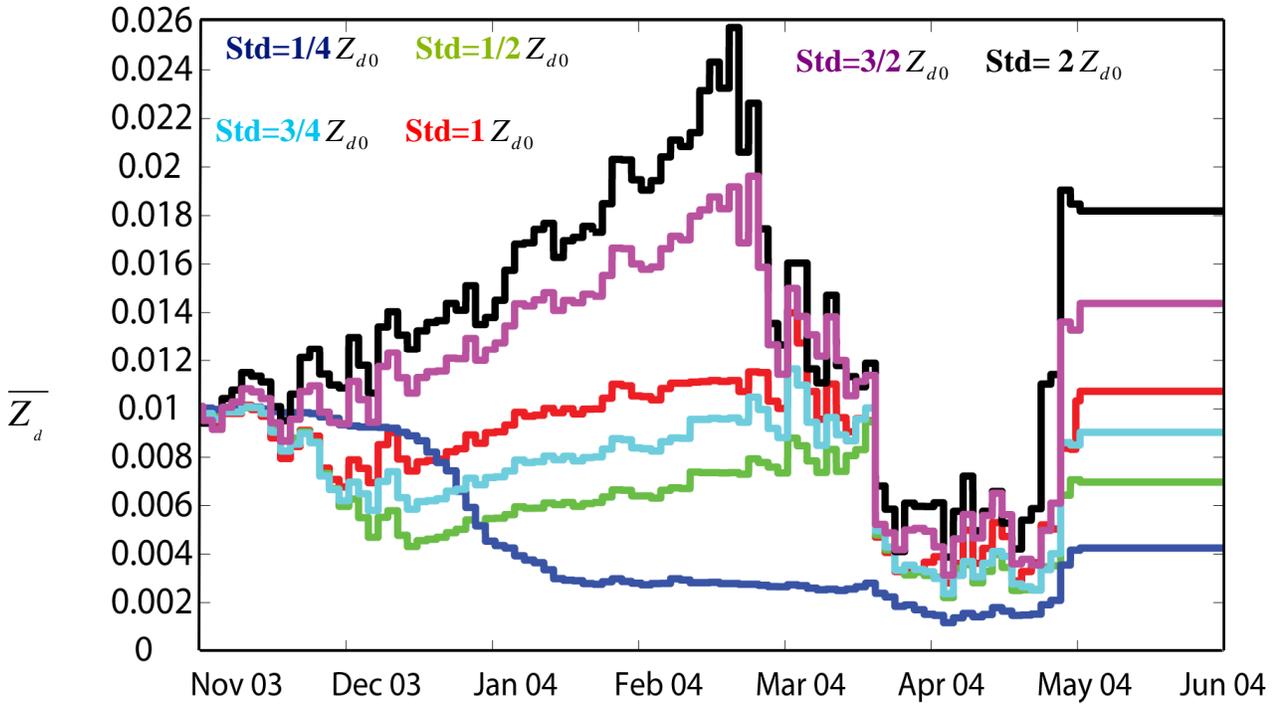


Figure 3.11. Parameter ensemble mean for DA\_STRUCT\_NEW with different  $Q_0$  constraining the parameter variance.

Here  $Q_0$  is represented by standard deviation ( $\sqrt{Q_0}$ ), which is equal to R multiplying the initial parameter:  $\text{Std} = R * Z_{d0}$

## **Chapter 4: Multi-sensor snow data assimilation at continental-scale: the value of GRACE TWS information**

### **4.1 ABSTRACT**

This investigation establishes a multi-sensor snow data assimilation system (for data over North America from Jan 2002 to Jun 2007) with improved estimation of snowpack (in particular, SWE and snow depth) by incorporating both GRACE TWS and MODIS SCF information into the CLM. The different properties associated with the TWS and SCF observations have been accommodated through a unified approach using the ensemble Kalman filter (EnKF) and smoother (EnKS). Results show that this multi-sensor approach can provide significant improvements over the traditional MODIS only approach, for example, in Saint Lawrence, Fraser, Mackenzie, Churchill & Nelson, and Yukon river basins, and the south-west rim of Hudson Bay. In mid-latitudes, for example, the North Central and Missouri river basins, inclusion of GRACE information preserves the advantages (compared with Open Loop) shown in the MODIS only run. However, in some high latitude areas and given months, the open loop run can have a comparable or even better performance, implying considerable room for refinements of the multi-sensor algorithm. In addition, ensemble based metrics are calculated and interpreted at domain wide. They indicate the potential importance of accurate representation of SWE auto-covariance in assimilating TWS observations, and the regional and/or seasonal dependence of the GRACE capability in reducing ensemble variance. These analyses contribute to clarifying the effects of GRACE's special features (e.g., a vertical integral

of different land water storage changes, coarse spatial and temporal resolution) in the snow data assimilation system.

## **4.2 INTRODUCTION**

Snow is an important component of the earth climate system. At continental and inter-annual scales SCF and SWE have large variations, depending on atmospheric circulation patterns. High albedo and low thermal conductivity of snow significantly affect land surface energy and water budgets. Consequently, accurate estimation of snowpack properties at large scale is important for various research areas, for example: (1) hydrological prediction and water resources management, especially for those regions in which fresh water availability is heavily dependent on snow melt (Barnett et al., 2005); (2) evaluation of coupled General Circulation Models (GCMs) in terms of their ability to represent observed snow dynamics (Frei and Gong, 2005); (3) climate trend quantification in cold regions; and (4) land-atmosphere-ocean interactions associated with snow cover (Gong et al., 2003).

In recent years, derivation of high quality snow datasets, SWE in particular, has increasingly relied on data assimilation technology, which optimally blends numerical model results and remotely sensed information to generate more accurate and physically consistent products. Compared with ground observations that are scattered and often do not represent regional averages, satellite observations effectively expand the spatial coverage to regional and continental scales. Among satellites observations, SCF products are unique in their estimation of SWE distribution when compared with other products, such as microwave-based estimates. Snow has distinct reflectance effects in visible and

infrared bands (Hall et al., 2002), which can be measured at relatively high spatial resolution (Hall et al., 2002; Hall and Riggs, 2007). Further, the SCF retrieval with these algorithms does not require information about the micro-scale internal properties of snowpack, for example, density, grain size, and liquid water content, although implicit relations may be involved. Consequently, remotely sensed SCF information has been increasingly used to correct SWE estimates from land surface models (LSMs), via the EnKF technology (e.g., Andreadis and Lettenmaier, 2006; Clark et al., 2006; Su et al., 2008). However, a number of limitations degrade the quality of assimilated SWE products, or hamper application in specific climatic and geographic environments, including:

(1) Low correlation between SCF and SWE when model grid averaged SWE exceeds a threshold. In this situation, small changes in SCF lead to a wide range of SWE for a given location. Several studies (Clark et al., 2006; Su et al., 2008) found the SCF assimilation performs best with partial snow cover (e.g., ephemeral snow in mountains and grasslands), but performs poorly when the SCF signal is saturated (near 100% SCF) and insensitive to further SWE increments (e.g., during the accumulation season over boreal forest and tundra).

(2) Parameter errors in the observational operator. A key component of the SCF approach is a parameterized relationship (observation operator or function) between SCF and SWE at each model grid. Various observation functions have been utilized in the literature (Andreadis and Lettenmaier, 2006; Clark et al., 2006; Su et al., 2008), each having some key parameters characterizing geographic and scale effects. These

distributed parameters are usually difficult to measure (because they rely on intensive calibration) and their errors can degrade SWE retrievals.

(3) Errors in satellite-derived SCF data. Although the EnKF algorithm can account for observational noise, SCF error magnitude (variance) can be difficult to quantify in certain environments like mountains (Hall and Riggs, 2007), or when obscured by cloud cover and vegetation (Hall and Riggs, 2007). These environments can also lead to systematic errors not accommodated by current data assimilation systems.

These three types of errors tend to be magnified when present simultaneously. For example, if the SCF signal is saturated during a boreal forest winter, a small amount of bias in SCF data or uncertainty in parameters may lead to significant errors in the observation operator and hence SWE update.

All these limitations motivate me to develop a new methodology for improving continental scale SWE and relevant estimates, using additional information from other satellites. Because SCF observations mainly characterize the spatial distribution of snowpack, inclusion of further model constraints such as mass and energy terms should be complementary. An analogous approach has been applied in estimating soil moisture, evapotranspiration, and other hydrological states and fluxes (Renzullo et al., 2008), where multiple data resources are shown to improve estimates. Nevertheless, there has been little research devoted to exploring the nature of multi-sensor or multi-frequency (for radiometer) snow data assimilation. Among the first studies are those of Durand and Margulis (2006, 2007), but their synthetic experiments are confined to point and river basin scale snowpack, and focus on radiometric observations.

Monthly global TWS estimates have been available from the GRACE satellite system since 2002. GRACE provides estimates of total surface mass change from month to month using changes in Earth's gravity field, with a spatial resolution comparable to satellite altitude of about 400 km. Thus, unlike visible band instruments, GRACE can monitor ground under all-weather conditions (as do microwave radiometers) and measures integrated total land water storage changes from canopy to deep groundwater. Much research has focused on extracting from GRACE meaningful trends and variabilities of individual TWS components (e.g., soil moisture, snow, groundwater) (Syde et al., 2008; Rodell et al., 2004; Niu et al., 2007). More recently Zaitchik et al (2008) incorporated GRACE TWS data into a land surface model using an ensemble Kalman smoother (EnKS) to improve water storage and flux estimates in the Mississippi River basin (where snowpack was simply updated without direct calculation of SWE increments from its ensemble statistics).

In this study I use GRACE TWS measurements to complement MODIS SCF data assimilation over North America. Integration of radiometer (at visible and infrared bands) and gravity measurements into a land surface model over such a large domain has received little attention. Accordingly I focus on the following questions: How can the two types of snow information that have distinct physical and geographic features be jointly assimilated? Can GRACE data assimilation improve SWE and snow depth retrieval, relative to MODIS only data assimilation? How do these improvements (multi-sensor vs. single sensor), if any, vary geographically and with what underlying mechanisms? Specific attention is given to the special properties of GRACE TWS data (its spatial and temporal resolution). Some controlling factor for GRACE TWS assimilation and its

capability of reducing errors were interpreted quantitatively. The central purpose was to develop observational and algorithmic techniques for accurately characterizing SWE and other cold region hydrological variables.

Section 4.3 introduces data and methods applied in the data assimilation experiments. Section 4.4 describes in detail how these experiments were implemented. The results are analyzed in section 4.5 and section 4.6 provides interpretations and comments on specific features of the multi-sensor data assimilation. Concluding remarks are given in section 4.7.

## **4.3 DATA AND METHODOLOGY**

### **4.3.1. MODIS and GRACE satellite datasets**

Daily MODIS SCF data at  $0.05^\circ$  resolution (MOD10C1) are used in this study. MODIS uses 7 spectral bands to retrieve land surface properties. Its snow mapping algorithm estimates SCF using Normalized Difference of Snow Index (NDSI) (Hall et al., 2002), and is able to distinguish between snow and clouds (Hall et al., 2002). Su et al. (2008) described the MODIS data processing used in this study, including spatial upscaling of raw data and cloud parameter selection for quality control.

GRACE monthly gravity fields are represented as spherical harmonics to degree and order 60, with most time variable atmospheric and oceanic gravitational effects removed during data processing. Remaining gravity changes are interpreted as monthly changes in vertically integrated water storage components, for example, snow, soil moisture, and groundwater. GRACE estimates are smoothed with a Gaussian averaging kernel with a 500 km radius, and filtered to remove longitudinal stripes that are a

recognized noise component in current solutions (Chen et al., 2008). GRACE estimates are then represented on 4 ° by 4 ° tiles using bilinear interpolation for compatibility with the model grid configuration (1 ° by 1 ° over North America). These time series span the period from November 2002 to May 2007, with missing values in December 2002 and June 2003. Here the TWS data are in their multi-year anomaly form, in which the long term mean of TWS is subtracted from each monthly value. In practice, GRACE time series values are computed from observations taken from about one-half month before to one-half month after the date assigned to the sample.

According to their physical features, MODIS and GRACE contain different information relevant to SWE retrieval. MODIS measures SCF at high spatial resolution compared to both GRACE and the numerical model, observing both accumulation and ablation with approximately the same level of accuracy. GRACE measures total column water storage change at a far coarser spatial and temporal scale, and does not contain information about the individual components contributing to water storage changes. However, SWE is expected to be the dominant variable component of TWS in winter in cold regions (Niu et al., 2007). Its relative contribution diminishes during melting, when MODIS is thought to be more closely correlated to SWE. GRACE estimates are not affected by vegetation (except as its mass changes), topography and cloud cover, and is useful in conditions when the value of MODIS is limited by these influences.

#### **4.3.2 Observation based climatologic SWE and snow depth datasets**

The Canadian Meteorological Center (CMC) snow depth and SWE climatology data (1969-1997) (Brown et al., 2003) were used for validation purpose. These provide daily

snow depth and SWE at 0.25 ° resolution. The snow estimates were obtained by combining abundant station observations in U.S. and Canada with model simulations by an optimum interpolation scheme (Brown et al., 2003). These observationally based datasets are regarded as the best available reference for this research.

#### **4.3.3 Land surface model**

The CLM used in these experiments includes an enhanced frozen soil hydrology scheme and a new aquifer dynamical scheme, among other modifications (Niu and Yang, 2006; Niu et al., 2007). The aquifer model, by explicitly simulating ground water dynamics, facilitates assimilating TWS observations. Water storage in the saturated zone is a prognostic variable and directly represented in the calculation of TWS in each grid, facilitating combination of GRACE data with model estimates (Zaitchik et al., 2008). In addition, CLM's sophisticated representation of frozen soil hydrology has improved its ability to characterize soil moisture and runoff variability in cold regions, thus reducing the systematic error in TWS estimation. These enhancements reduce model biases (see Niu and Yang, 2006; Niu et al., 2007 for more discussion). The negative effects of model biases cannot be eliminated by updating state variables alone, and model bias can result in complex effects into the data assimilation system (e.g., c.f. De Lannoy et al. , 2008).

#### **4.3.4 The ensemble Kalman filter and smoother**

The EnKF (Evensen, 1994, 2003) and EnKS are used to incorporate MODIS and GRACE data into CLM, respectively. The choice of algorithms (the EnKF for MODIS SCF assimilation and EnKS for GRACE TWS assimilation) depends on the nature of satellite datasets.

The EnKF treats some crucial model inputs, such as forcing data, model parameters, and model initial conditions, as random variables, and ensembles of these inputs are generated to represent their distributions. Each ensemble member is propagated forward using the model until a measurement becomes available. The measurement is assimilated into the model simulation by using the ensemble of state variables to represent a low-rank approximation of the joint pdf between state variables and measurements. The EnKF update is optimal only when certain assumptions are met: (1) unbiased measurements and background (model simulated) variables; (2) Gaussian type random inputs (e.g., the forcing errors); and (3) linear relationships between states and measurements. Given the above properties, the EnKF is able to characterize highly nonlinear land hydrological processes and their associated uncertainties. Such sequential data assimilation accounts for the temporal sampling discrepancy between CLM (3-hours) and MODIS data (daily), as discussed in Su et al. (2008) where additional details are provided.

The EnKS (Dunne et al., 2005, 2006) is theoretically similar to the EnKF but allows for observations that: (1) are defined at different times than the model state; and (2) span multiple periods of time comprising, for example, both current and historical model states. Because GRACE data are at monthly intervals and CLM runs at three hours, the EnKS is used to compare model estimates of TWS with those of GRACE and derive updates for state variables. The update of the EnKS is:

$$X_{i,t}^a = X_{i,t}^b + K_{t,T1}(Y_{T1} - H_{T1}(X_{i,t}^b) + v_{T1}^i) \quad (4.1)$$

where  $X_{i,t}^a$  represents the updated  $i$ th ensemble member of the state vector,  $X_{i,t}^b$  represents the corresponding ensemble member simulated by the model. The ensemble

state vector is defined at time  $t$ , which can be a daily average value and differs from the GRACE observation  $Y_{T1}$  (monthly TWS anomaly with respect to a multi-year mean) defined for a month  $T1$ .  $H_{T1}(X_{i,t}^b)$  is the observation function for the month  $T1$ , as obtained by integration of model TWS components over all grids within the GRACE tile ( $4^\circ$  by  $4^\circ$  in this study), and over all days within the month  $T1$ . The noise term  $v_{T1}^i$  is randomly drawn from a Gaussian distribution (with zero mean and the variance equal to that of the observation error) to ensure an adequate spread of the analysis ensemble members (Burgers et al., 1998). The Kalman gain  $K_{t,T1}$  is obtained with the same ensemble approach as used in the EnKF,

$$K_{t,T1} = Cov(X_t^b, H_{T1}(X_t^b)) [Cov(H_{T1}(X_t^b), H_{T1}(X_t^b)) + R_{T1}]^{-1} \quad (4.2)$$

where  $R_{T1}$  is the auto-covariance of observation error. The auto-covariance of model simulated observation ( $Cov(H_{T1}(X_t^b), H_{T1}(X_t^b))$ ), and cross covariance ( $Cov(X_t^b, H_{T1}(X_t^b))$ ), are estimated from inner products of corresponding ensemble ( $X_{i,t}^b$  and  $H_{T1}(X_{i,t}^b)$ ) anomalies (which are ensemble minus their mean).

The EnKS provides a reasonable way to match GRACE estimates of changes in TWS to each model simulated day. In reality GRACE estimates incorporate varied information about any particular geographical location because orbits do not repeat. Thus it is difficult to set a uniform frequency and associated time accurately characterizing the satellite track at each grid. The approach appears justifiable because with slow temporal variation at large spatial scales, the monthly samples should adequately describe TWS.

#### 4.4 IMPLEMENTATION OF THE DATA ASSIMILATION EXPERIMENTS

Three experiments were designed to address questions stated in section 4.2. One is the open loop (OL) simulation where CLM alone is used to estimate SWE and other land variables. Second is a MODIS only (MOD) data assimilation experiment similar to that used in Su et al. (2008). Third is the joint MODIS\_GRACE (MOD\_GR) data assimilation experiment.

All simulations are driven by the meteorological forcing dataset from the Global Land Data Assimilation System (GLDAS) at  $1^{\circ} \times 1^{\circ}$  resolution. The GLDAS forcing data are observationally derived fields including precipitation, air temperature, air pressure, specific humidity, and shortwave and longwave radiation. The forcing data (e.g., precipitation) biases are not explicitly accounted for in this data assimilation approach, because of the lack of such information. CLM was run with data from Jan, 2002 to June, 2007. The ensemble runs do not assimilate observations until Nov, 2002. In MOD\_GR, the relative error in log-normal perturbation of precipitation is 65%, and the e-folding scale of horizontal error correlations is  $3^{\circ}$  (in both latitude and longitude) for precipitation and temperature. A temporal correlation of 3 days is assumed for the forcing perturbation. The selection of these forcing parameters is based on previous research on GRACE data assimilation (Andreadis and Lettenmaier, 2006; Zaitchik et al, 2008). These parameters are also applied in MOD. Additional experiments show that the change of forcing error parameters in Su et al. (2008) to the above values did not influence the MOD run significantly, and the main purpose here is to keep them the same in both MOD and MOD\_GR. All other ensemble parameters in MOD and MOD\_GR are the same as in Su et al. (2008). It is recognized that a more comprehensive description of forcing error

(e.g., only errors in precipitation and temperature are considered in this research) needs to be included in further research. The ensemble size is 25, which has been demonstrated to be suitable for large scale snow data assimilation in Su et al. (2008). Here only describes implementation of MOD\_GR with EnKS.

At each day in a given month, the MODIS SCF is integrated into the ensemble simulation at every  $1^\circ \times 1^\circ$  model grid as performed in the MOD experiment. Here a “fixed interval state inflation” is applied, which periodically augments the ensemble spread of SWE at all tiles in every CLM grid. Specifically, the SWE simulation takes the form of

$$x_{SWE,t} = f(x_{SWE,t-1}, p_t) + \omega_t \quad (t = \text{every } q \text{ days}) \quad (4.3)$$

every  $q$  days. Here  $f$  represents CLM,  $\omega_t$  represents the perturbation on the state variable  $x_{SWE,t}$  with variance of  $Q$ ,  $p_t$  represents the perturbed forcing. At other steps the SWE is simulated by the function  $f$  without any state inflation:

$$x_{SWE,t} = f(x_{SWE,t-1}, p_t) \quad (t = \text{other time steps}) \quad (4.4)$$

(note that if after inflation, SWE is below or equal to zero, then the inflation is not given).

This inflation scheme is tailored to the needs of ensemble simulation of SWE. The absence of inflation may lead to too small a spread of the ensemble, degrading EnKF and EnKS performance. On the other hand, too frequent an inflation can cause excessive ensemble spread and unrealistic updates. Augmenting the state at each time step is not necessary because the main source of SWE uncertainties, the forcing uncertainty, has been dealt with elsewhere. For this reason, the selection of  $q$  and  $Q$  is largely application specific, and here  $q = 6$  and  $Q = 36 \text{ mm}^2$  (which are representative in both MOD and MOD\_GR, as demonstrated below) are taken as domain-wide values for both

MOD and MOD\_GR. This study does not address development of more objective ways to select these parameters, such as the adaptive filter algorithm (Reichle et al., 2008). My initial tests found that for MOD run, state inflation using parameters ( $q_1$  and  $Q_1$ ) within a reasonable range ( $q_1 \geq 3$  and  $Q_1 \leq 60\text{mm}^2$ , which includes the case of no inflation) affected (relative to the observational data of CMC) the data assimilation results slightly; for MOD\_GR run, a similar range ( $3 \leq q_2 \leq 8$  and  $20\text{mm}^2 \leq Q_2 \leq 100\text{mm}^2$ ) exists in which the changes in  $q_2$  and  $Q_2$  also affected little (relative to observation data CMC) the data assimilation results. Parameters that are significantly outside the above ranges would dramatically alter the results in two experiments by degrading the quality of the SWE estimates when compared with the observational dataset of CMC (detailed results are not shown here).

At the end of the month when all the MODIS data have been assimilated, GRACE TWS information (on  $4^\circ$  by  $4^\circ$  tiles) is optimally distributed into the archived daily state vector (on  $1^\circ \times 1^\circ$  grids) consisting of the daily averaged SWE, snow depth, canopy snow, soil moisture, and aquifer storage. This spatial and temporal disaggregation is accomplished by using the EnKS (equation 1) with GRACE observation error  $\sqrt{R_{T1}}$  set to 20 mm, consistent with previous studies (e.g., Zaitchik et al, 2008). Because the observation  $Y_{T1}$  in equation (4.1) is an anomaly value (with respect to a mean over the GRACE observation period),  $H_{T1}(X_{i,t}^b)$  takes into account model TWS climatology at each GRACE tile. The state vector at the last step of each month is updated with equation (4.1), then propagated by the model to next month to repeat the above data assimilation cycle.

The above method utilizes each daily ensemble of state variables ( $X_{i,t}^b$  in equation (4.1)) to calculate the corresponding Kalman gain to give a theoretically robust estimate of data assimilation increments, although these updates are not involved in the model propagation. The memory of state variables update is represented by reinitializing the simulation (with the updated state vector) at the last step of each month. My adaptation of the EnKS could be improved, given the complexity resulting from the temporal scale difference between GRACE data and model.

## **4.5 RESULTS**

This work focuses on evaluating the estimates of SWE and other snow variables, even though other updated land surface states and fluxes are also provided by the MOD\_GR simulation. An extensive assessment of the improvement in all the other hydrological variables from the multi-sensor snow data assimilation should be addressed in future research (initial analyses find that the impacts of MOD and MOD\_GR on estimation of water and energy fluxes (e.g., latent and sensible heat, runoff etc.), are small at monthly scale).

### **4.5.1 Monthly SWE difference between MOD and MOD\_GR**

The spatial distribution of SWE differences between single-sensor (MOD) and multi-sensor (MOD\_GR) experiments illustrates the incremental value of GRACE information. Figure 4.1 shows that this monthly averaged field has considerable spatial heterogeneity in the cold season (Jan-Apr). Large changes in the SWE estimate of the MOD\_GR run (compared to MOD) are concentrated in high latitude regions. In

particular, lower SWE estimates are found in boreal forests, with the difference ranging from 20 mm in January to 100 mm in April. In the tundra region of the Arctic SWE estimates are higher by up to 30 mm (in April) after assimilating GRACE data. All of these differences correlate well with the period of snow accumulation, which starts around January and peaks in April. In contrast, the northern Great Plains and mid-west mountainous area show little change.

Monthly difference fields in other years demonstrate similar patterns, although the sign of the difference may vary from year to year. A detailed investigation of the sign and its spatial and temporal variation would involve quantitative analyses of several complicated factors, including the SCF parameterization curve, MODIS data bias, and others. The interaction of these components may be complex as demonstrated in section 4.2, and is not a focus here.

Generally, the distinct patterns of differences in Figure 4.1 are consistent with remarks about strengths and limitations of SCF data assimilation presented in section 4.2. In the regions where the SCF signal is saturated (boreal forest and tundra) and the correlation between SCF and SWE is low, the TWS signal is still sensitive to SWE variation and so the EnKS algorithm corrects the MOD estimate. For those areas where MOD is expected to achieve its best performance (e.g., the Northern Great Plains), the impact of GRACE is less evident. The large change in north-west Pacific coastal regions may reflect the potential of GRACE to: (1) alleviate MODIS errors in mountainous regions; (2) correct parameters error in the observational function; and (3) reduce the influence of forcing bias in that area. However, it is difficult to identify the relative

contribution of these factors given the lack of evaluation tools (e.g., abundant station measurements).

SWE differences alone do not verify the MOD\_GR approach, so it is important to directly evaluate the MOD\_GR along with other simulations.

#### **4.5.2 Terrestrial water storage anomaly**

Figures 4.3 and 4.4 show the long term (Nov, 02 - May, 07) monthly TWS anomaly averaged over eight large river basins (shown in Figure 4.2) in North America, as simulated by OL, MOD, MOD\_GR and observed by GRACE. For those basins where boreal forests dominate, for example, the Mackenzie River basin and the Churchill & Nelson River basin, winter TWS is generally overestimated by MOD and OL relative to GRACE in the first two years (Nov, 02-Apr, 04). The MOD\_GR run agrees better with GRACE. Because the winter TWS anomaly is mainly attributed to SWE in those regions (Niu et al., 2007), these results correspond well to the SWE difference depicted in Figure 4.1. In the following winters, the difference between GRACE and OL/MOD may vary, but as expected, MOD\_GR agrees better with GRACE than the other two simulations.

In the Saint Lawrence and Fraser River basins, where the snow classes (Sturm, 1995) are maritime and alpine, respectively, results are comparable to those above. Overestimation of TWS (especially in Fraser) by MOD in most winters reveals the deficiency of MODIS updates in these geographic environments (related to vegetation cover and/or mountains). The poor performance of MOD in the Fraser River basin may be due to forcing or parameters errors, because the SCF signal should be responsive to SWE variations in that mountainous area.

In the Yukon River basin, all estimates agree reasonably well with each other except for a closer match between MOD\_GR and GRACE in the winter of 2007. Spatial heterogeneity of the SWE differences shown in Figure 4.1 may explain this agreement, which is: overestimation of MOD relative to MOD\_GR in the northern part is offset by underestimation in the south. The agreement in the Columbia River basin may have different reasons, such as high quality forcing, reliable connection between SCF and SWE as described by the observation function, and accurate treatment of MODIS error in the ensemble approach. The hydroclimatologic conditions in this river basin have been studied intensively, and my analyses as to the reliability of the forcing data and SCF parameterization in this region support the above attribution. Details are not presented here.

In the North Central and Missouri River basins, where MOD has been found to perform well in this region of flat topography, low vegetation and unsaturated SCF (Su et al., 2008), MOD and MOD\_GR TWS estimates are similar to each other, and to GRACE. In particular, Figure 4.4 shows an increase of TWS in the first two winters over the Missouri river basin in MOD and MOD\_GR relative to OL, presumably from the increase of the SWE estimate as validated by Su et al. (2008) with independent satellite datasets. Overall, these results imply that the MODIS data have well constrained the SWE simulation in these two basins where GRACE has had little impact, though it does not degrade the SWE estimates.

### 4.5.3 Climatologic monthly SWE and snow depth

SWE and snow depth estimates generated by different simulations are directly evaluated through their comparison with the CMC monthly climatology. My experiments estimate a climatology of SWE for five consecutive winters, as limited by the relatively short length of satellites data.

Figure 4.5 shows the difference of (multi-year) average April SWE (mm) between simulation result (MOD\_GR, MOD and OL) and CMC. In the central northern areas, the CMC SWE is systematically lower than model or data assimilation values. However, in many places (especially in high latitudes), the difference between CMC and MOD\_GR is significantly smaller than that between CMC and MOD. Those improvements over MOD across the boreal forest are consistent with those shown in the TWS anomaly comparison (Figures 4.3 and 4.4). These effects are most prominent in the southern Mackenzie River basin, the south-west rim of Hudson Bay, the center of the Churchill & Nelson River basin, and north of the Rocky Mountains. The OL has a comparable or even better agreement than MOD\_GR in a significant portion of the (central) high latitude areas as displayed in the figure. In the mid-latitude part of the domain the differences among OL, MOD, and MOD\_GR are much less significant (e.g., the Columbia River basin, where the results agree with the pattern shown in Figure 4.4). Similar to what were shown in Su et al. (2008), in some boreal forest regions, MOD SWE differs from CMC by a much larger magnitude than the difference between OL and CMC, indicating that in some locations the MODIS snow data assimilation system may degrade results relative to OL, probably owing to structural problems in the observation function (e.g., negligible correlation between SCF and SWE, parameters error) or other components. Similar

effects brought by model deficiencies have been documented previously (Zaitchki et al., 2008).

Table 4.1 gives the mean absolute error (MAE) of monthly SWE (mm) from January to June at eight river basins (in middle and high latitudes) in North America. MAE is calculated in each river basin and month by averaging the absolute difference between simulation results and CMC (monthly) over grids in that river basin. A significance test of MAE is performed and the superscripts show that MOD\_GR and OL have significantly lower MAE (t-test, p-value < 0.01) than some of their counterparts in associated river basins and month. In the Columbia River basin, the errors of three experiments are not distinguishable at p<0.01 level for all months (Jan to Jun). In North Central, Missouri and Saint Lawrence MOD\_GR (also MOD, not shown here) have significantly lower MAE than does OL. Also MOD\_GR has consistently lower error than MOD in Saint Lawrence. MAE results between MOD and MOD\_GR in high latitude areas are similar to that in Figure 4.5, indicating consistently better performance of MOD\_GR over MOD there. In some high latitude river basins (e.g., Mackenzie, Churchill & Nelson and Yukon) and given months, OL can have either indistinguishable or better performance than MOD\_GR and in most of these areas OL also performs better than MOD. Together with Figure 4.5, these results indicate potential deficiencies in the MOD\_GR experiment. In particular, the bias and variance magnitude of GRACE observational error could be important. As indicated in Wahr et al., 2006, GRACE error variance is probably latitude dependent, diminishing at high latitudes where satellite track density increases. A spatially uniform error variance was assumed for GRACE TWS in this research. Other problems associated with GRACE estimates, such as bias and spatial

leakage, including leakage of tide model errors from adjacent oceans may be important. Another recognized error source is the diminished variance introduced by smoothing GRACE data to suppress noisy spherical harmonics at high degree. Such problems may contribute to poor performance relative to OL. Further improvement of GRACE estimates including bias correction and regional error magnitude (variance) description are appropriate, but outside the scope of this paper.

Seasonal variations (from Nov to Jun) of SWE and snow depth (climatological values) for selected rectangular areas are shown in Figure 4.6 and Figure 4.7. Upper panel of Figure 4.6 shows an area located south of Hudson Bay, comparing the performance of MOD and MOD\_GR for a northern densely vegetated region. From mid December, MOD simulated SWE and snow depth are larger than MOD\_GR and OL, with the difference peaking in March or April and then gradually decreasing. The benchmark CMC curves are well mimicked by the MOD\_GR run. MOD estimates tend to be closer to CMC than to OL during the melting season (May), demonstrating the recovery of MODIS capability for monitoring snowpack mass variation as the SCF falls far below 100%. Figure 4.6 lower panel shows an area located in the central prairies region. OL significantly underestimates snowpack, as shown in Su et al. (2008), and MOD\_GR uniformly agrees better with CMC than does MOD, suggesting that contribution of GRACE in mid-latitudes may be location and scale dependent. Even at the large basin scale, there is a need for a more comprehensive assessment of the GRACE contribution when MODIS performance is adequate. This issue is discussed in section 4.6.2.

Figure 4.7 gives another comparison in two different places: Upper panel, 62°–68 ° N, 120° –130°W; Lower panel, 55°– 60° N, 100° –110°W. Similar patterns are shown in these two places, in which MOD\_GR and OL are both better than MOD and are close to each other. The OL could be slightly better in Feb, Mar and Apr. These features are consistent with those analyzed in Table 4.1, reflecting considerable room for refinement of MOD\_GR in those areas.

## 4.6 DISCUSSION

### 4.6.1 Role of the auto-covariance of SWE ensemble

It has been shown that GRACE TWS data can have a substantial influence on snowpack estimates over many high-latitude and some mid-latitude regions. The key elements that affect how GRACE contributes in an ensemble context include its fundamental nature as a measure of total column water storage, and its coarse spatial and temporal resolution. According to Equations (4.1) and (4.2), the covariance between the analyzed variable, SWE, and the simulated TWS largely controls the magnitude of the EnKS increments given the unit innovation. This covariance (in scalar form) can be explicitly expanded as:

$$Cov(X_{t,l,SWE}, X_{T1,L1,TWS}) = Cov(X_{t,l,SWE}, \overline{\sum_{ii=1}^N \sum_{li=1}^M X_{ii,li,SWE}}) + Cov(X_{t,l,SWE}, \overline{\sum_{ii=1}^N \sum_{li=1}^M X_{ii,li,SM}}) + Cov(X_{t,l,SWE}, \overline{\sum_{ii=1}^N \sum_{li=1}^M X_{ii,li,wa}}) \quad (4.5)$$

where  $X_{ii,li,SWE}$ ,  $X_{ii,li,SM}$ ,  $X_{ii,li,wa}$  represent SWE, total soil moisture and aquifer water storage at day  $ti$ , land tile  $li$ , in month  $T1$  (with N days), and GRACE footprint L1

(with M model grids), respectively.  $X_{T1,L1,TWS}$  represents monthly (T1) average TWS over L1. The symbol  $\overline{\sum\sum}$  represents spatial and temporal averaging. The other symbols have the same meaning as before. Here the decomposition of TWS neglects canopy snow for simplicity. If further simplify equation (4.5) by only considering zero-lag covariance parts of the second and third terms on the right side, it becomes

$$Cov(X_{t,j,SWE}, X_{T1,L1,TWS}) \approx Cov(X_{t,j,SWE}, \overline{\sum_{ii=1}^N \sum_{ll=1}^M X_{ii,ll,SWE}}) + Cov(X_{t,j,SWE}, X_{t,j,SM}) + Cov(X_{t,j,SWE}, X_{t,j,wa}) \quad (4.6)$$

Although incomplete, this expression provides a first-order estimate of the covariance between daily SWE at any grid and the GRACE data, in particular for the accumulation season. It assumes that soil moisture and groundwater anomalies are temporally and spatially not well connected to the SWE anomaly before snow melts (a separate calculation of the lagged correlation between SWE and the other two TWS components supports this assumption, but is not shown here).

Figure 4.8 provides a monthly composite description of the cross-correlation between SWE and the other two TWS components (the second and third terms in the right side of equation (4.6)) in February, 2003; other months before strong melting show similar results. Only in those colored areas, is there a significant correlation (p value < 5%) for more than two days in February. It is shown that over most of the domain both correlation fields are not significant for a majority of days within that month. This implies that the auto-correlation of SWE (the first term on the right side of equation (4.6)) largely determines the magnitude of GRACE information that can be utilized by CLM.

#### 4.6.2 Ensemble variance reduction by assimilating GRACE

By design, the EnKS reduces ensemble error by combining observations with model estimates. Thus it is valuable to analyze error reduction (or some related quantity) by GRACE in the multi-sensor data assimilation framework. In addition the relevant metric can contribute to understanding the GRACE effects in regions where MODIS alone provides considerable improvement. The TWS anomaly shown in Figure 4.4 (the Missouri River basin and North Central River basin) may be inconclusive for this purpose.

This work uses the following statistic, an effectiveness ratio  $\rho$  to define ensemble variance reduction capability (in scalar form) of GRACE:

$$\rho = \frac{\text{Var}(X_{SWE}^b) - \text{Var}(X_{SWE}^a)}{\text{Var}(X_{SWE}^b)} \quad (4.7)$$

where  $X_{SWE}^b$  and  $X_{SWE}^a$  are background and analysis SWE ensembles in the EnKS. Also note that  $X_{SWE}^b = X_{SWE}^a(EnKF)$ . Note that here one can't directly calculate the ensemble error because the ensemble may have bias. Also there is no high-quality observation to quantify ensemble error. Equation (4.7) provides a purely ensemble based statistic, which may, to some extent, be an indicator of uncertainty reduction from the EnKS. With this in mind, the normalized index facilitates inter-comparison of GRACE's ensemble variance reduction capability (to the SWE ensemble) among different regions. Its theoretical value ranges from 0 (no reduction in ensemble variance) to 1 (strongest capability for reduction of ensemble variance). To minimize influence of sampling error

in calculating  $\rho$  with equation (4.7), the daily river basin averaged values of  $\rho$  has been derived. Figure 4.9 provides the results for two river basins, the Mackenzie and North Central, from Jan, 2002 to Jun, 2002.  $\rho$  in the Mackenzie River basin is systematically larger than that at mid-latitudes, and its average effectiveness ratio can reach 25% in April, but decreases in the melting season when the MODIS capability returns. In the North Central River basin this ratio is consistently below 10% and without evident seasonal variation. Other boreal forest, tundra (compared to the Mackenzie River basin) and mid-latitude flat regions (compared to the North Central River basin) have similar patterns as shown here. However, results in mountainous regions are less consistent. It is argued that  $\rho$  (for a large basin average) is also a function of the spatial correlation structure of the MODIS updated ensemble within the GRACE footprint, considering the spatial aggregation nature of GRACE. Further explanation of spatial and seasonal variations of  $\rho$  is the subject of continued research.

#### **4.7 CONCLUDING REMARKS**

This study develops a continental scale multi-sensor snow data assimilation system that assimilates both GRACE TWS and MODIS SCF information into CLM with the EnKS and EnKF, respectively. Through this new framework, various deficiencies associated with MODIS-only data assimilation are effectively corrected domain wide. These improvements result from the unique information from GRACE, which provides complementary constraints on the ensemble simulation for various climatic and geographical locations. In addition, in those regions where MODIS performs adequately, inclusion of GRACE TWS information does not degrade the estimates, further indicating

robustness of this joint assimilation system. Comparison of MOD\_GR and OL reveals more complex patterns. In the North Central, Missouri, and Saint Lawrence river basins, MOD\_GR is consistently better than OL. In Fraser and Yukon river basins, MOD\_GR is better than or comparable to OL. In the Mackenzie, Churchill & Nelson river basins OL can have comparable or better performance than MOD\_GR. These features demonstrate a need to improve the GRACE data assimilation approach, including improved characterization of GRACE bias and error variance.

I also found that measurement of total column water storage (integrating several water storage components), and the coarse spatial and temporal resolution of GRACE may both benefit and complicate the task of estimating SWE. The impacts of these characteristics on the EnKS update deserve further investigation. Advantages of the finer resolution of MODIS data in the multi-sensor system may need more detailed analyses in order to better characterize the different features associated with each data type and their interaction in the multi-sensor data assimilation framework.

Table 4.1 The mean absolute error (MAE) of monthly SWE (mm) from Jan to Jun at eight river basins in North America for three experiments. The superscripts represent that a specific experiment has significantly lower MAE (t-test, p-value < 0.01) in associated river basin and month than some of its counterparts. In particular, **(a)** - MOD\_GR MAE is significantly lower than that of both MOD and Open Loop; **(b)** - MOD\_GR MAE is only significantly lower than MOD; **(c)** - MOD\_GR MAE is only significantly lower than Open Loop; **(d)**- Open\_Loop MAE is significantly lower than that of both MOD and MOD\_GR; **(e)** – Open Loop MAE is only significantly lower than MOD.

<b>Columbia</b>	Jan	Feb	Mar	Apr	May	Jun
MOD_GR	34.2	48.6	48.1	36.2	27.4	2.4
MOD	36.9	46.1	47.0	32.8	24.8	4.0
Open_Loop	38.6	50.0	53.2	38.3	26.0	2.5
<b>Fraser</b>						
MOD_GR	<b>53.3<sup>(b)</sup></b>	<b>68.8<sup>(b)</sup></b>	<b>89.3<sup>(a)</sup></b>	<b>116.2<sup>(b)</sup></b>	<b>62.1<sup>(a)</sup></b>	<b>12.6<sup>(a)</sup></b>
MOD	62.4	86.5	104.1	137.2	68.2	30.9
Open_Loop	<b>50.7<sup>(e)</sup></b>	74.9	103.0	126.8	86.0	21.6
<b>Saint Lawrence</b>						
MOD_GR	<b>12.6<sup>(a)</sup></b>	<b>18.2<sup>(a)</sup></b>	<b>23.8<sup>(a)</sup></b>	<b>32.8<sup>(a)</sup></b>	<b>12.1<sup>(a)</sup></b>	2.2
MOD	23.1	29.1	36.5	47.2	21.8	4.1
Open_Loop	37.8	35.3	50.8	68.2	22.6	2.0
<b>Mackenzie</b>						
MOD_GR	<b>27.7<sup>(a)</sup></b>	<b>23.3<sup>(a)</sup></b>	<b>26.5<sup>(a)</sup></b>	<b>67.8<sup>(b)</sup></b>	<b>36.3<sup>(b)</sup></b>	<b>8.8<sup>(b)</sup></b>
MOD	39.1	39.6	53.5	86.6	46.2	22.0
Open_Loop	46.5	37.8	41.7	<b>58.89<sup>(e)</sup></b>	<b>26.2<sup>(d)</sup></b>	<b>4.7<sup>(e)</sup></b>
<b>Churchill &amp; Nelson</b>						
MOD_GR	<b>21.6<sup>(b)</sup></b>	<b>26.9<sup>(b)</sup></b>	<b>42.1<sup>(b)</sup></b>	<b>58.1<sup>(b)</sup></b>	6.2	1.9
MOD	36.2	36.9	69.2	82.6	6.2	2.6
Open_Loop	29.1	<b>21.3<sup>(e)</sup></b>	<b>36.1<sup>(e)</sup></b>	<b>48.6<sup>(d)</sup></b>	6.3	1.3
<b>Yukon</b>						
MOD_GR	<b>52.8<sup>(c)</sup></b>	<b>46.2<sup>(a)</sup></b>	<b>52.1<sup>(a)</sup></b>	<b>58.6<sup>(b)</sup></b>	<b>33.9<sup>(a)</sup></b>	<b>26.1<sup>(b)</sup></b>
MOD	51.2	57.1	62.6	70.1	52.1	36.8
Open_Loop	63.1	62.4	68.3	<b>56.2<sup>(e)</sup></b>	59.8	<b>18.5<sup>(e)</sup></b>
<b>Missouri</b>						
MOD_GR	<b>18.0<sup>(c)</sup></b>	<b>20.9<sup>(c)</sup></b>	<b>12.9<sup>(c)</sup></b>	11.0	2.7	0.1
MOD	19.3	21.2	12.1	11.7	3.6	1.0
Open_Loop	27.6	29.6	21.3	10.2	2.7	0.1
<b>North Central</b>						
MOD_GR	<b>19.8<sup>(c)</sup></b>	<b>21.1<sup>(c)</sup></b>	<b>15.6<sup>(c)</sup></b>	4.1	0.1	0.0
MOD	16.2	18.2	12.1	3.7	1.5	1.2
Open_Loop	26.2	26.4	21.8	3.3	0.1	0.0

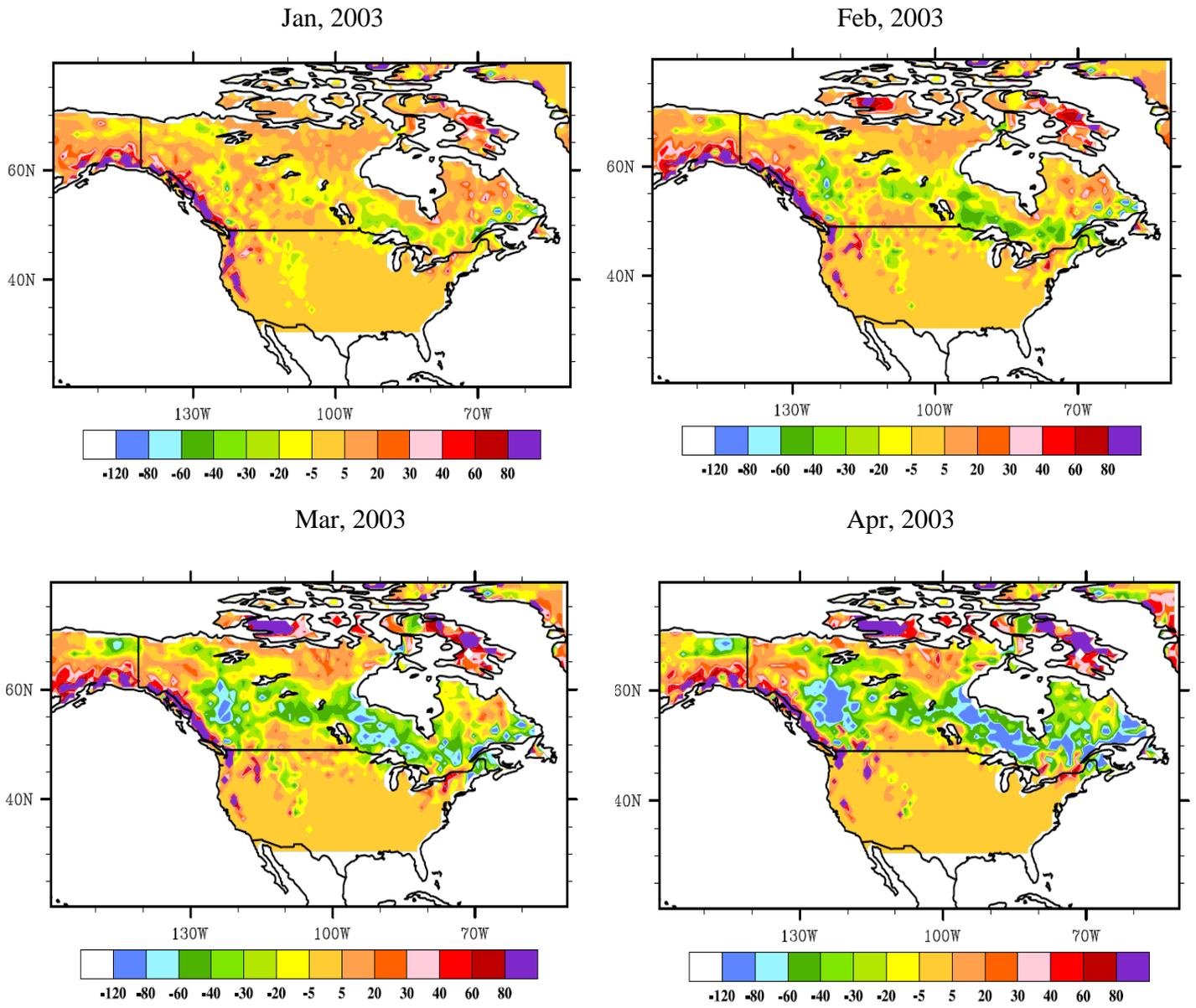


Figure 4.1. The difference of monthly SWE (mm) between MOD\_GR and MOD data assimilation experiments in the cold season of 2003.

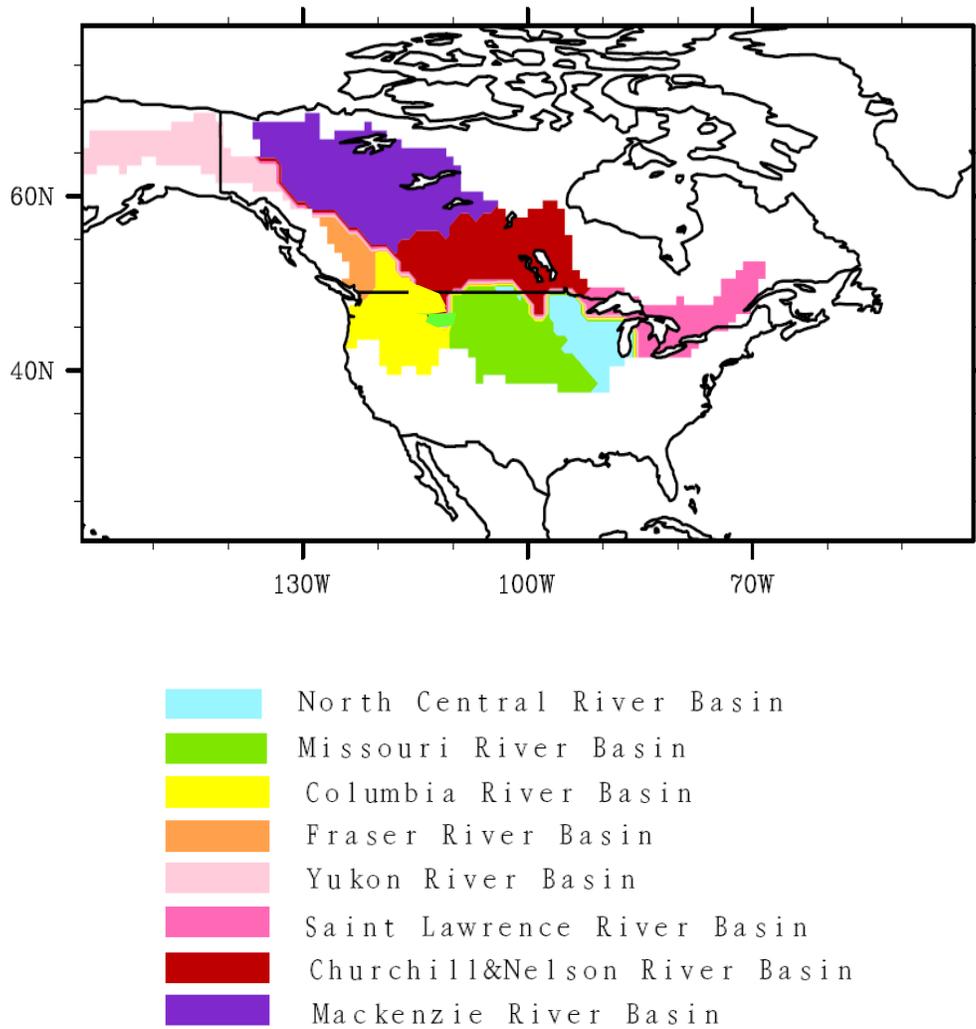


Figure 4.2. Eight river basins in North American that are analyzed.

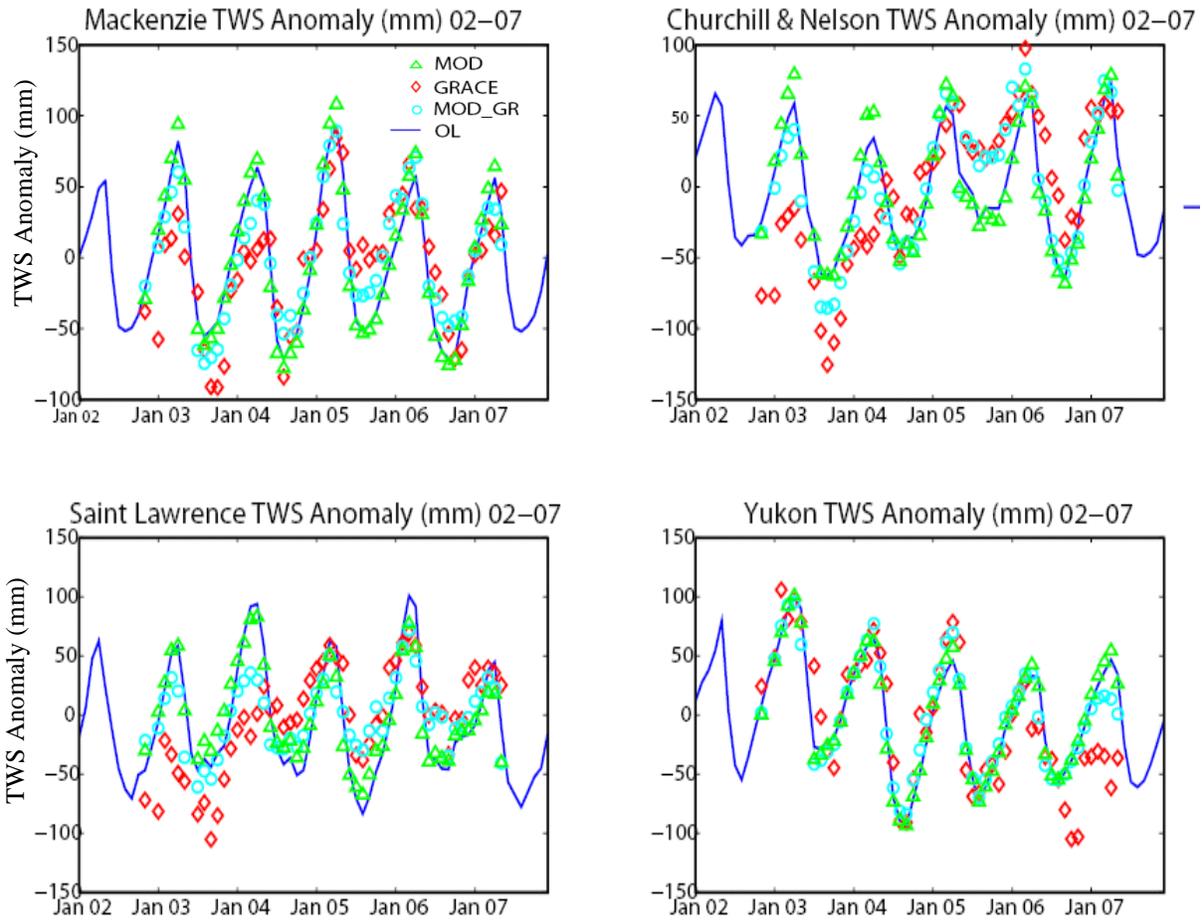


Figure 4.3. The monthly TWS anomaly (Nov, 2002-May, 2007) from the simulations: OL, MOD, MOD\_GR and the GRACE observation, averaged over four river basins in North America. In OL, the TWS anomaly in other months in the years of 2002 and 2007 are also shown for reference.

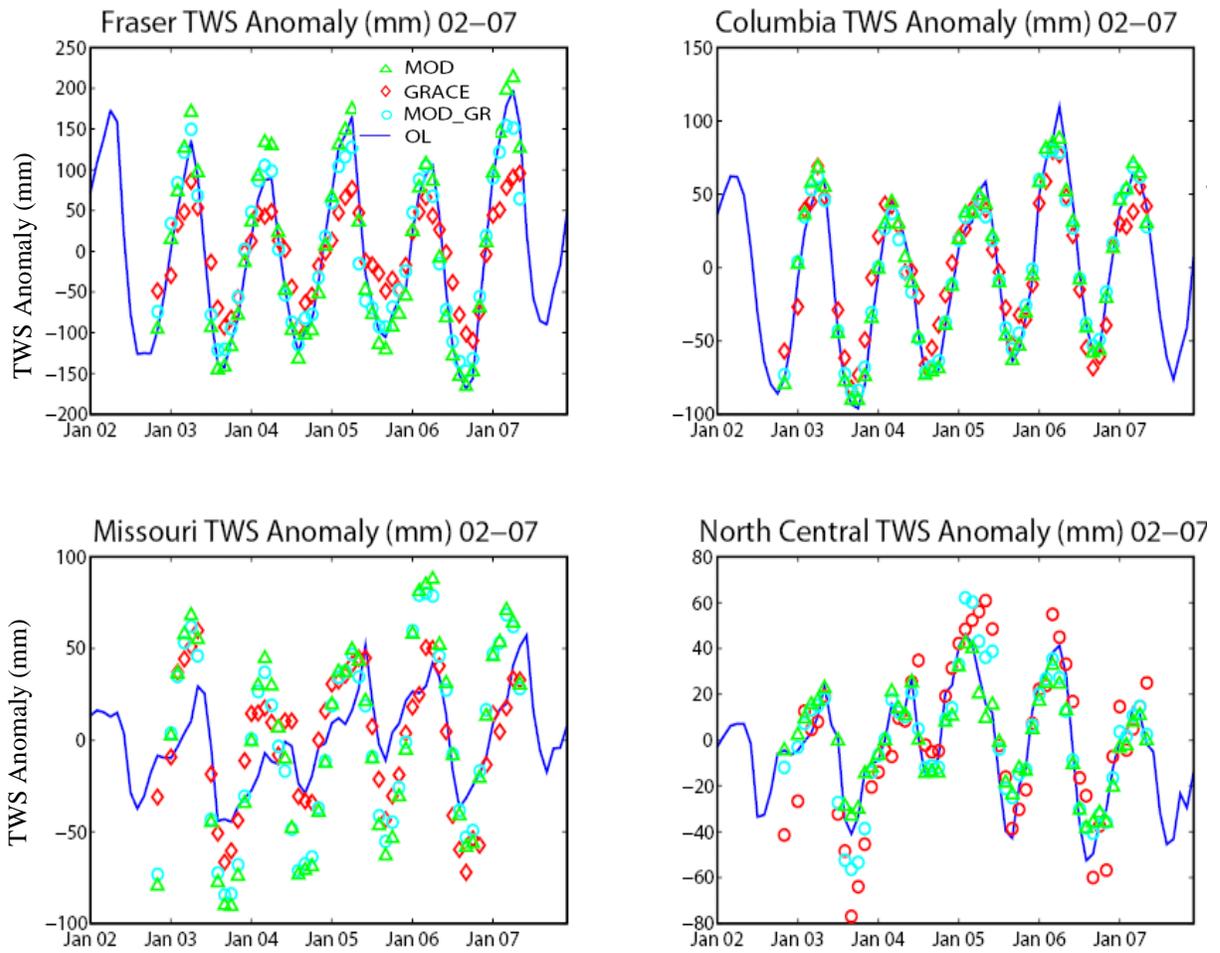
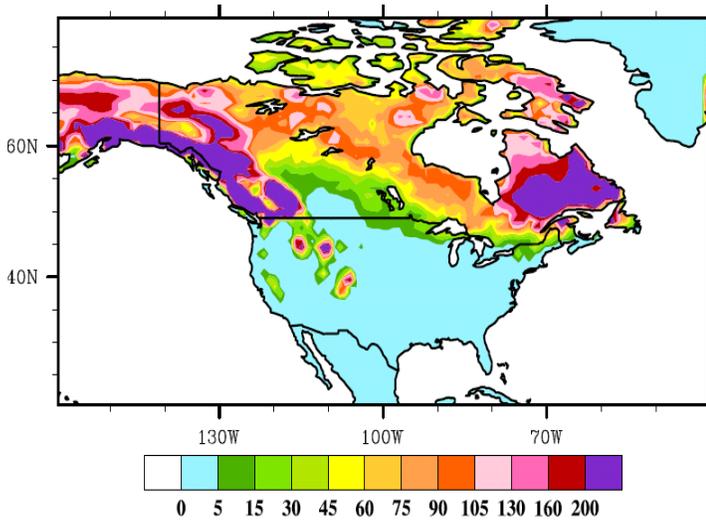


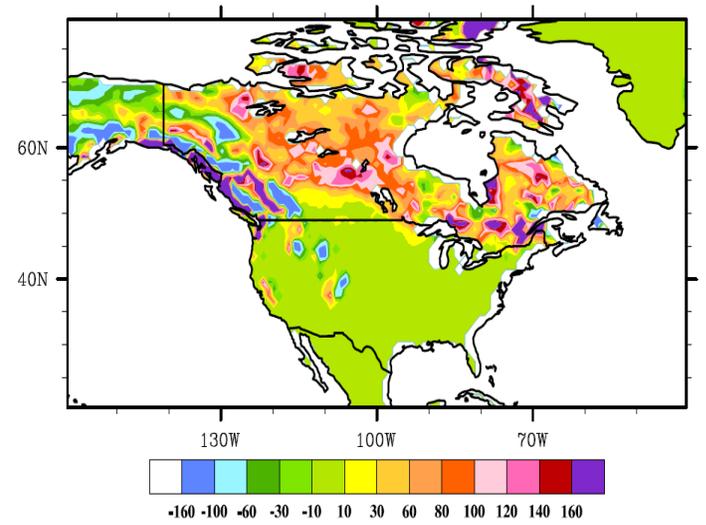
Figure 4.4. Same as Figure 4.3., but for another four river basins in North America.

CMC (Apr)

MOD\_GR – CMC (Apr)



MOD – CMC (Apr)



OL – CMC (Apr)

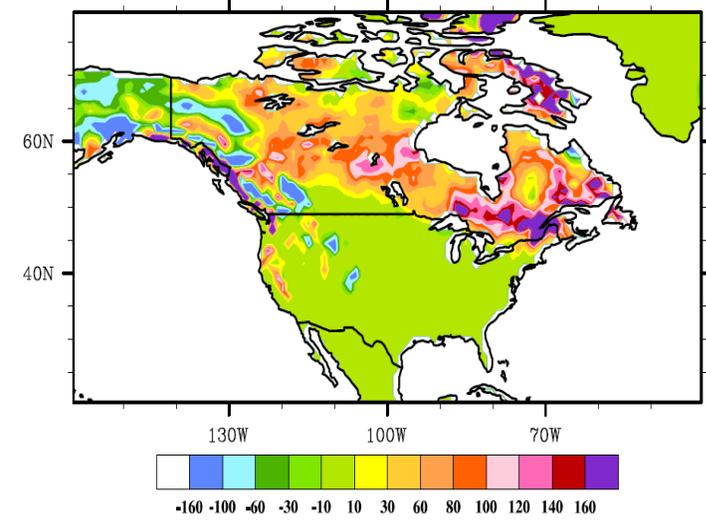
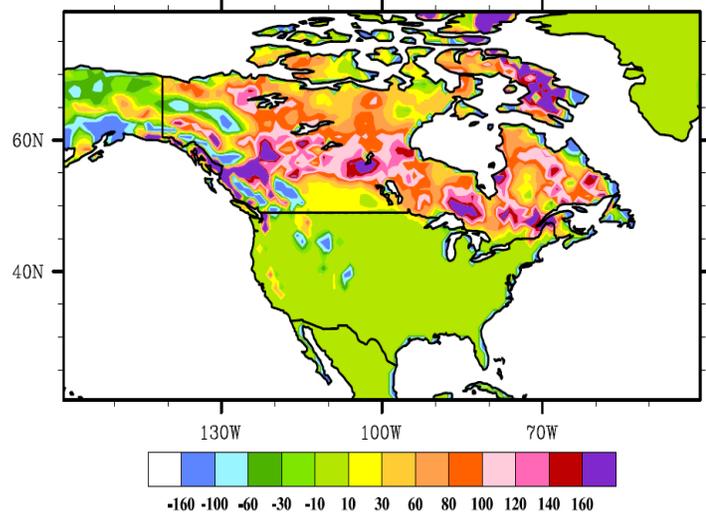


Figure 4.5. The difference of average Apr SWE (mm) between simulation result (MOD\_GR, MOD and OL) and CMC. CMC Apr SWE is given for reference.

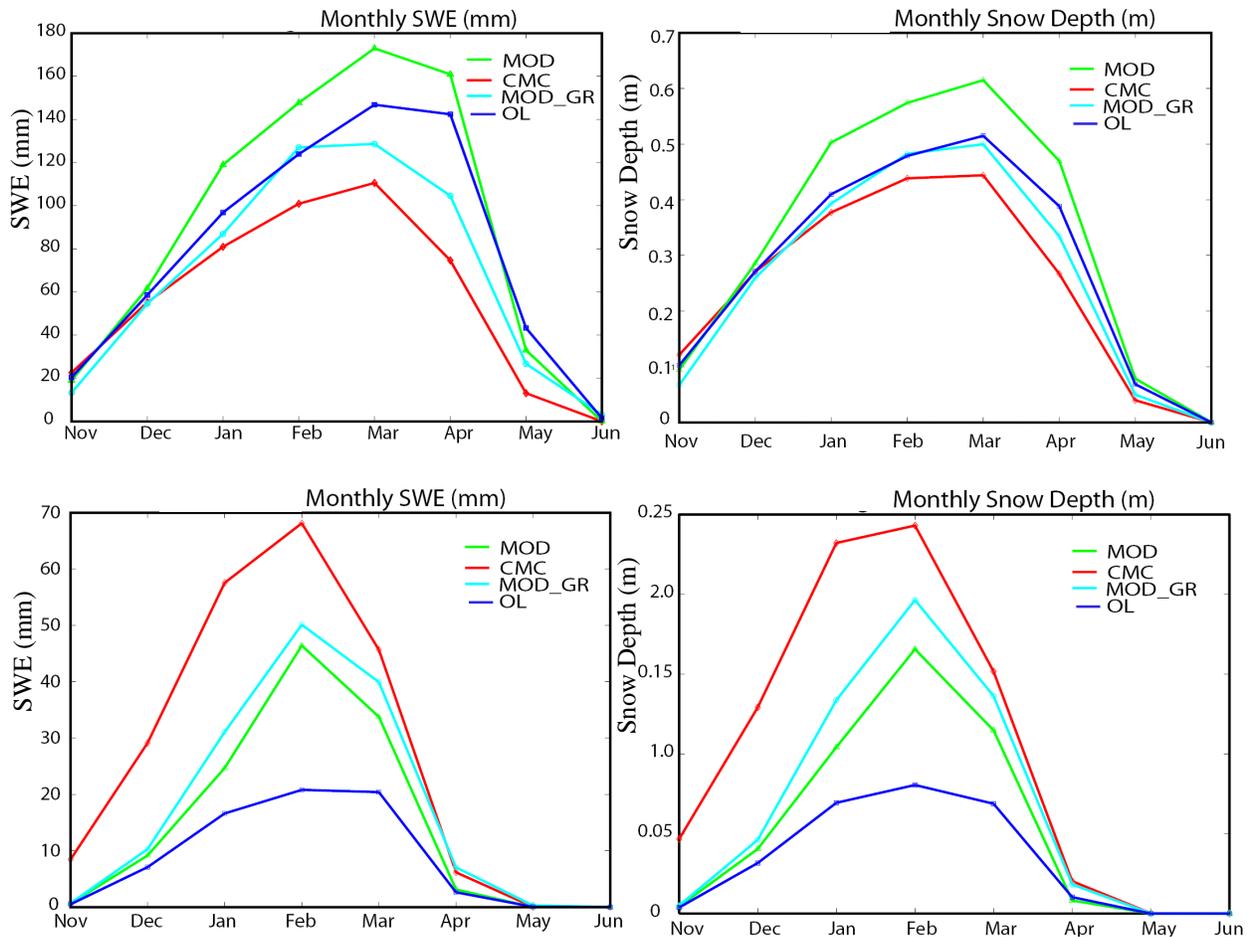


Figure 4.6. The climatological monthly mean SWE (mm) and snow depth (m) from Nov to Jun in two rectangular regions for the simulations (MOD, MOD\_GR and OL), and the CMC long term observation data. Upper panel: (A)  $51^{\circ}$ – $55^{\circ}$  N,  $94^{\circ}$  – $85^{\circ}$ W; Lower panel: (B)  $46^{\circ}$ –  $49^{\circ}$  N,  $98^{\circ}$  – $94^{\circ}$ W. See the rectangular boxes in Figure 4.8 for their locations.

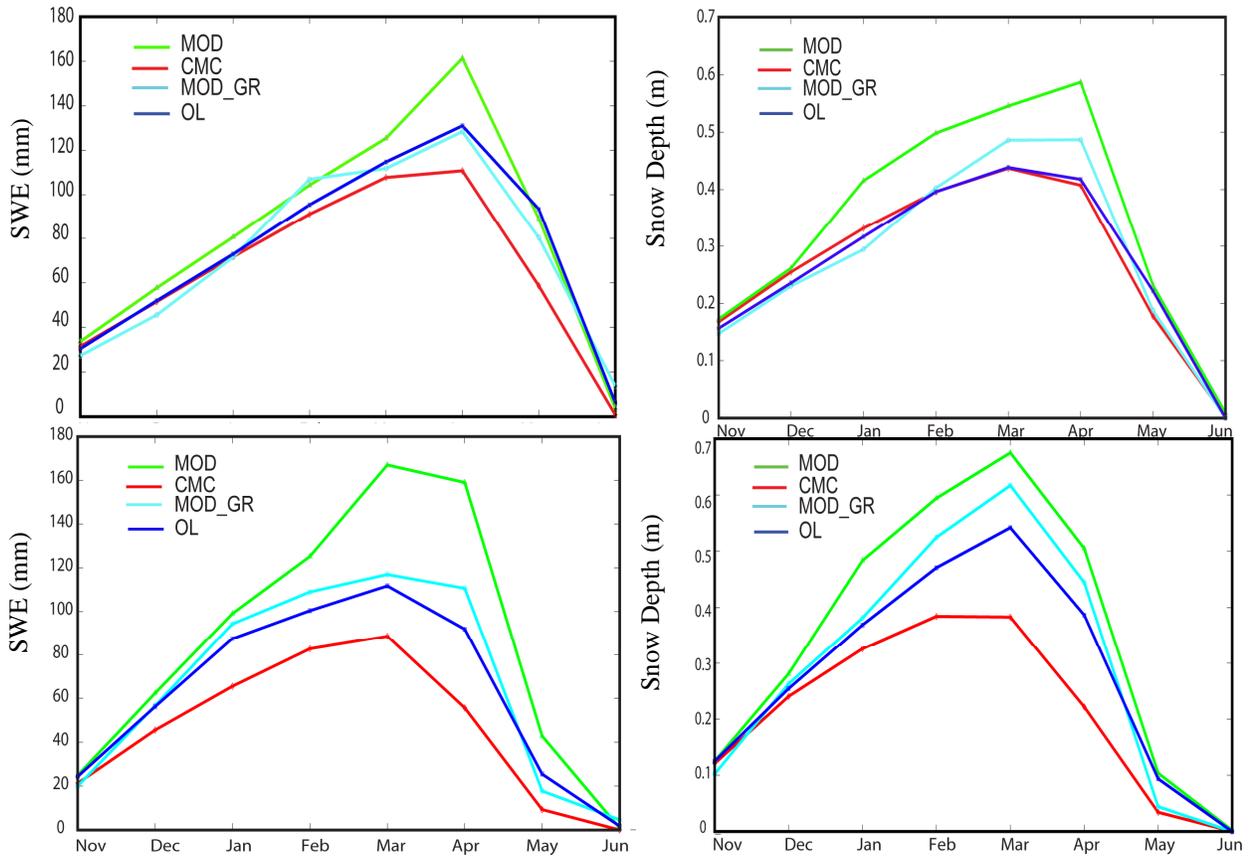


Figure 4.7. Same as in Figure 4.6 but for different locations. Upper panel: (C) 62°–68° N, 120°–130°W; Lower panel: (D) 55°–60° N, 100°–110°W. See the rectangular boxes in Figure 4.8 for their locations.

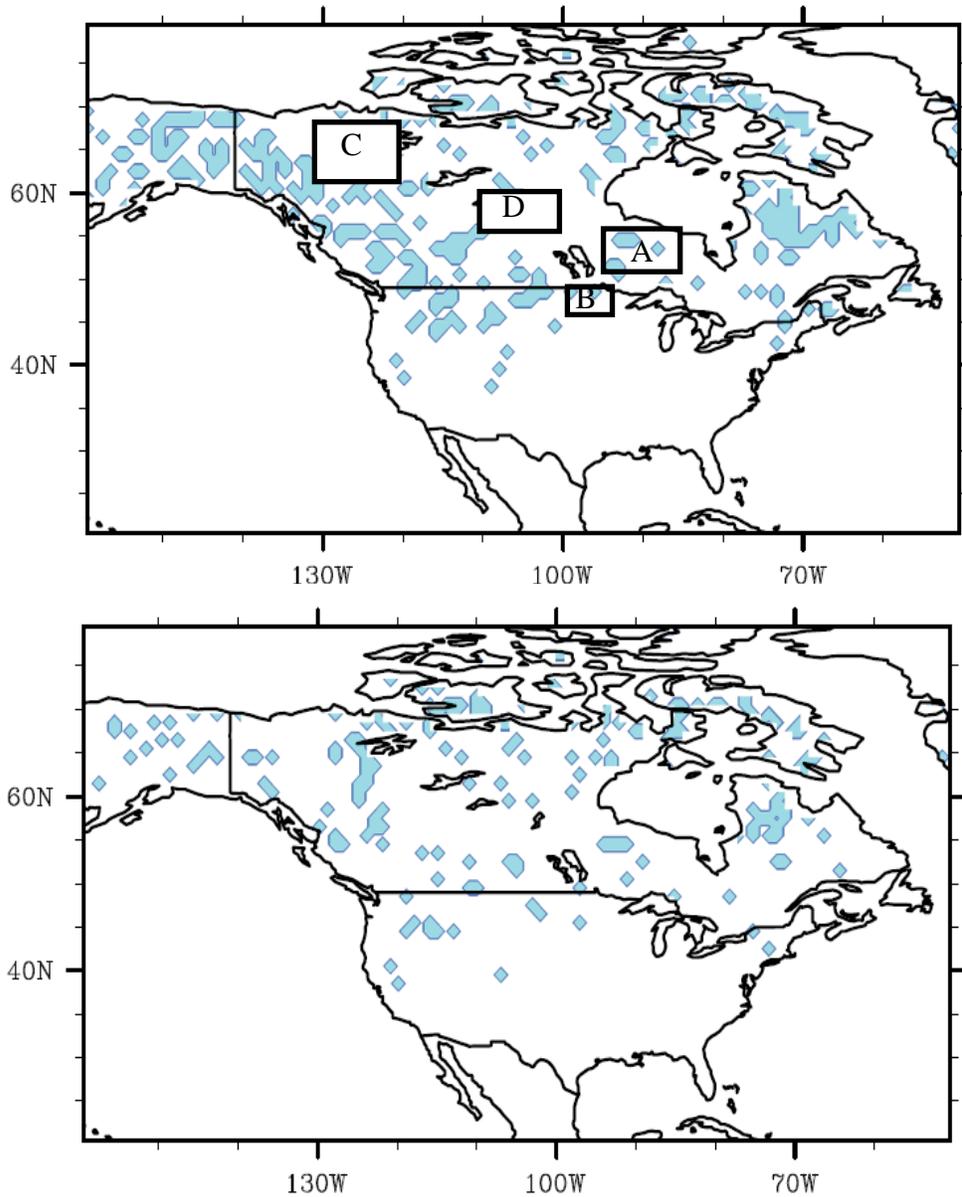


Figure 4.8. In those colored grids, the number of the days in which the corresponding daily correlation (zero temporal and spatial lag) between (1) SWE and soil moisture (upper) (2) SWE and groundwater (lower) is significant ( $p$  value  $< 5\%$ ) exceeds two in February 2003.

Using a lower standard in the  $p$ -value test (e.g.,  $p$  value  $< 10\%$ ) didn't change these two colored maps significantly (remain almost same). Rectangular boxes in the upper panel are for Figure 4.6, 4.7.

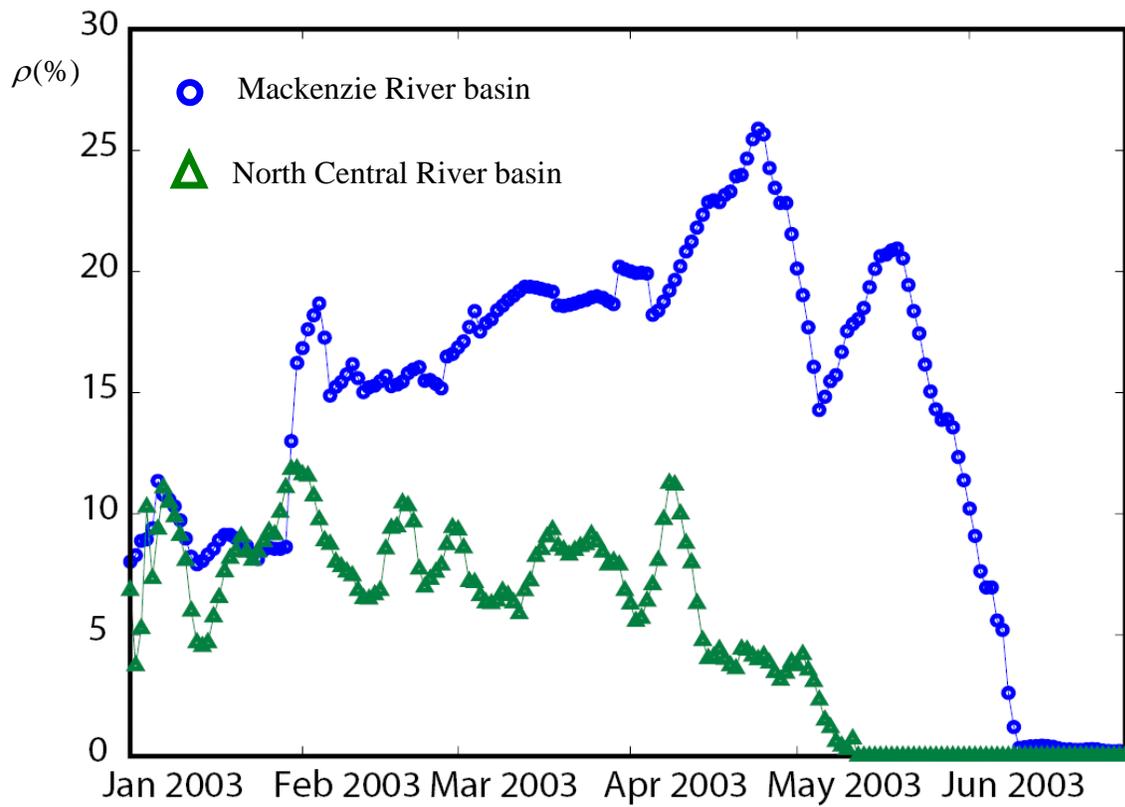


Figure 4.9. The daily river basin averaged  $\rho$  (%) (equation (4.7)) from Jan to Jun 2003, for the Mackenzie River basin and the North Central River basin.

## **Chapter 5: Conclusions and future work**

### **5.1 SUMMARY**

The three studies described above are all devoted to developing improved ensemble data assimilation approaches and strategies for estimating large-scale snowpack properties (e.g., SWE, snow depth). Each study focuses on a specific aspect. Chapter 2 plays the role of “proof-of-concept” that first expands the EnKF SCF data assimilation to a continental-scale. With this novel platform, new observation function and filter characteristics are evaluated and interpreted on a new level. Following this initial test, a more theoretically inclined topic is explored in Chapter 3, which tackles parameter and model structure errors in the ensemble snow data assimilation system. Knowledge gained from this chapter paves the way to more advanced large-scale snowpack estimation practice in data-sparse areas where the true (or most appropriate) parameter and/or model parameterization are poorly known. Chapter 4 concentrates on multi-sensor data assimilation in the North American domain, where various observations are blended in an approach incorporating both EnKF and EnKS. This study is partially motivated by findings in Chapter 2 (the relatively poor performance in the boreal forest for MODIS SCF data assimilation), and the comparison and contrast of these two studies leads to valuable ramifications for large-scale ensemble snow data assimilation.

The major original findings and conclusions in each chapter are summarized below.

In Chapter 2 it is demonstrated that MODIS SCF observation can be used to estimate SWE at a continental-scale (North American) more precisely through the EnKF

approach. The potential of a newly developed SCF observation function has been assessed, which shows that it can fit the specific needs of large-scale SWE estimation. The data assimilation performance is found to be region dependent, where the climatic and geographic (e.g., topography and vegetation) features can play an important role. The largest improvements of EnKF experiment are in the mountainous West, the Northern Great Plains, and the West and East Coast regions. In given areas, the MODIS assimilation run can reduce the error of Open Loop from twice the standard deviation (calculated from climatology) to within one standard deviation. However, the MODIS EnKF approach is shown to perform poorly in boreal forests. In addition, the EnKF statistics (innovation mean and mean of normalized innovation variance) have been calculated and interpreted at domain wide. It is found that in middle-latitude areas there are significant bias and misrepresentation of model error.

In Chapter 3 two parameters, the melting exponent in a SCF parameterization and liquid water holding capacity, have been used to mimic parameter error in the EnKF data assimilation. In presence of parameter error, the error in SWE estimation could be 100+ mm with a low *Nash-Sutcliffe* efficiency (0.22 for ensemble mean simulation), even though measurements are assimilated. Incorporation of parameter estimation in traditional EnKF could increase *Nash-Sutcliffe* efficiency to 0.96 (with 0.98 the theoretical limit) and significantly reduce the SWE error. The energy balance related variables are also estimated more accurately when performing parameter estimation. Another experiment reveals that parameter estimation could diverge in the presence of model structural error. It is speculated that the structural problem can undermine the observation's capability of leading to stable parameter retrieval. In the perfect-model-

structure scenario, parameter estimation converges and is not affected by the change of variance of the parameter ensemble.

In Chapter 4, snow areal extent related observations (MODIS SCF) and mass related observations (GRACE TWS) are blended into CLM for SWE and snow depth estimation. It is found that the integrated EnKF and EnKS approach can adequately cope with different features in these two datasets, for example, the discrepancy in their spatial and temporal scales. This GRACE/MODIS data assimilation run achieves a significantly better performance than the MODIS only run in Saint Lawrence, Fraser, Mackenzie, Churchill & Nelson, and Yukon river basins. These improvements demonstrate the value of integrating complementary information for continental-scale snow estimation, especially, by incorporating TWS observation from GRACE. In middle latitude river basins (e.g., North Central and Missouri) the multi-sensor approach preserves the advantages (compared with Open Loop) shown in the MODIS only run. Further analyses show that the auto-correlation of the SWE ensemble largely controls the magnitude of GRACE information that can be absorbed by CLM. Also the capacity of GRACE observation in reducing the SWE ensemble variance (a surrogate of estimation error) is assessed at river basin scale, with a first-order result showing that this capacity is larger in high latitude flat areas than in middle latitude flat areas.

## 5.2 FUTURE WORK

There are many limitations and constraints revealed in the above investigations. In general, research presented in this dissertation can be expanded and improved by investigating the following issues.

(1) Characterization of observation error. In two satellite datasets involved studies (Chapters 2 and 4), the observation errors are specified in a simple way which, in some region and period, could significantly depart from the true value. MODIS SCF data may have large uncertainties in forest and mountain areas, and GRACE TWS error may be latitude dependent. In Chapter 4 it is hypothesized that, the simple treatment of TWS error could be responsible for the indistinguishable or even degraded performance of multi-sensor runs when compared to the Open Loop run over some high latitude areas. It is recommended to incorporate spatially and temporally distributed estimates of observation errors, and evaluate their impacts on data assimilation performance.

(2) Representation of spatial and temporal structures of large-scale meteorological forcing errors. As highlighted in Crow and Van Loon (2006), accurate description of forcing (or model) error magnitude could be paramount to a land data assimilation system. Durand and Margulis (2006) also showed the importance of spatial covariance of precipitation error in an ensemble snowpack estimation experiment. In Chapter 2, it is found the forcing errors are misrepresented in middle latitude areas. In Chapter 4, the auto-correlation of SWE is demonstrated to be important to GRACE information absorption. This ensemble metric is a function of the spatial correlation structure of forcing data (e.g., precipitation and temperature). That said, how to simulate these forcing errors adequately at continental to hemispheric scale is not covered in this dissertation

and previous research. Solid precipitation data error might be linked to the feature of large-scale frontal systems in winter. In addition, these forcing data errors are largely related to the way they are generated (e.g., the production of reanalysis data through blending multiple sources like satellite observation and coupled GCM simulation). Therefore great efforts are needed to derive dependable algorithms that can better quantify these forcing error structures.

(3) Adaptive filter algorithm that can more efficiently transform information in satellite observation (e.g., GRACE TWS) to model simulation. This requirement is related to the increasing computational demand when higher resolution LSMs are used in snow data assimilation. My study reveals that the effectiveness of GRACE assimilation might vary regionally, with given areas affected insignificantly. Also it might not be necessary to assimilate MODIS SCF information at daily frequency considering the memory of snow cover in given season and area. Although mechanisms that control the regionally and temporally dependent filter performance are not yet clear, it can be speculated that an adaptive approach that can automatically determine the application of the EnKF could reduce both computational burden and sampling error. The EnKF update (of given observations) may not need at particular places or periods because its expected (theoretical) value is marginal. So it may be appropriate to adjust the size of areas (or temporal interval) involved in the ensemble update for a particular observation.

(4) Assimilation of range-rate data from GRACE satellite. Considering the limitations of current version of monthly GRACE TWS data (for example, the coarse temporal and spatial resolution, and the aliasing problems), assimilating range-rate variation along the satellite ground track could improve results. Range-rate data can form

local estimates of surface mass change near the ground track with variable temporal sampling intervals, and have spatial coverage depending on the details of ground tracks. These features potentially enable SWE estimation at high spatial and temporal resolutions. An Observation System Simulation Experiment (OSSE) is desirable to fully test the performance of range-rate data assimilation and the associated technical details.

(5) Generation of longer period (e.g., decadal) snowpack estimates using AVHRR satellite data. Currently the snowpack estimates span only several years, which are limited by the availability of MODIS and GRACE datasets. AVHRR provided SCF data from 1970s (although at coarser spatial resolution than MODIS). Using the same EnKF technology, these data can be assimilated to derive long-term snowpack estimates. These estimates could be useful for a wide range of applications, especially for evaluating long-term hydroclimatological change.

(6) Integration of ensemble snow data assimilation methods into coupled meteorological and/or climate models. As indicated in Chapter 1, one reason for developing snow products through data assimilation is to provide reliable boundary conditions for meteorological and climate simulation. All three chapters demonstrate that the characteristics (e.g., error magnitude) of SWE, snow depth and other snowpack estimates are largely controlled by the model features, for example, its numerical configuration, accuracy of parameters and structure, reliability of observational function, etc. So the integration of ensemble snow data assimilation methods into the meteorological and/or climate models (e.g., using the same LSM to assimilate observation and simulate snowpack related boundary states and fluxes in GCM) is promising to produce a seamless approach. Currently it is not clear how to develop a

computationally efficient way to achieve the above goal. There are further questions about the benefit of this approach for intra-seasonal to seasonal atmospheric simulation. The study toward this goal could be integrated into some community efforts that have potentially far-reaching impacts and cover wide range of scales and areas. For example, the Data Assimilation Research Testbed (DART) is a community facility for ensemble data assimilation developed and maintained by the Data Assimilation Research Section (DAReS) at the National Center for Atmospheric Research (NCAR). It includes multiple comprehensive atmosphere and ocean general circulation models (GCMs) and modular programming facility for ensemble data assimilation. The integration of the snow data assimilation component into this community platform can characterize the effects of optimized snow estimation to climate simulation.

## Appendix

### Abbreviations

AMSR-E	Advanced Microwave Scanning Radiometer-Earth
AVHRR	Advanced Very High Resolution Radiometer
CLM	Community Land Model
EnKF	Ensemble Kalman Filter
EnKS	Ensemble Kalman Smoother
GCMs	General Circulation Models
GLDAS	Global Land Data Assimilation System
GRACE	Gravity Recovery and Climate Experiment
MODIS	Moderate Resolution Imaging Spectroradiometer
NCAR	National Center for Atmosphere Research
NDSI	Normalized Difference of Snow Index
NRCS	Natural Resources Conservation Service
OSSE	Observation System Simulation Experiment
PDO	Pacific Decadal Oscillation
PFTs	Plant Functional Types
PNA	Pacific-North America (pattern)
SCF	Snow Cover Fraction
SDC	Snow Depletion Curve
SNOTEL	Snowpack Telemetry
SWE	Snow Water Equivalent
VIS/IR	Visible/Infrared

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